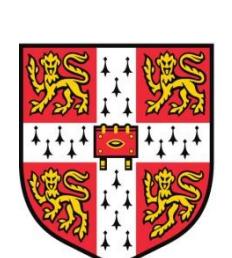


# Shrinkage Estimation of the SN Ia Host Galaxy Dust Law Distribution with a Hierarchical BayeSN SED model

Stephen Thorp, Kaisey S. Mandel,  
Suhail Dhawan, Ana Sofía M. Uzsoy, Sam M. Ward (IoA, Cambridge),  
Gautham Narayan (UIUC), Andrew S. Friedman (UCSD),  
Arturo Avelino (CfA, Harvard), David O. Jones (UCSC)

[Mandel, Thorp, Narayan, Friedman, Avelino, arXiv:2008.07538]

[Thorp, Mandel, Jones, Ward, Narayan, arXiv:2102.05678]



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# **Part I: SN Ia Cosmology and the Problem of Dust**

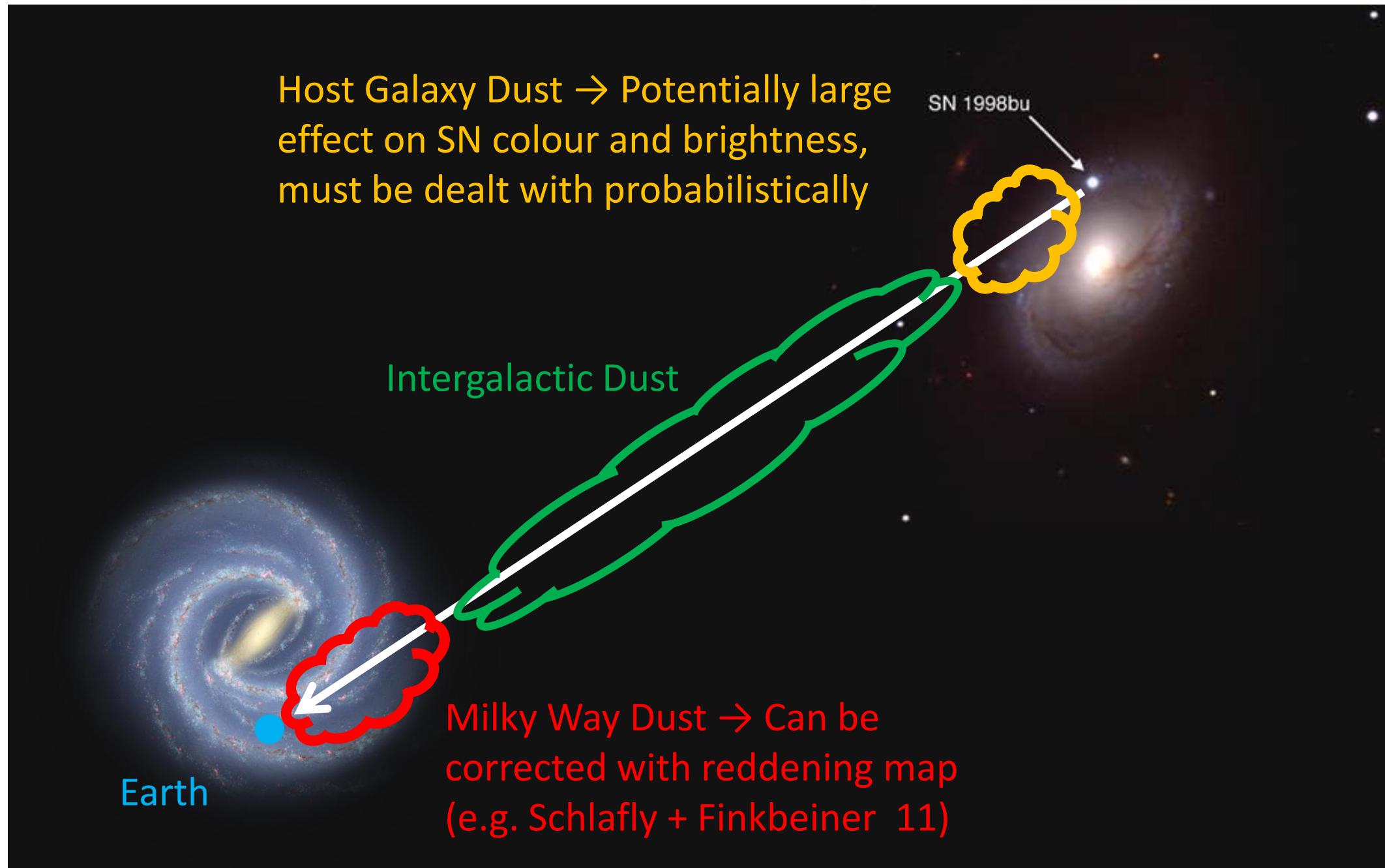
# SN Ia Cosmology

- Relies on effective standardisation of SNe Ia  
→ need a robust way of determining distance from photometric light curves
- Unprecedented data volume incoming  
→ need to worry about details that were previously subdominant sources of error

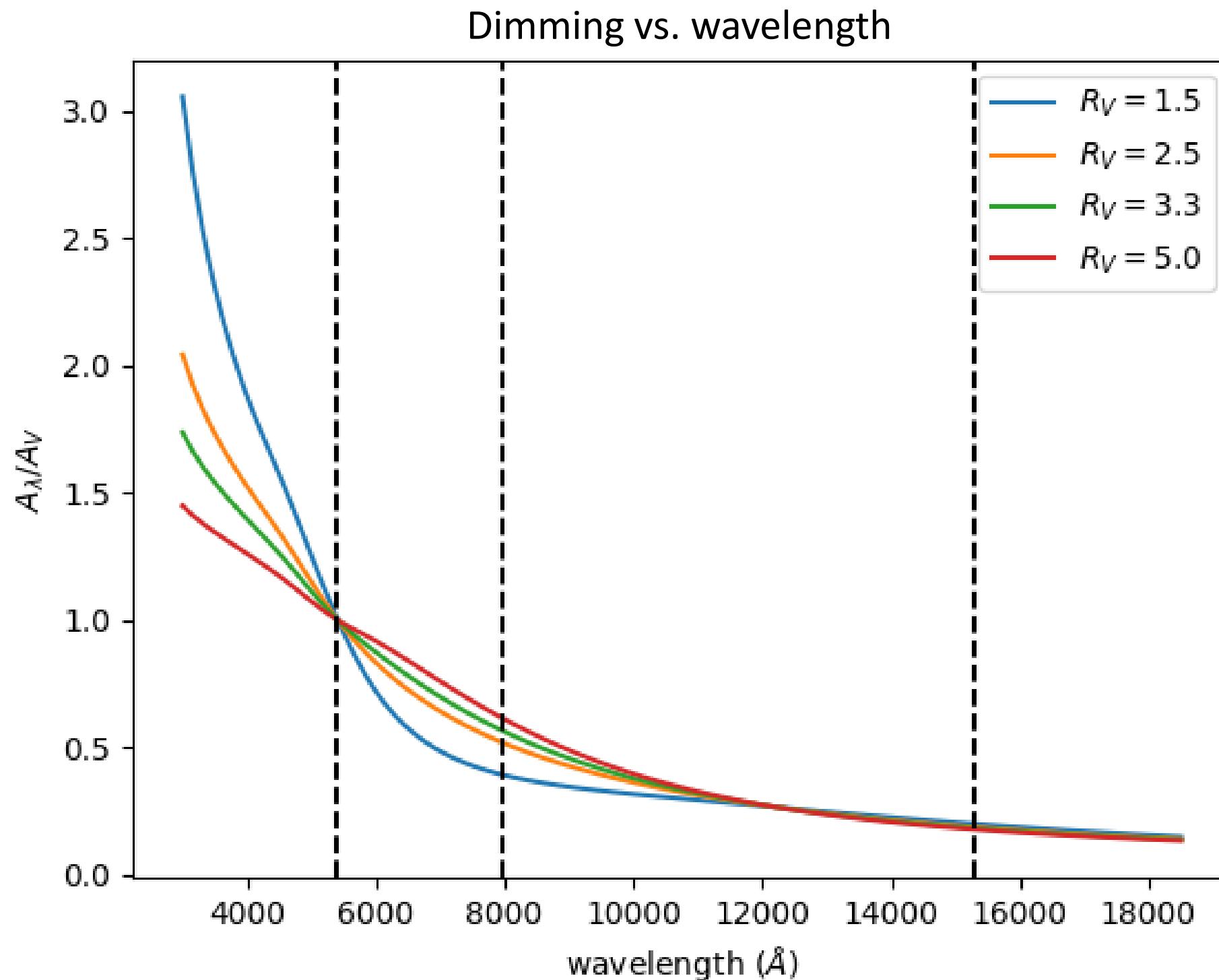
# Dust in SN Ia Host Galaxies

- Correctly handling dust is key to correctly estimating SN Ia distances, and potential systematic if done wrong
- Currently a lot of controversy over the dust laws in SN Ia host galaxies → particularly the distribution of  $R_V$

