

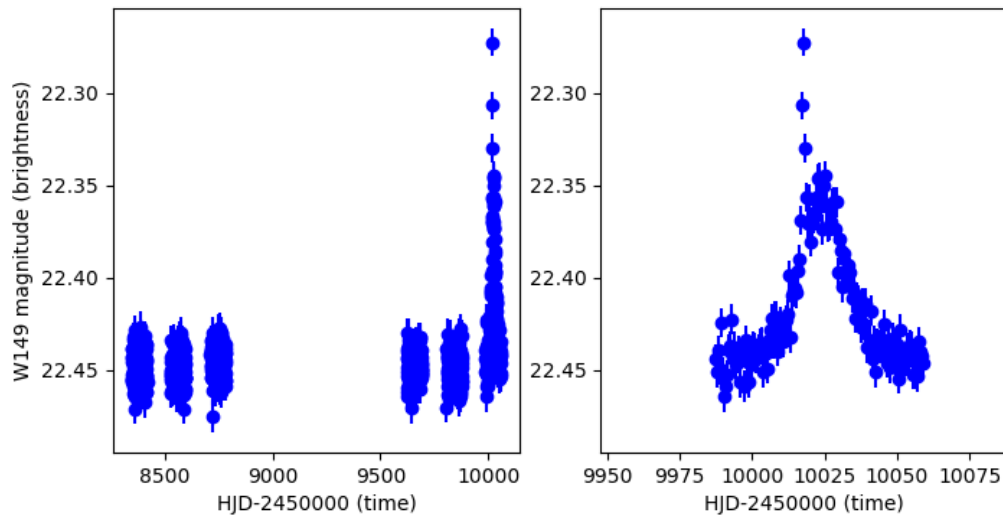
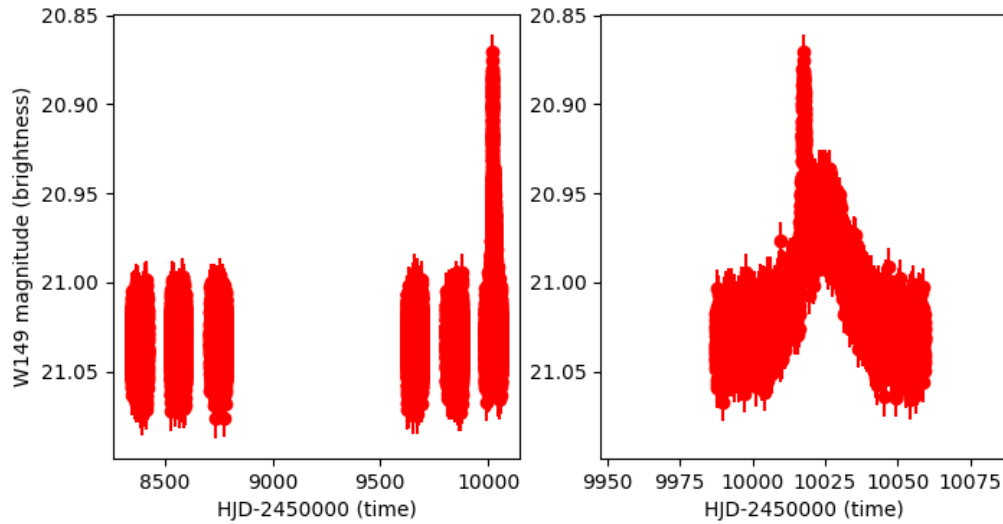


