TIME DELAY COSMOGRAPHY TOWARD THE HUBBLE CONSTANT ESTIMATION: PAST, PRESENT, AND FUTURE

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INTRODUCTION

Video Credit: Science, American Association for the Advancement of Science

The Hubble constant H_0 represents the current expansion rate of the Universe, as well as the age $(= H_0^{-1})$, size, and density of the Universe.

INTRODUCTION (CONT.)

But the Hubble constant estimates have been inconsistent!



Image Credit: Science, American Association for the Advancement of Science

The most recent estimates from these two methods are

- $67.4 \pm 0.5 \text{ km s}^{-1} \text{Mpc}^{-1}$ via CMB (Plank collaboration, 2018).
- ▶ $74.0 \pm 1.4 \text{ km s}^{-1} \text{Mpc}^{-1}$ via CDL (Reiss et al., 2019).

Is this 4.4 σ difference true (new physics)? Independent methods are necessary to confirm this difference.

TIME DELAY COSMOGRAPHY

Quasar is a highly luminous galaxy hosting a supermassive black hole at the center. Since it is extremely bright, it can be seen at a great distance.



Image Credit: Carnegie Institution for Science

TIME DELAY COSMOGRAPHY (CONT.)

Video source: https://www.youtube.com/watch?v=iE8x9kDHCFo

Strong gravitational lensing: The strong gravitational field of the intervening galaxy bends the light rays towards the Earth (like a lens), and thus we see multiple images of the same quasar in the sky.

TIME DELAY COSMOGRAPHY (CONT.)

Credit: NASA's Goddard Space Flight Center

Time delay: Light rays take different routes and travel through different gravitational potential, and thus their arrival times can differ \rightarrow time delay!

TIME DELAY COSMOGRAPHY (CONT.)

Inference on H_o via an equation for additional travel distance (Refsdal, 1964).



Image Credit: Tommaso Treu (UCLA) in "Dark Matter and Strong Lensing (2014)"

Additional travel distance = Speed of light $(c) \times \text{Time delay} (\Delta_{ij})$ = Time delay distance $(D_{\Delta t}(H_o, z, \Omega)) \times \text{Fermat potential difference } (\phi_{ij})$



TIME DELAY ESTIMATION: DATA

Data for a doubly-lensed quasar are two time series (light curves) with known measurement errors (Tak et al., 2017)



We can estimate Δ by the horizontal shift between two time series.

TIME DELAY CHALLENGE

Time Delay Challenge (Dobler et al., 2015; Liao et al., 2015)

- A blind competition held by 8 astrophysicists from 2013 to 2014.
- Goal was to improve existing estimation methods.
- ▶ 5,000+ simulated data sets with some time delays.
- 13 teams blindly analyzed the simulated data sets.



Image Credit: HBO website

Our work after the TDC

1. Tak, H., Mandel, K., van Dyk, D. A., Kashyap, V. L., Meng, X-.L., and Siemiginowska, A. (2017) "Bayesian Estimates of Astronomical Time Delays Between Gravitationally Lensed Stochastic Light Curves", *AoAS*.



- A fully Bayesian approach / Bayesian hierarchical modeling
- A damped random walk process (Kelly et al., 2019).
- A polynomial regression for microlensing.
- Scientifically-motivated and weakly-informative priors.
- Metropolis-Hastings within Gibbs sampler.
- Adaptive Markov chain Monte Carlo (MCMC).
- Profile likelihood approach to multimodality.

OUR WORK AFTER THE TDC (CONT.)

2. An R package "timedelay" is publicly available.



First launched in 2015 with the last update in 2018.

Its median daily-download-count was 9 last year.

OUR WORK AFTER THE TDC (CONT.)

3. Kimura, M., Kato, T., Isogai, K., Tak., H., and 23 people (2017) "Rapid optical variations correlated with X-rays in the 2015 second outburst of V404 Cygni (GS 2023+338)", *MNRAS*.



 A collaboration with Japanese astronomers thanks to the timedelay package.

OUR WORK AFTER THE TDC (CONT.)

4. Tak., H., Meng, X-.L., van Dyk, D. A. (2018) "A Repelling-Attracting Metropolis Algorithm for Multimodality", *JCGS*.



- A multi-modal MCMC sampler motivated by Time Delay Estimation.
- Easy-to-implement.
- Effective in low-dimensional parameter sampling (possibly embedded in high-dimensional problem).
- ► The R package, timedelay, is equipped with this sampler.

CURRENT WORK IN PREPARATION

1. Hu, Z. and Tak., H. (2020+) "A Multivariate Damped Random Walk Process for Modeling Irregularly-Spaced Multi-Band Light Curves with Heteroscedastic Measurement Errors."



- A multivariate generalization of a univariate damped random work process (Kelly et al., 2009).
- A multivariate generalization of a univariate time delay estimation (Tak et al., 2017).
- A new R package, drw, to fit a multivariate damped random work process is in preparation. The existing R package, timedelay, will be updated to incorporate this multivariate feature.

CURRENT WORK IN PREPARATION (CONT.)

2. Tak., H., Ding, X., Birrer, S. (2020+) "A Bayesian Estimate of the Hubble Constant via Time Delay Cosmography."



- Based on another blind competition called Time Delay Lens Modeling Challenge (TDLMC) held from 2018 to 2019 (Ding et al., 2020+).
- ► A closed-form marginal posterior distribution of the Hubble constant.

CURRENT WORK IN PREPARATION (CONT.)

3. Vishwanath, S. and Tak., H. (2020+) "A Repelling-Attracting Metropolis for High-Dimensional Multimodality."



- Mixing anti-Langevin and Langevin algorithms to incorporate gradient information to RAM, as Christian Robert suggested.
- Preventing a chain from going back to the original mode.
- Detailed balance condition is already proven.
- Working on simulations.

Future work (2021+)