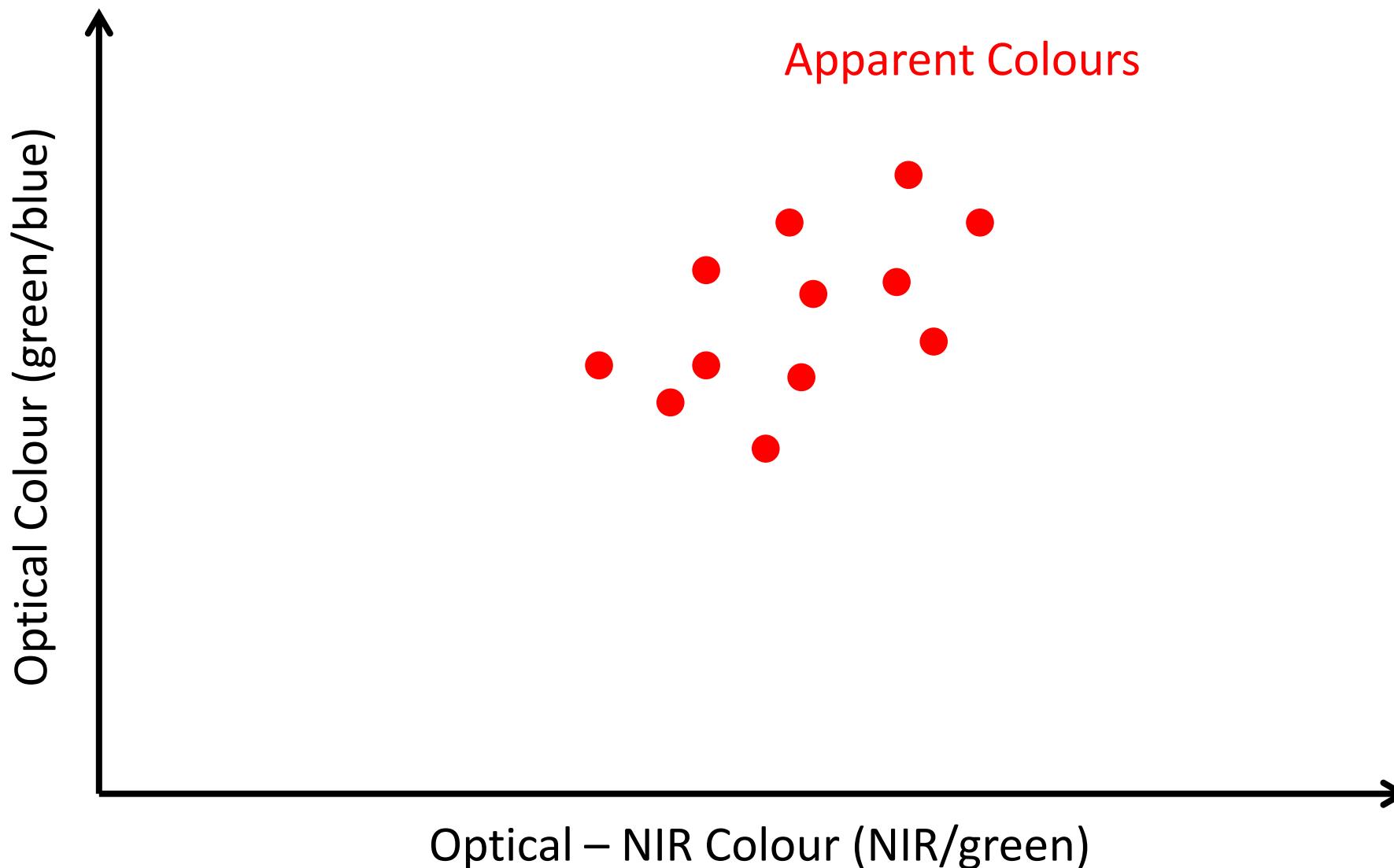
# What We Mean When We Talk About Dust



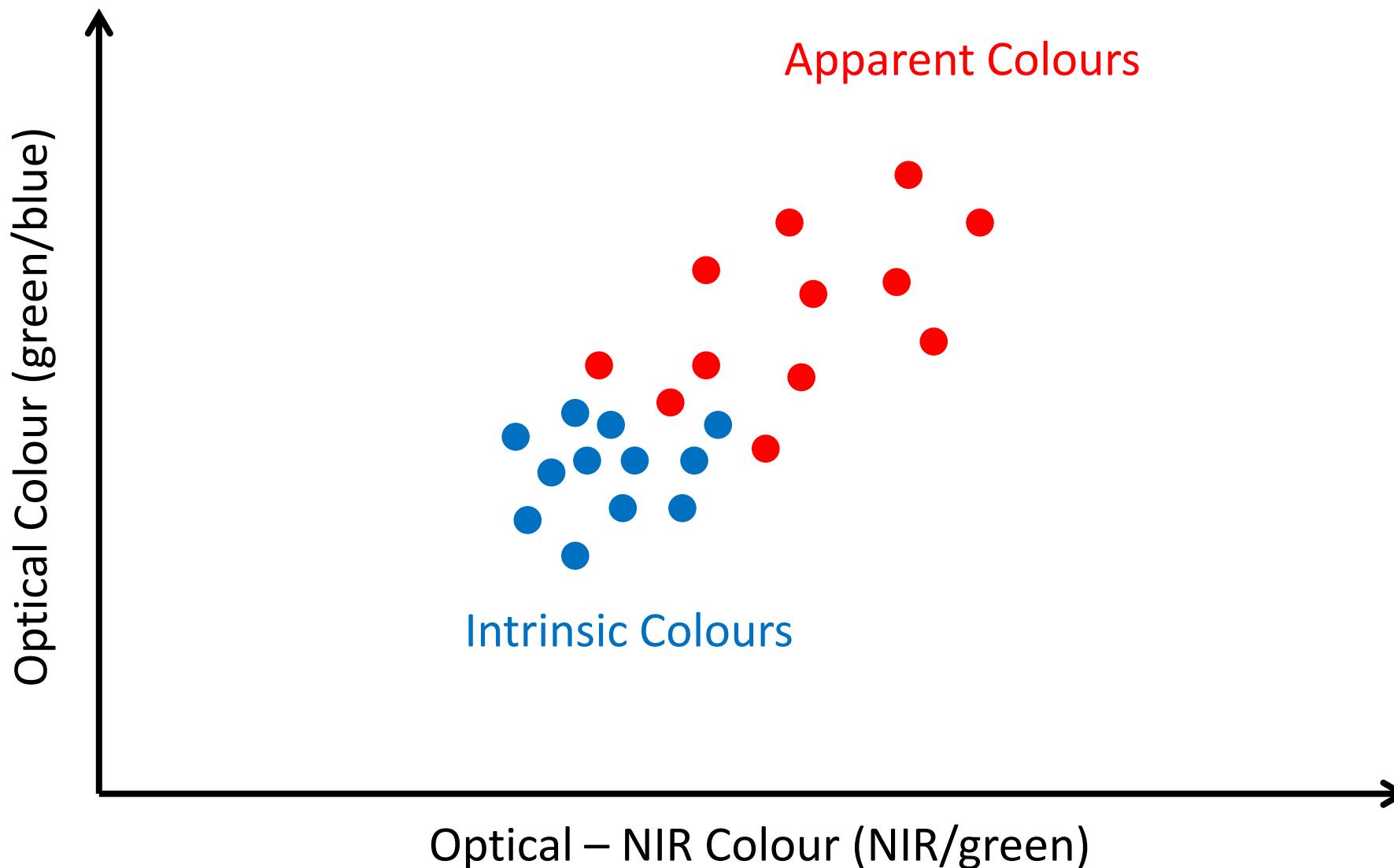
# Effect of $R_V$ on Fitzpatrick (1999) Dust Law



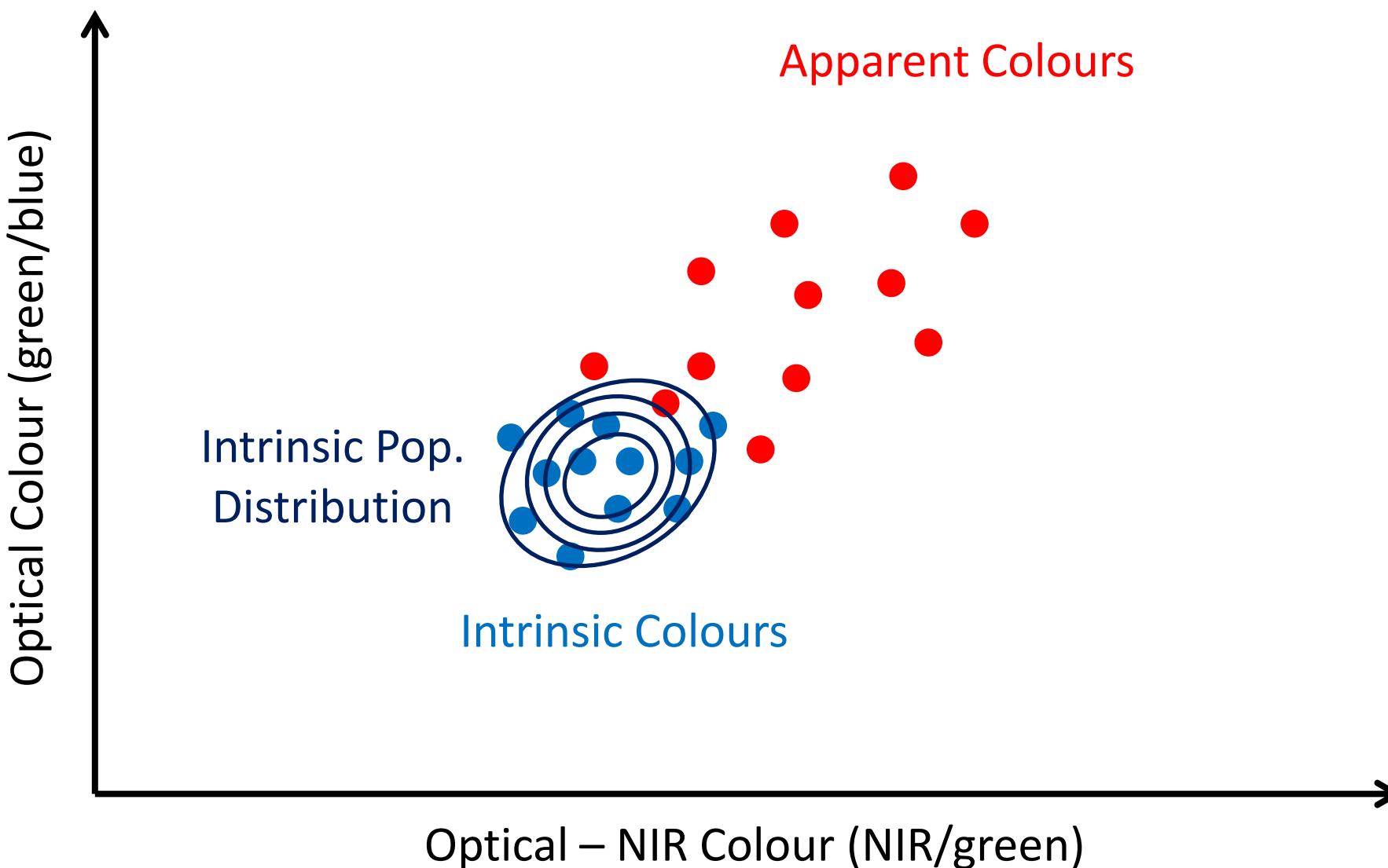
# How Do We Constrain $R_V$ ?