HARVARD-SMITHSONIAN  
CENTER FOR ASTROPHYSICS

# WFIRST Data Analysis Challenge

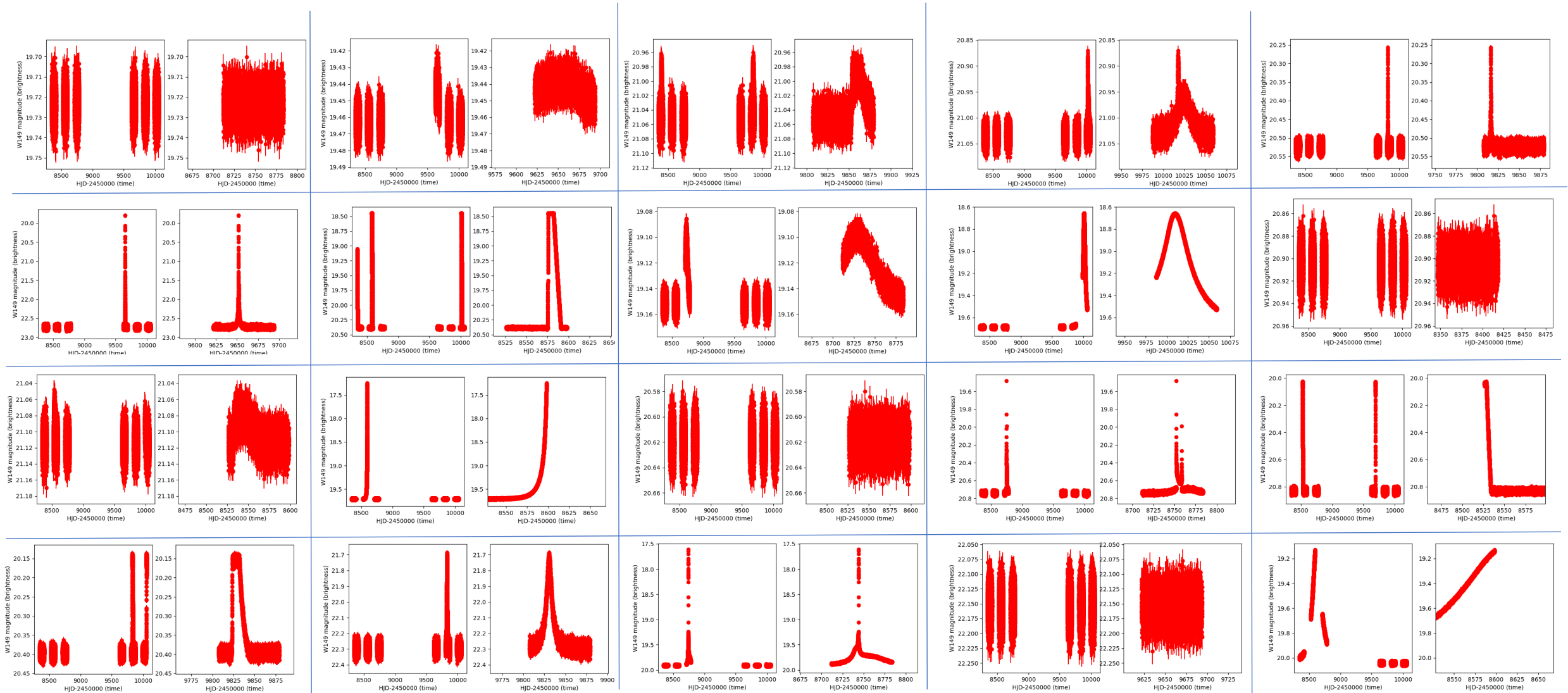
Jennifer C. Yee

# A Data Challenge Light Curve



- Magnitude (brightness) vs. Time