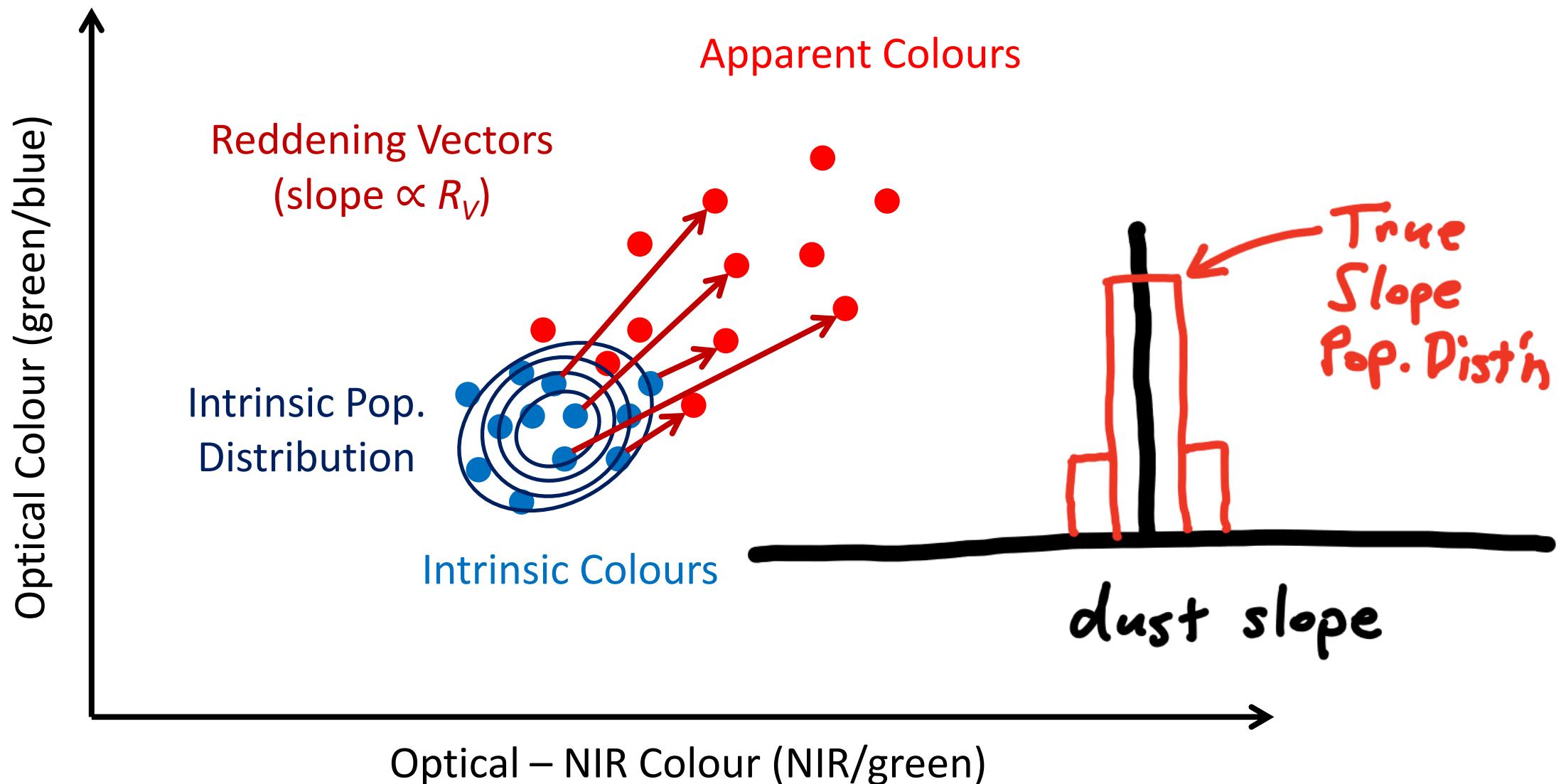
# How Do We Constrain $R_V$ ?



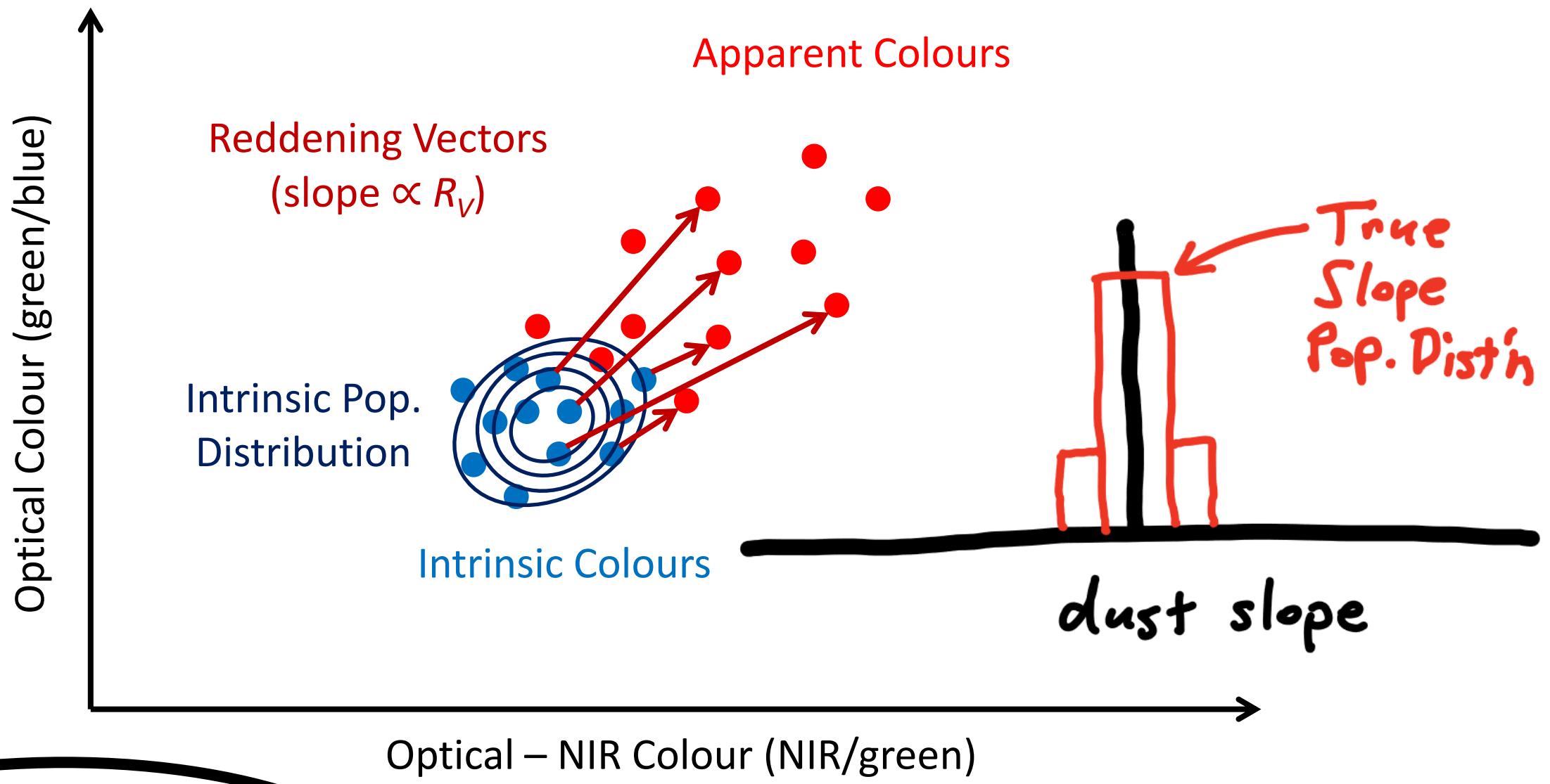
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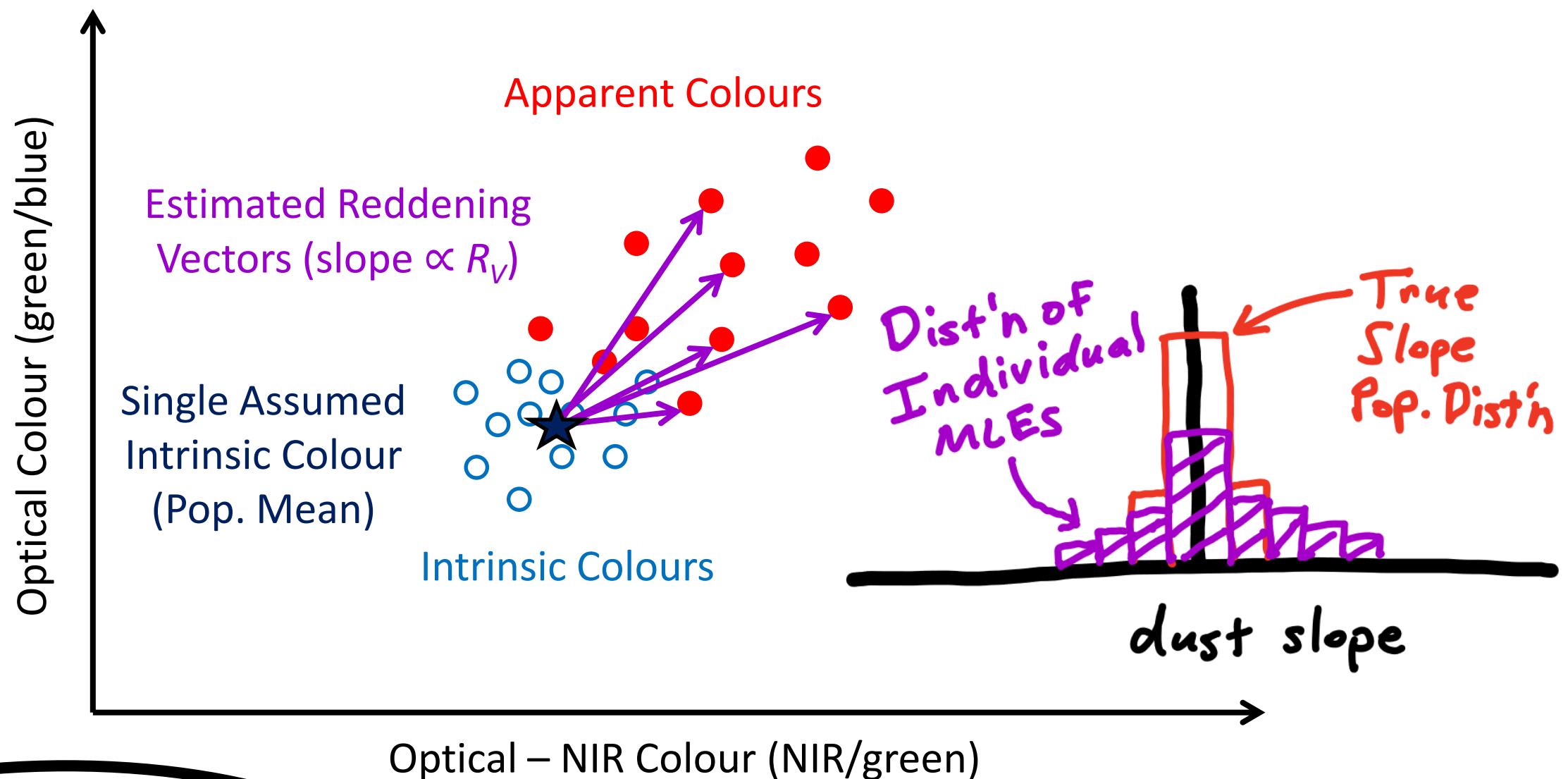


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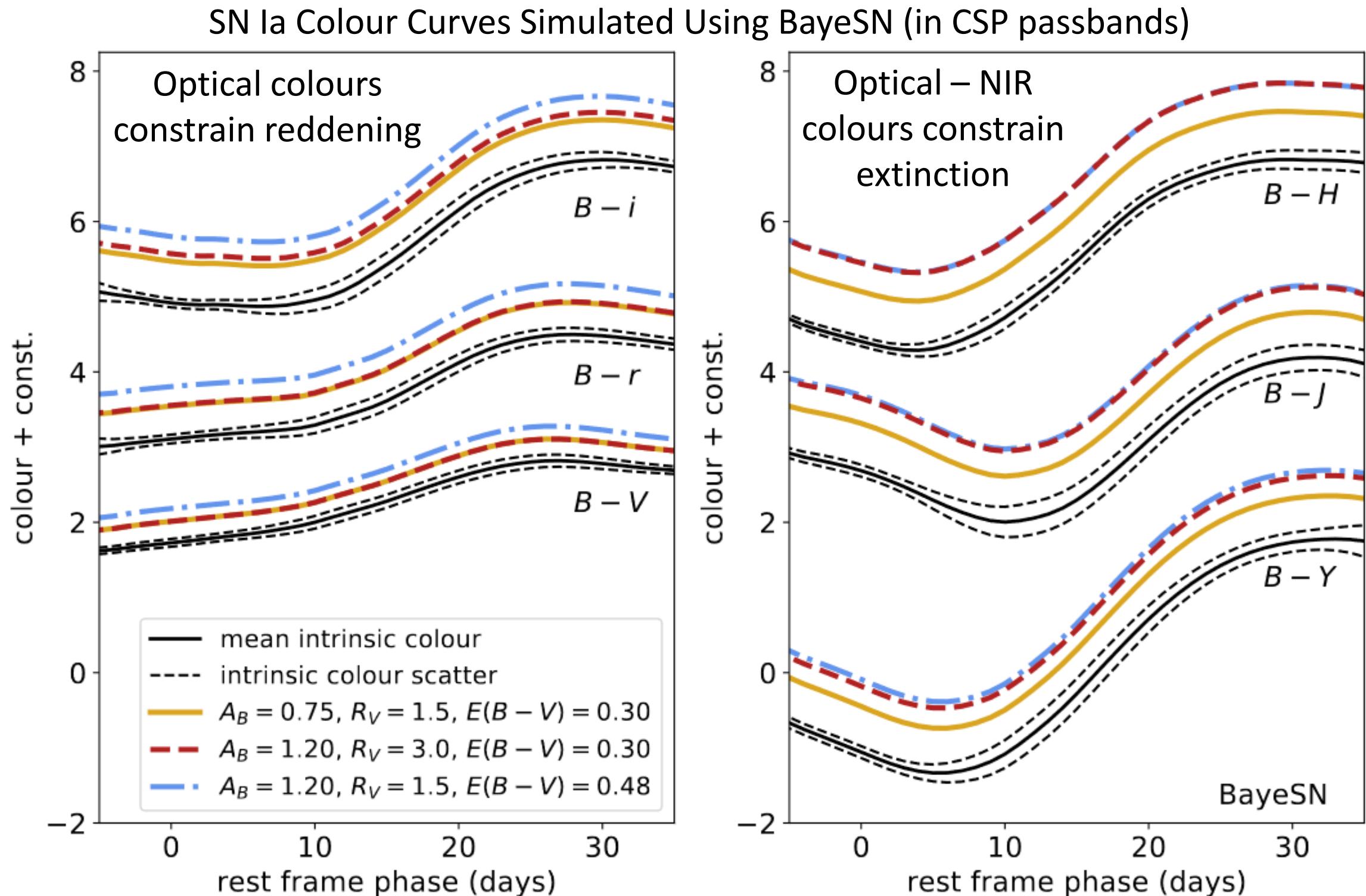


Need to account for  
intrinsic colour scatter  
when inferring  $R_V$

# How Do We (Not) Constrain $R_V$ ?

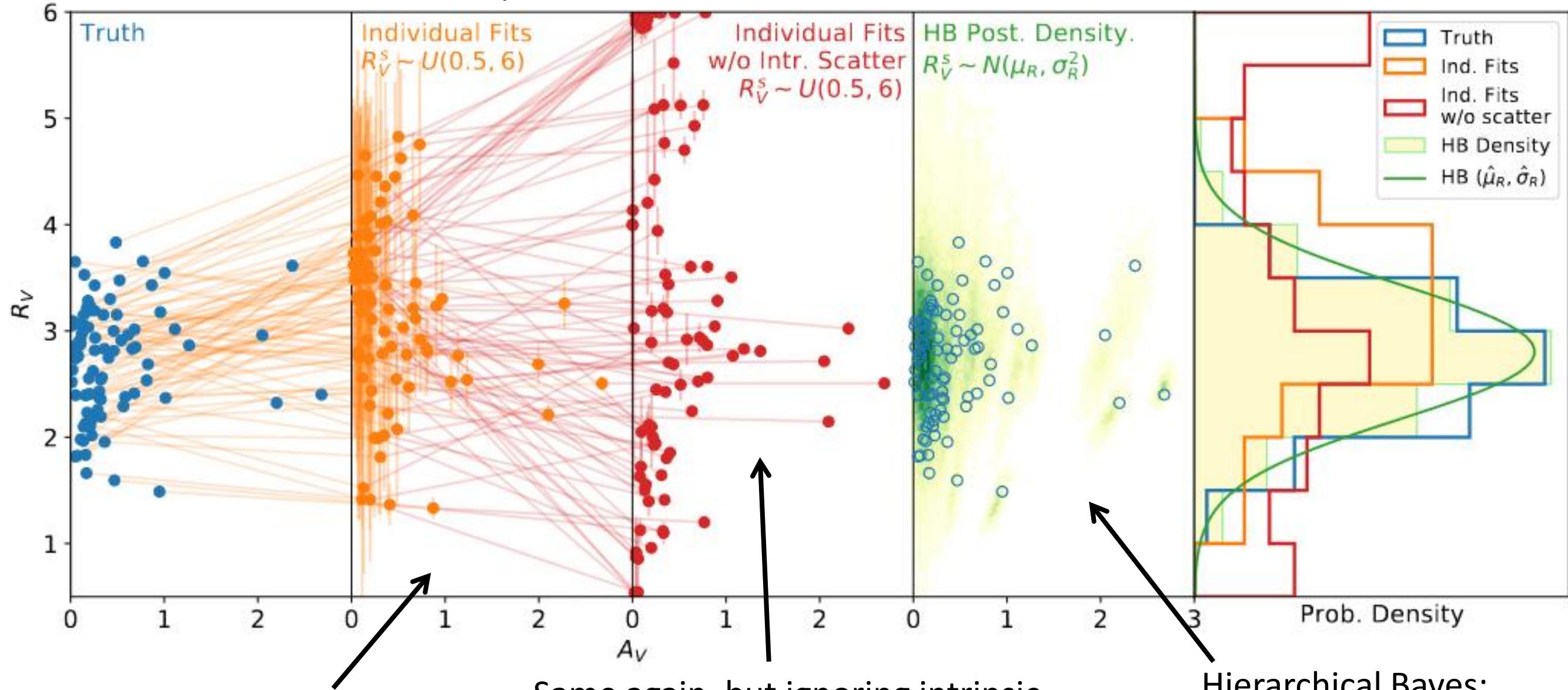


# Why Use Optical + NIR Data?



# Why Use Hierarchical Bayes?

Recovery of  $R_V$  Population Distribution in CSP-like Simulated Data



Recovery of  $R_V$  values from fits to each SN individually:  
overdispersed point estimates,  
but reasonable uncertainties

Same again, but ignoring intrinsic colour scatter: overdispersed and overconfident

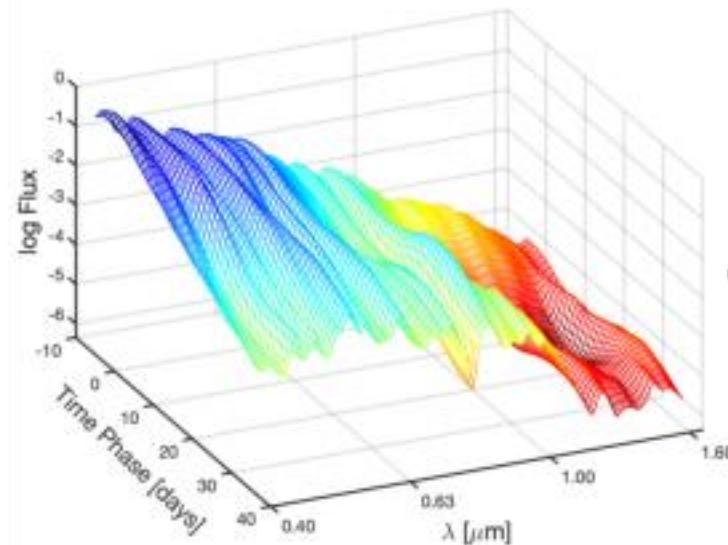
Hierarchical Bayes:  
effectively captures true population distribution

Thorp + Mandel, in prep.