- 2 wavelengths  $\rightarrow$  2 light curves

# Data Challenge: "Solve" 293 light curves

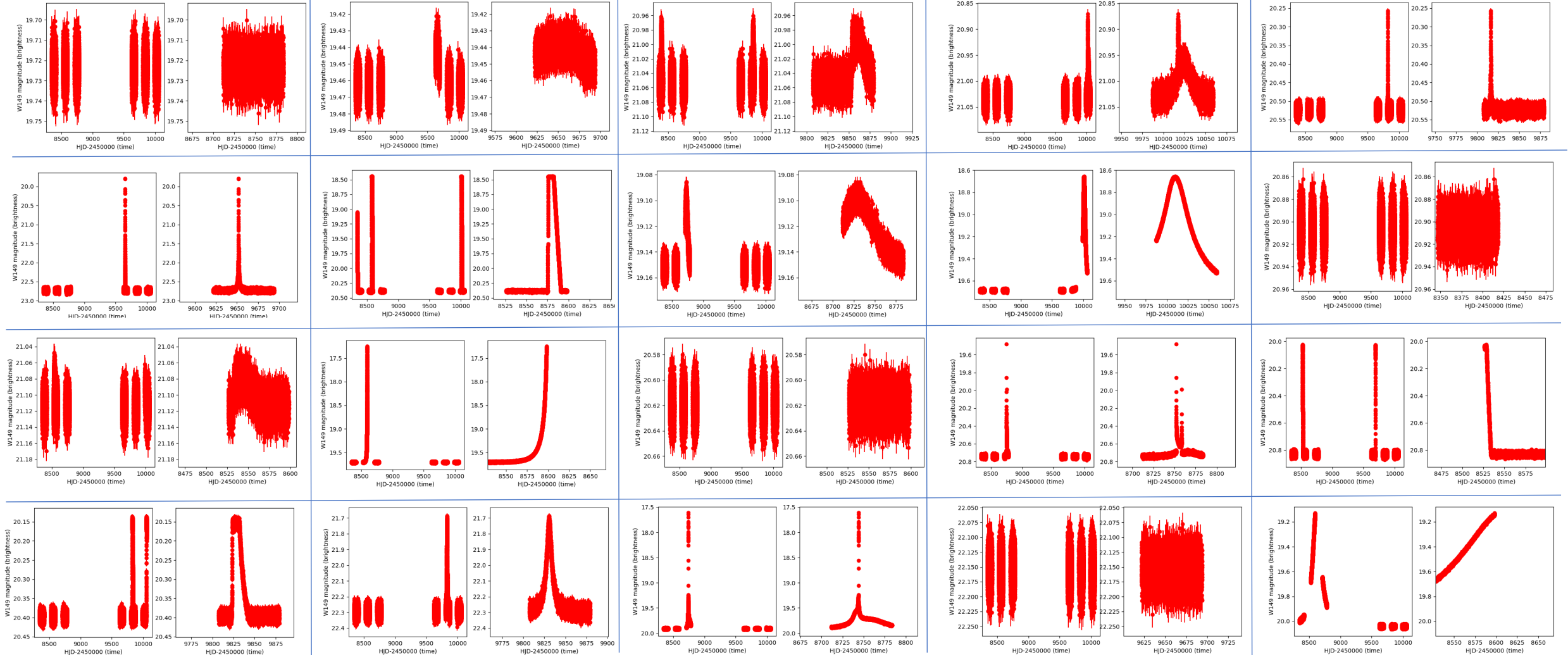


Astronomer's Question: Which ones have planets and what are their properties?