# **Part II: Results Using the BayeSN Hierarchical Model for SN Ia SEDs**

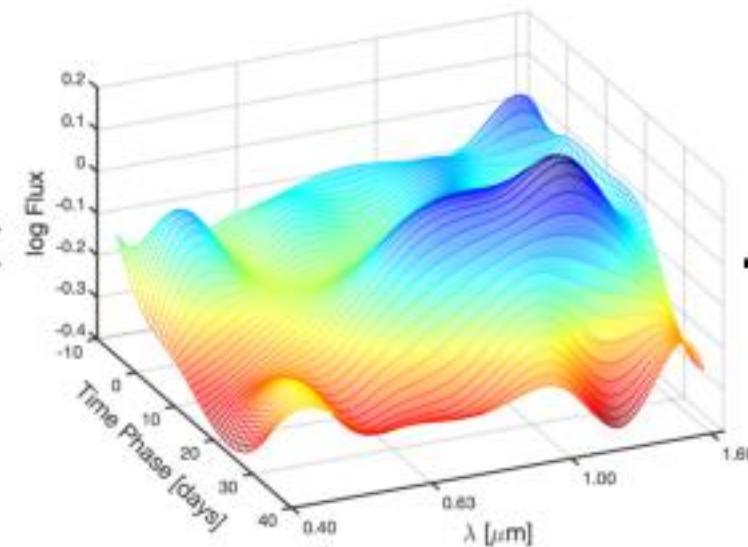
# The BayeSN SED Model

Mean Intrinsic SED



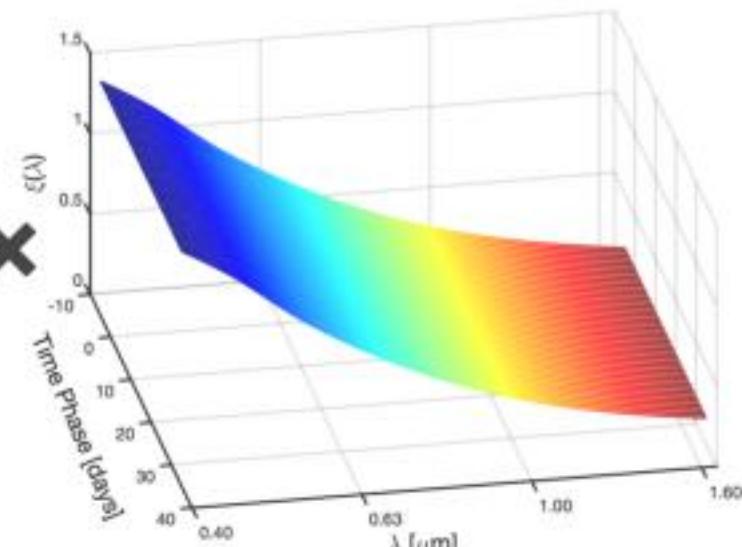
Intrinsic Functional Component  
 $W_1[t, \lambda] + \theta_2 W_2[t, \lambda] + \dots$

$+ \theta_1 \times$

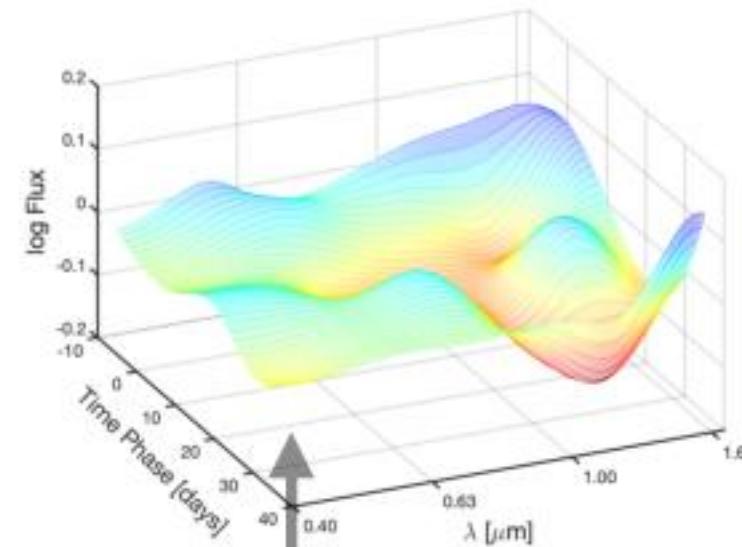


Dust Extinction Law ( $R_V$ )

$- A_V \times$



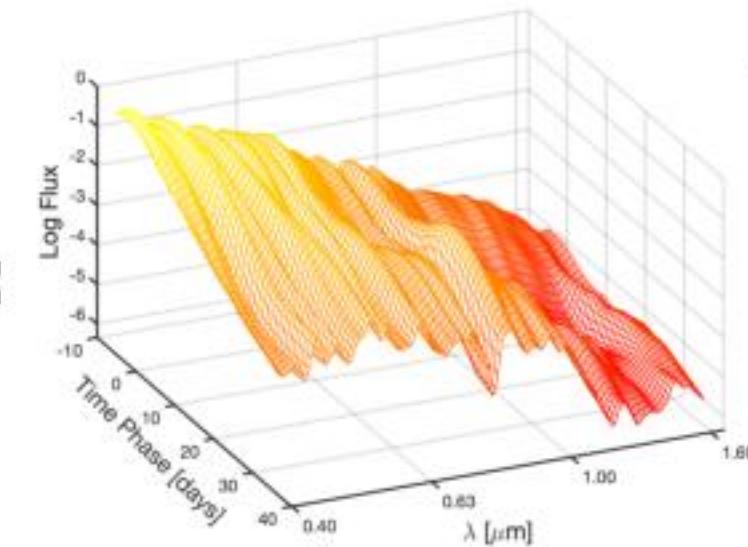
SED Residuals



$+$

Latent SN SED

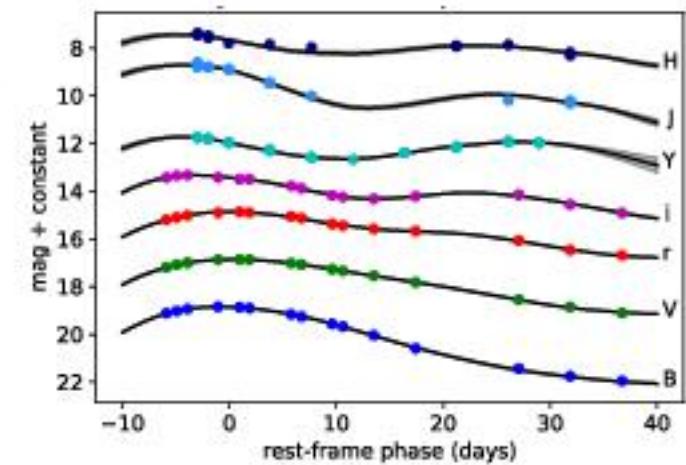
$=$



$\mu, z$   
cadence  
filters

$\rightarrow$

SN Ia Opt+NIR LCs

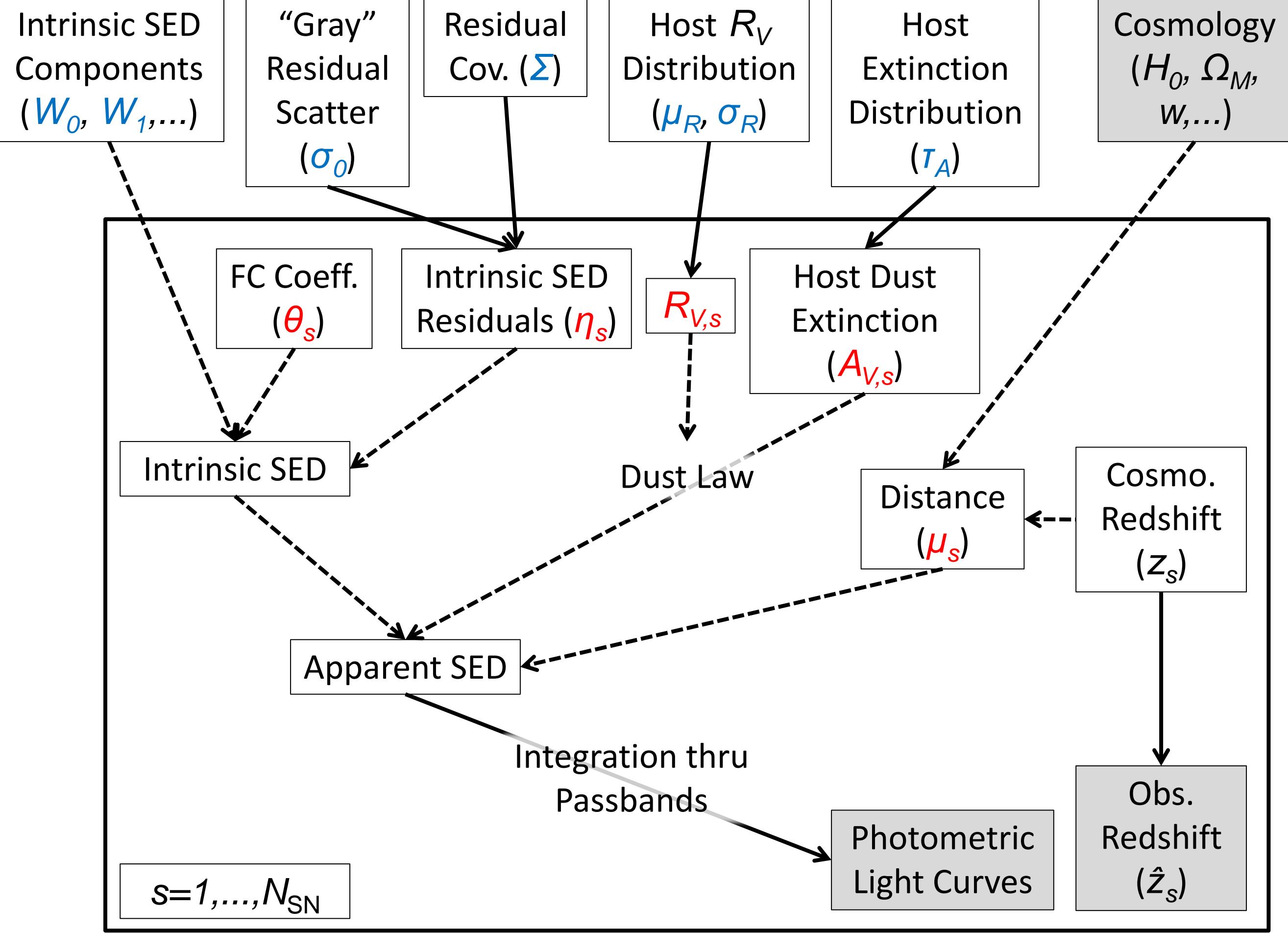


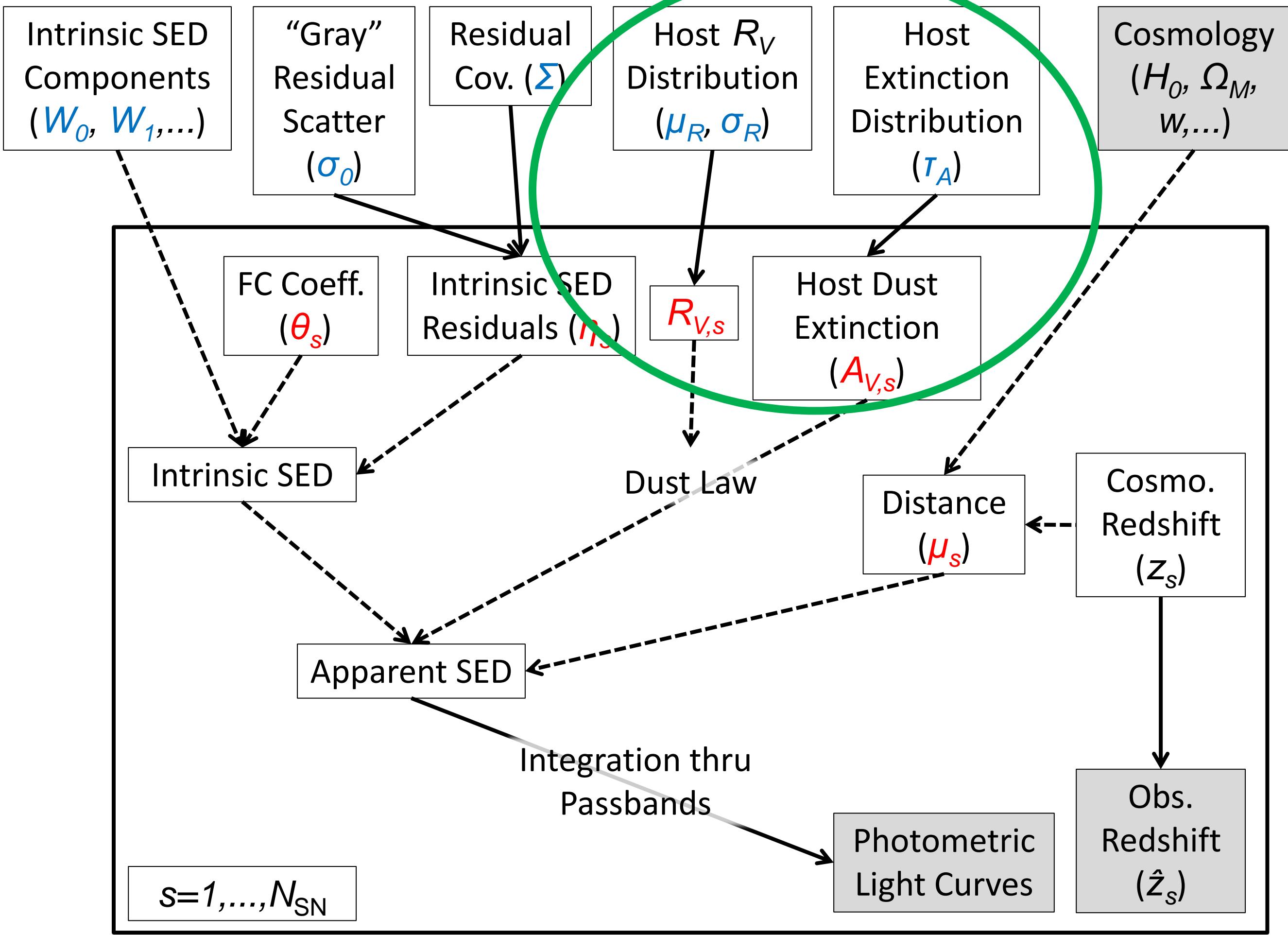
$\text{Cov } \Sigma(t, \lambda; t', \lambda')$

# The BayeSN SED Model

$$\begin{aligned} -2.5 \log_{10} [\textcolor{red}{S}_s(t, \lambda_r) / \textcolor{blue}{S}_0(t, \lambda_r)] &= \textcolor{blue}{M}_0 + \textcolor{blue}{W}_0(t, \lambda_r) \\ &+ \theta_s \textcolor{blue}{W}_1(t, \lambda_r) + \delta M_s + \varepsilon_s(t, \lambda_r) + A_{V,s} \xi(\lambda_r; \textcolor{red}{R}_V) \end{aligned}$$

$$\eta_s = \delta M_s + \varepsilon_s(t, \lambda_r)$$





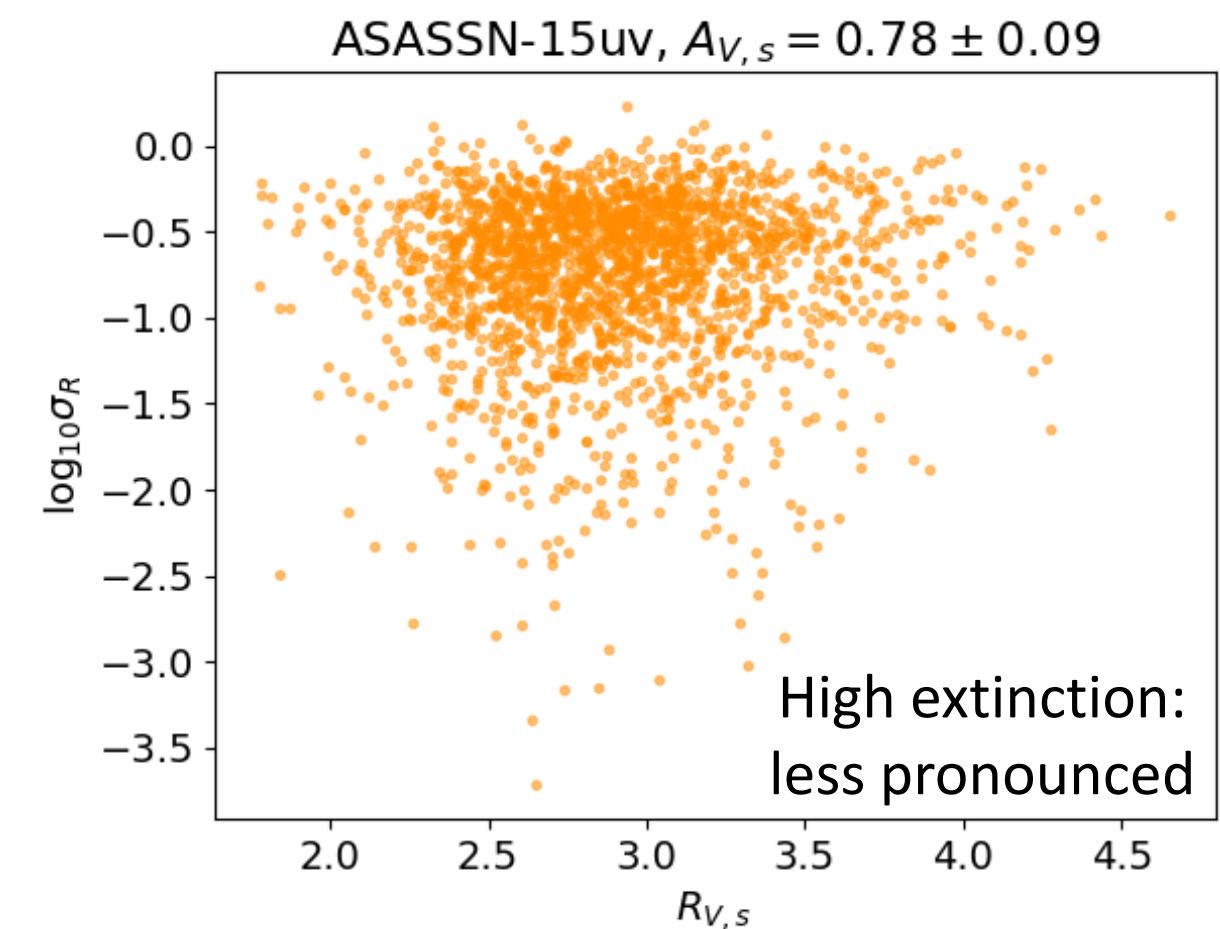
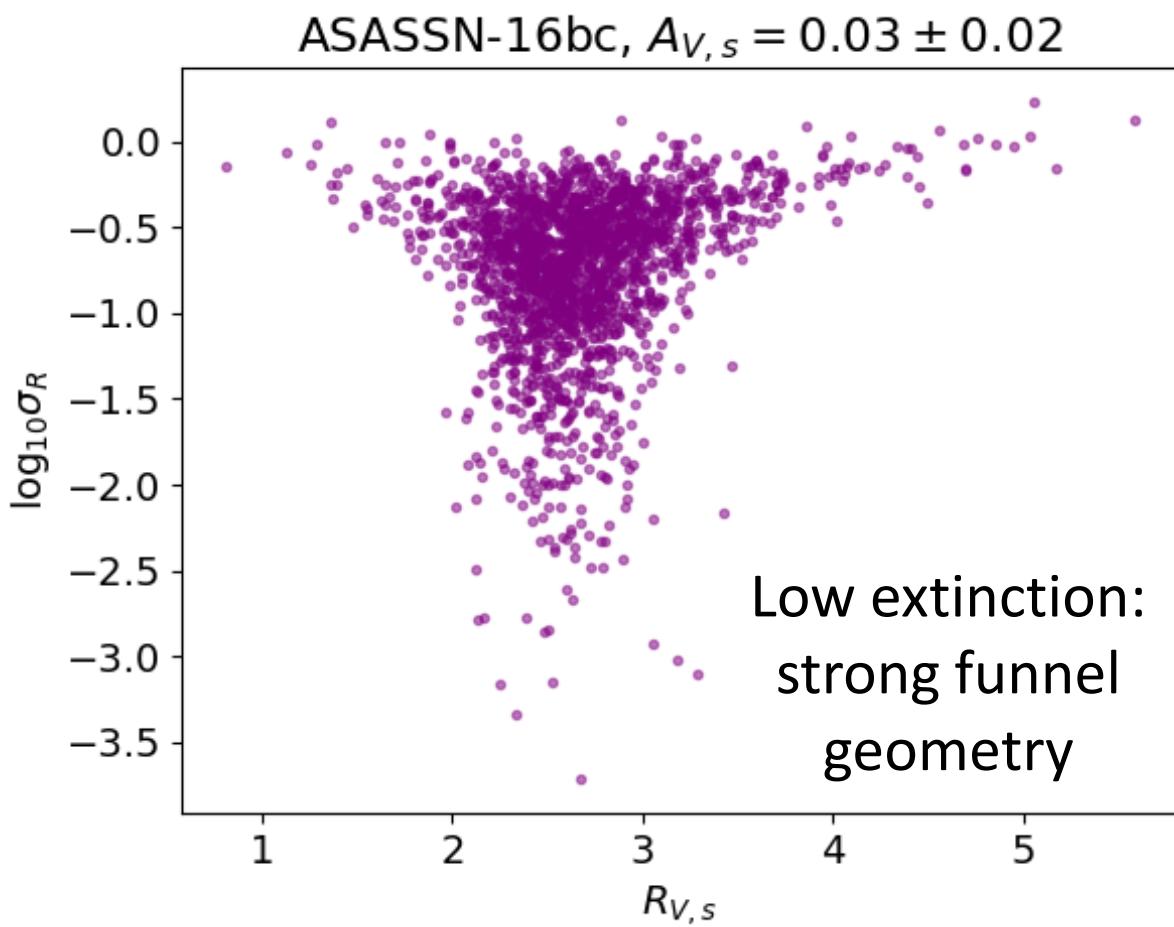
# Performing the Inference

- Implement hierarchical model in Stan
- Uses HMC to sample joint posterior of global and supernova-level parameters
- Check convergence using standard diagnostics (G-R, divergences, etc.)



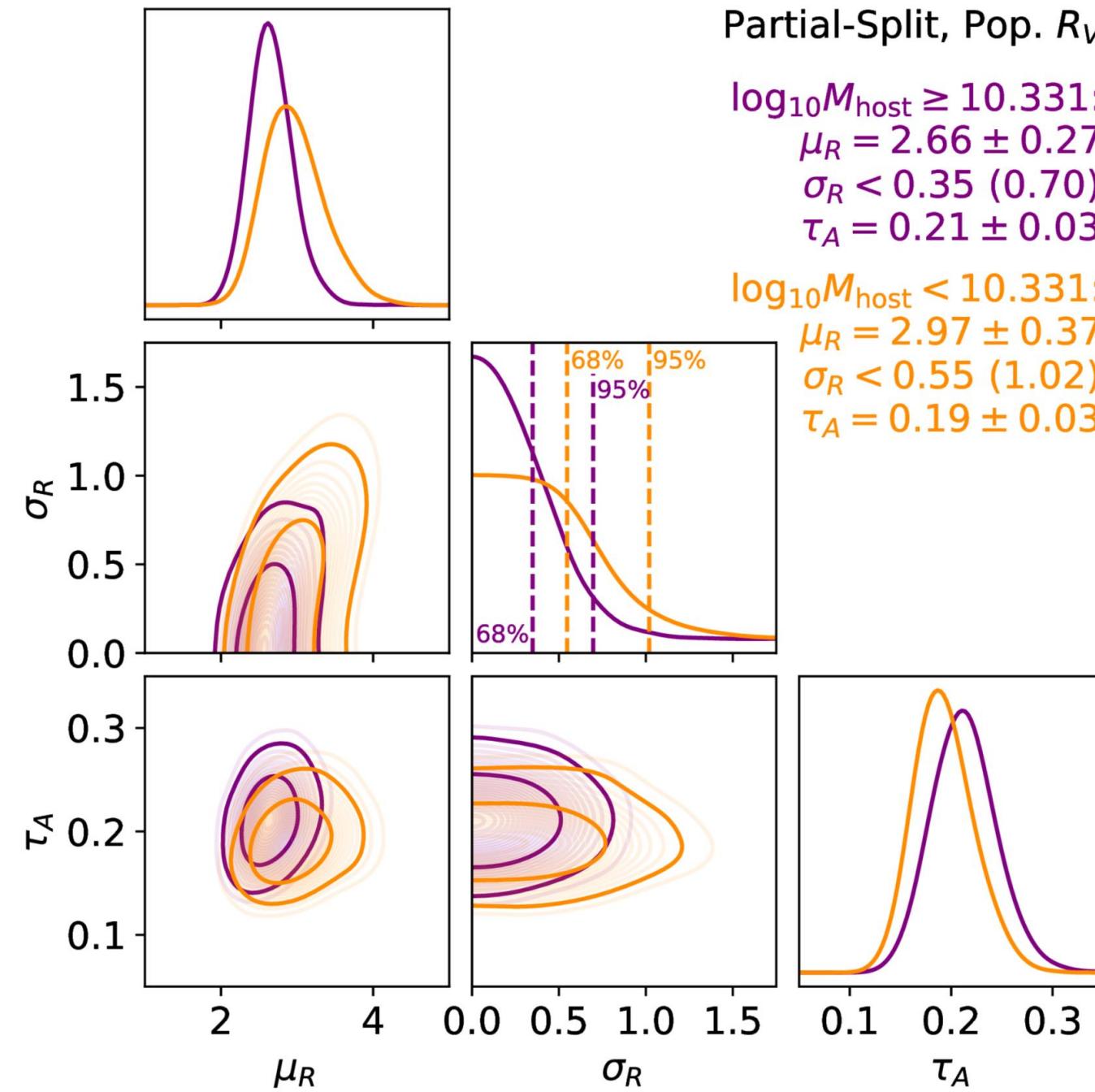
# Computational Challenges

- Modelling  $R_V$  population distribution creates difficult posterior geometry  
→ non-centred parameterisation!

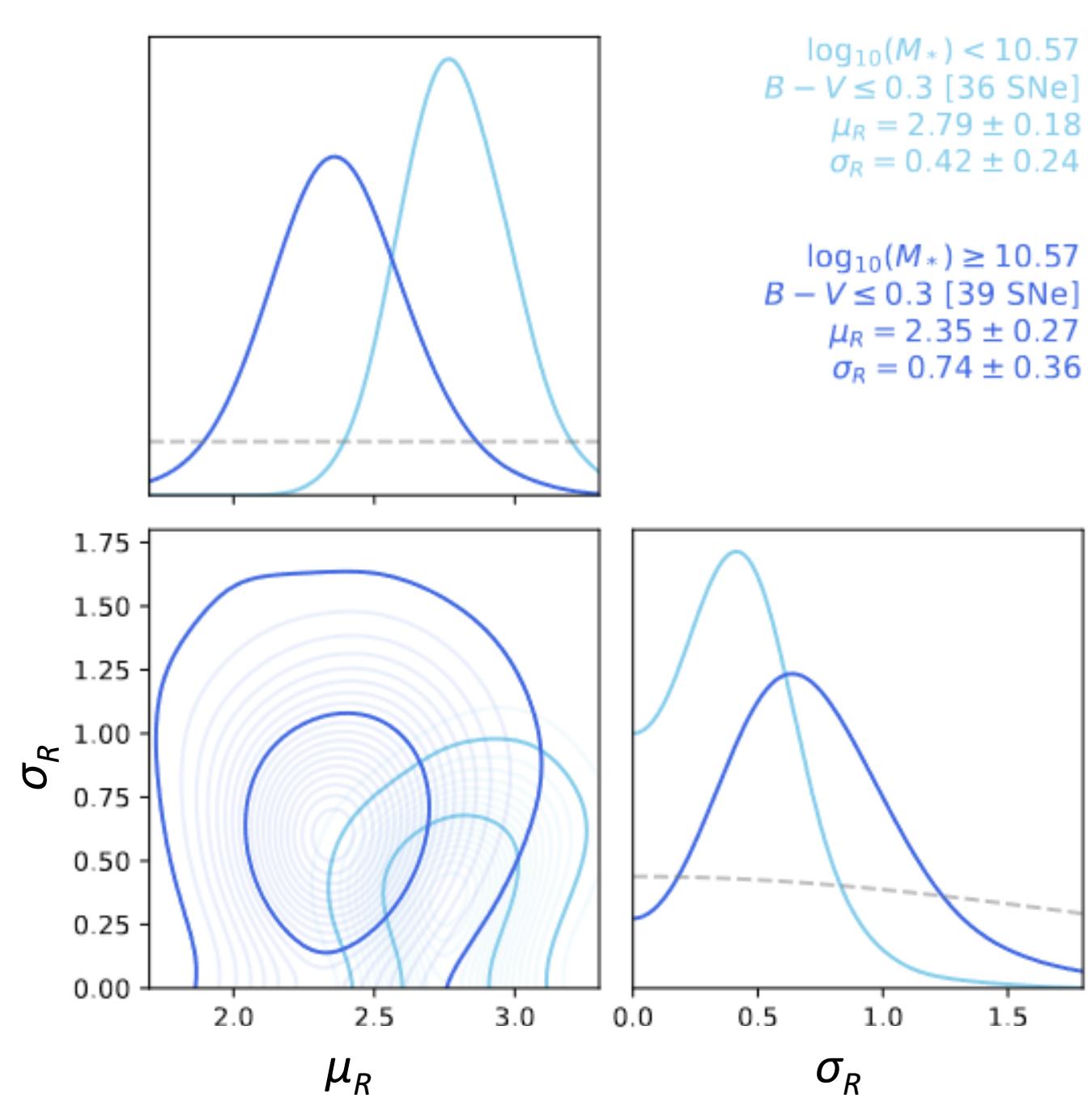


# BayeSN Results on Low-z Data

$R_V$  pop. distribution inference from Foundation



$R_V$  pop. distribution inference from CSP

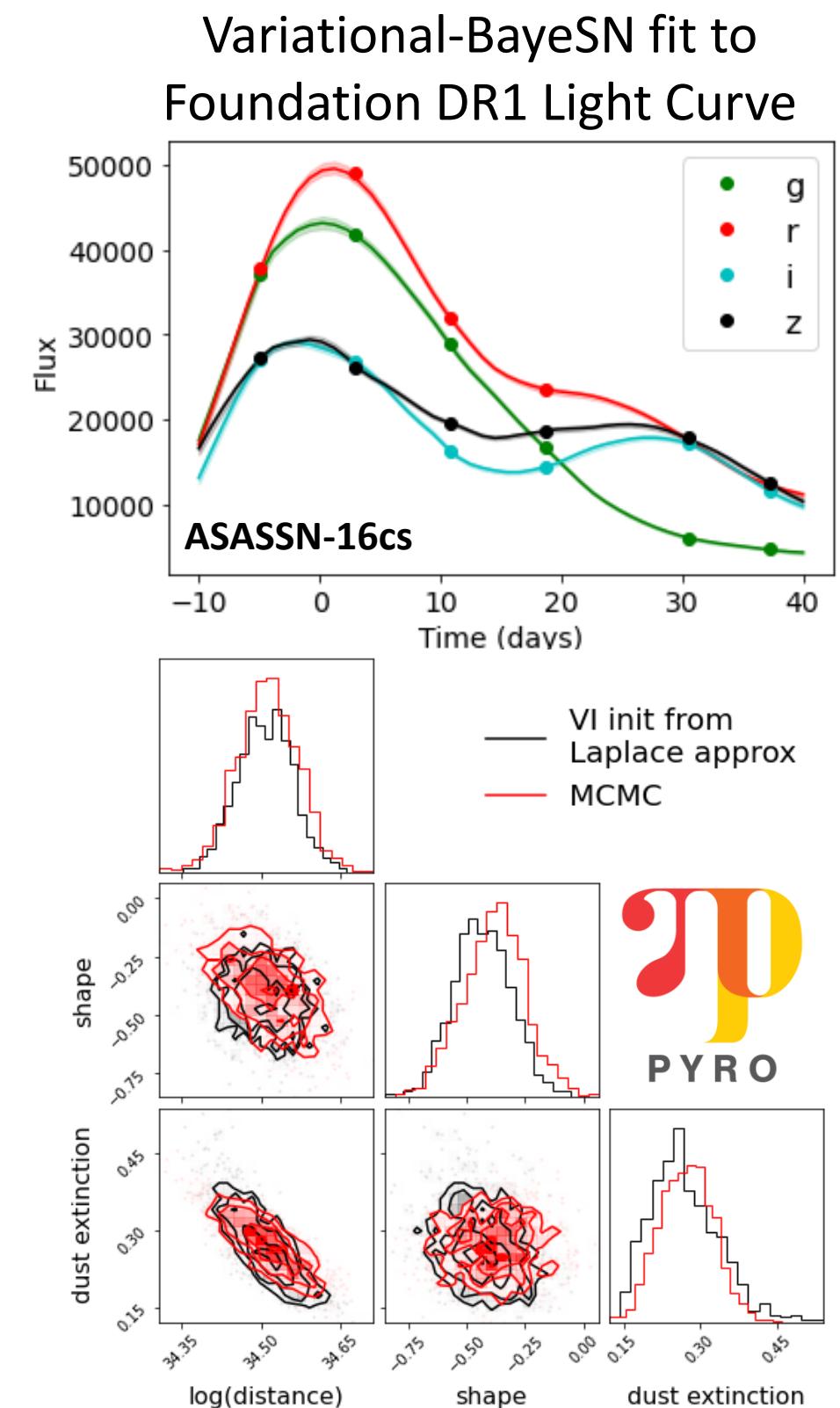


# Headline Results

- Hierarchical Bayesian approach lets us perform robust inference of  $R_V$  distribution in SN Ia host galaxies
- Favour small to moderate  $R_V$  distribution width, without strong dependence on host galaxy stellar mass

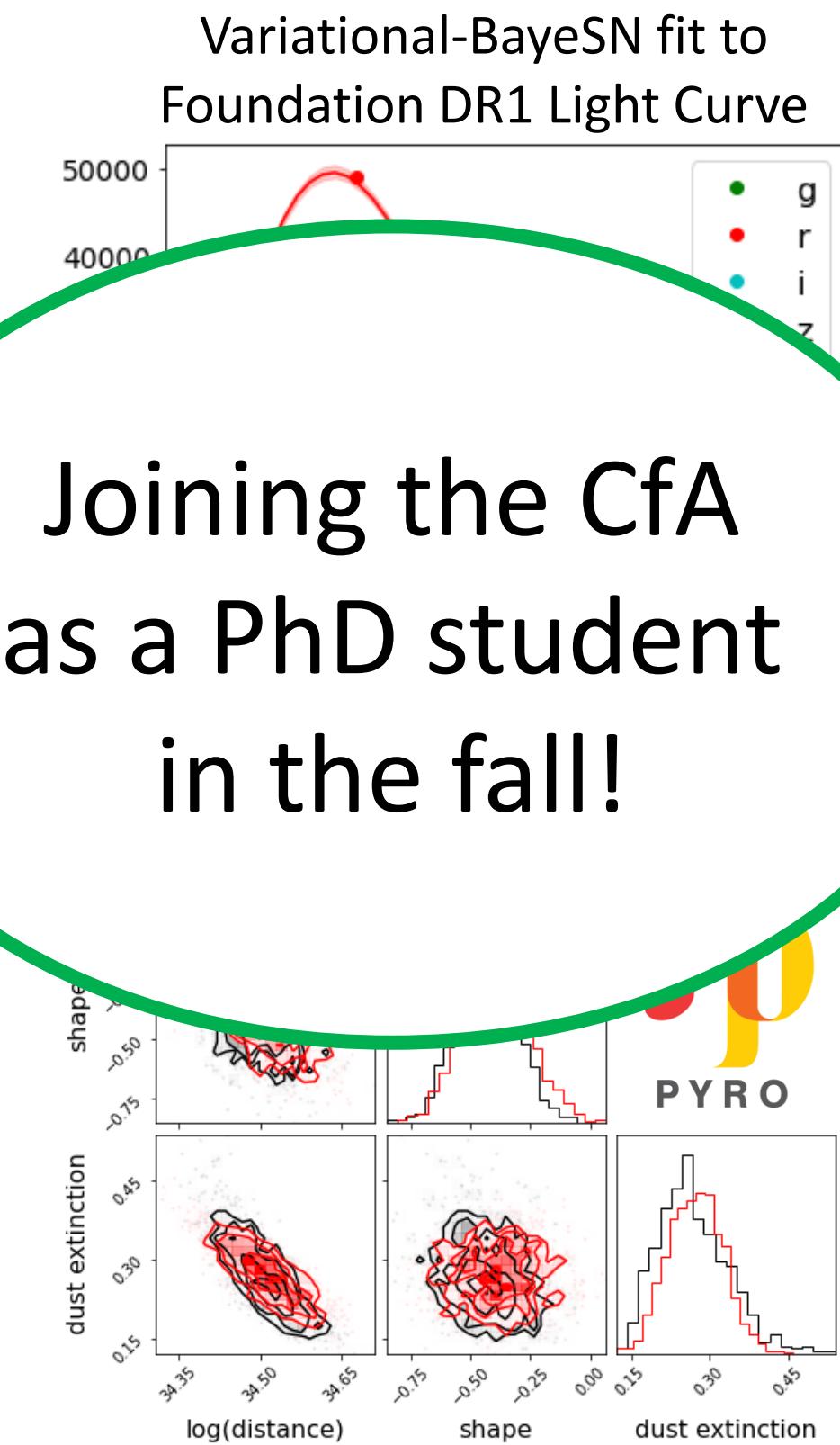
# Other BayeSN Activities

- $H_0$  w/ SN Ia siblings  
(Sam Ward)
- $H_0$  from optical+NIR  
(Suhail Dhawan)
- Improving scalability  
using variational  
inference  
(Ana Sofía Uzsoy)



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using variational  
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# Future Goals

- Scaling to LSST sized datasets whilst retaining Bayesian advantages (already making good progress with VI)
- Figuring out seamlessly integrated Bayesian treatment of selection effects
- Longer term... fully hierarchical cosmological analysis → SN photometry to cosmology with a single Bayesian model