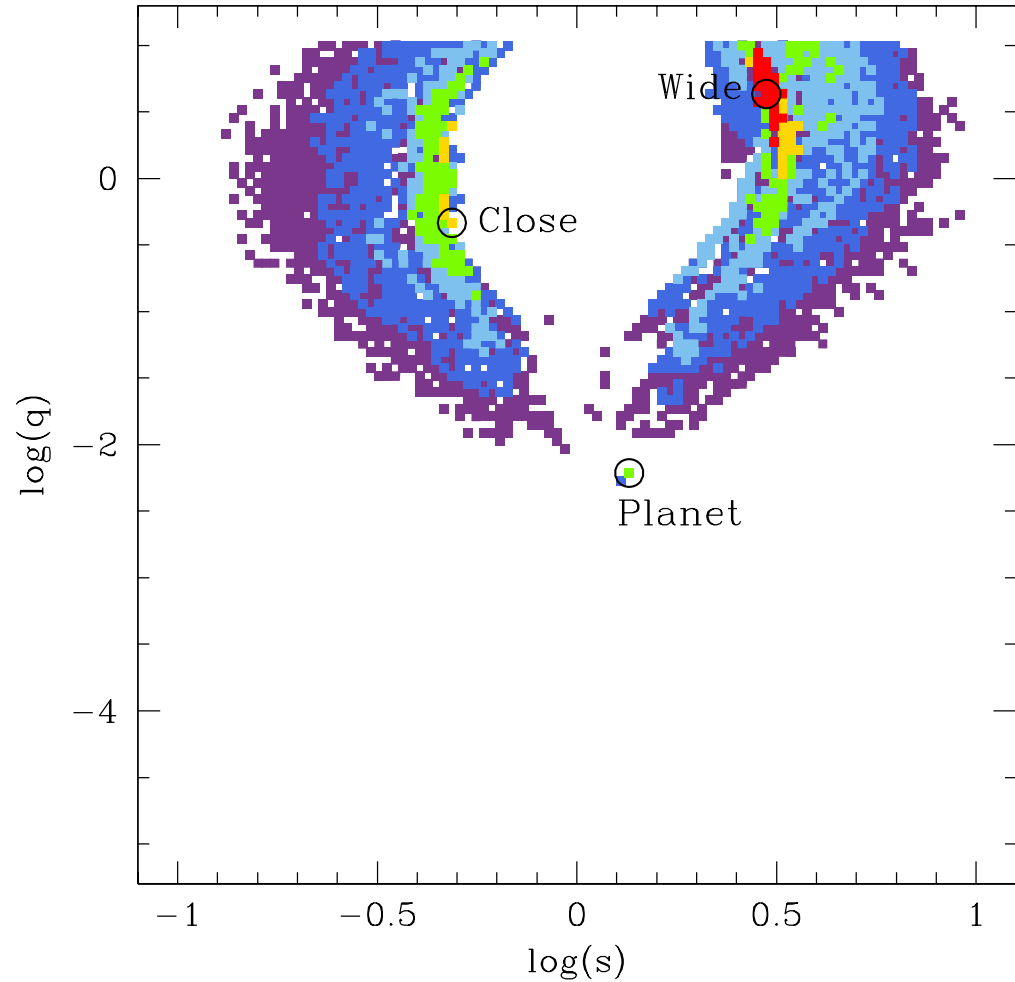
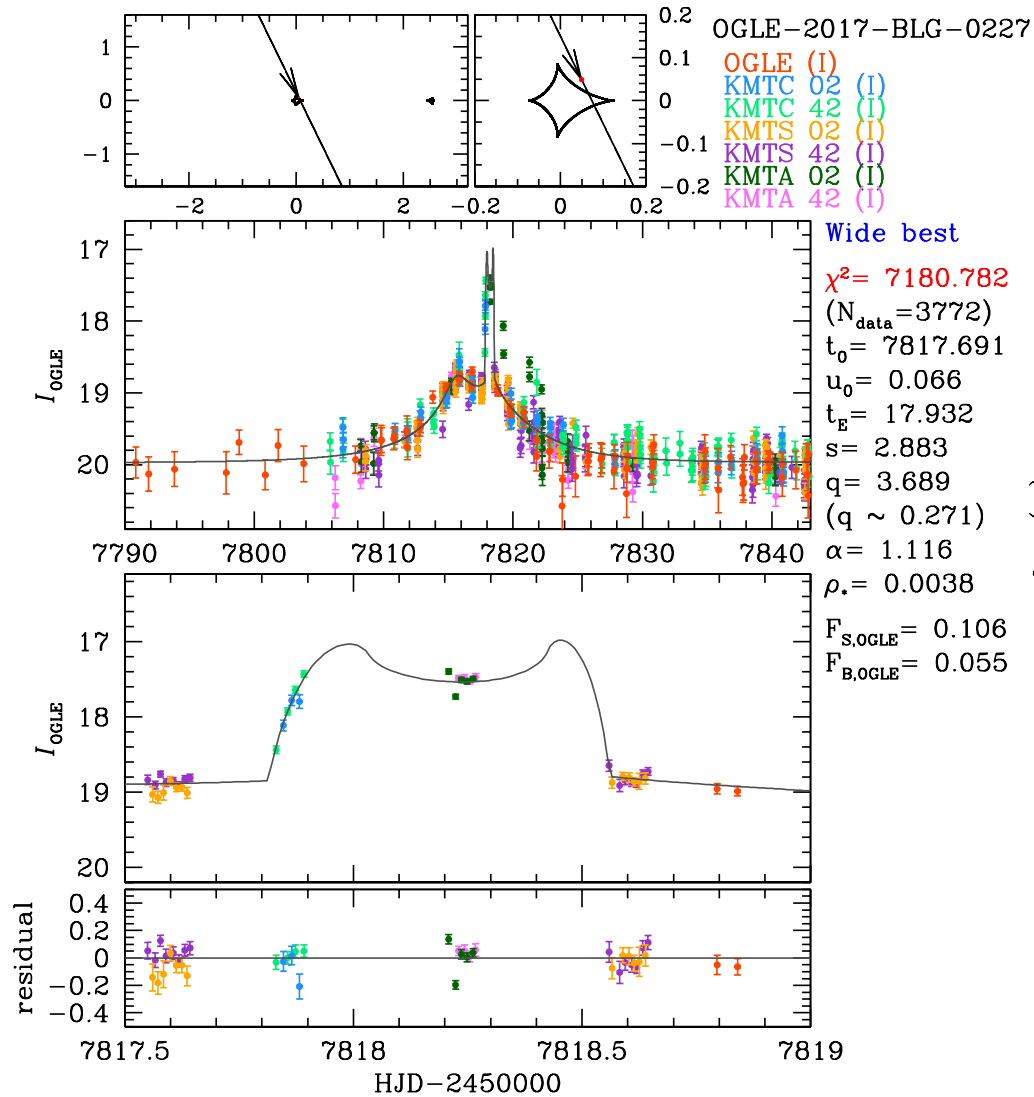
## More General Questions:

- Microlensing or Not Microlensing?
- 1-body or 2-bodies?
- What are the parameters?

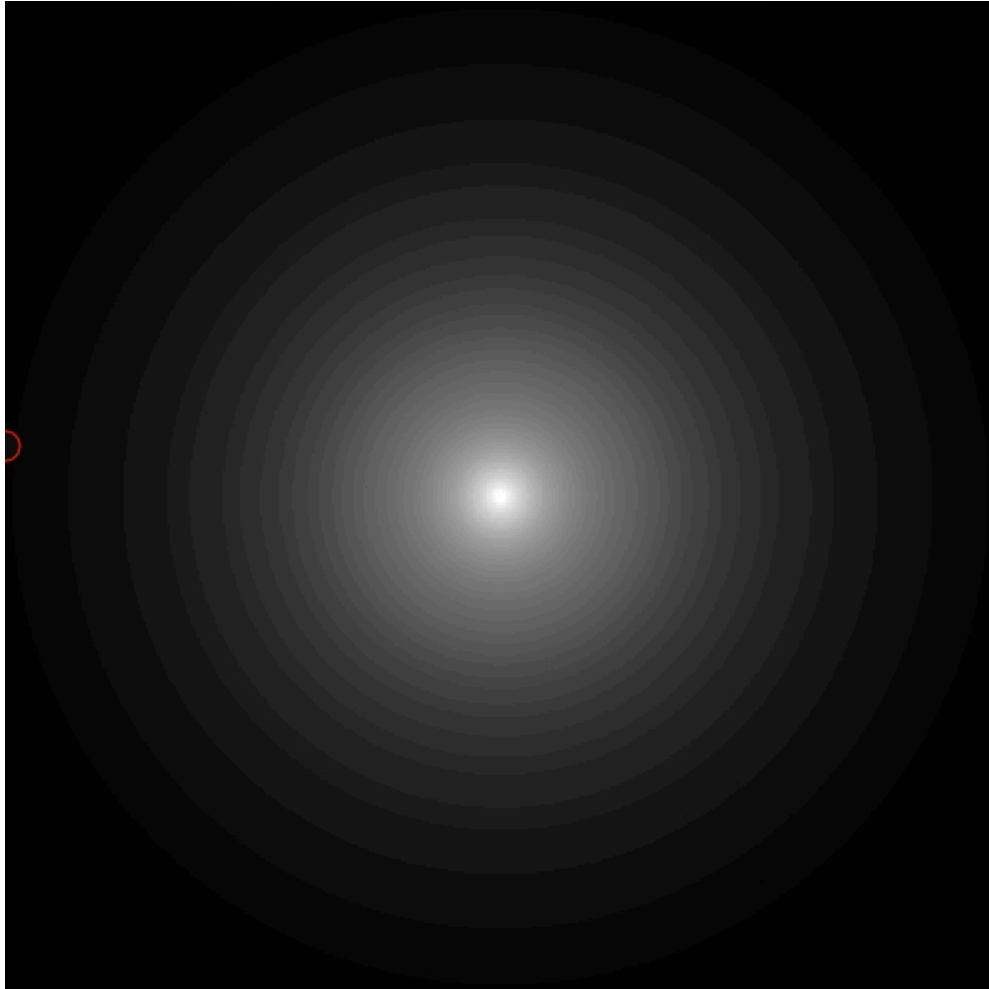
# By-eye Identification



# Grid Search for Best Model



# Microlensing with 1-body: $t_0$ , $u_0$ , $t_E$



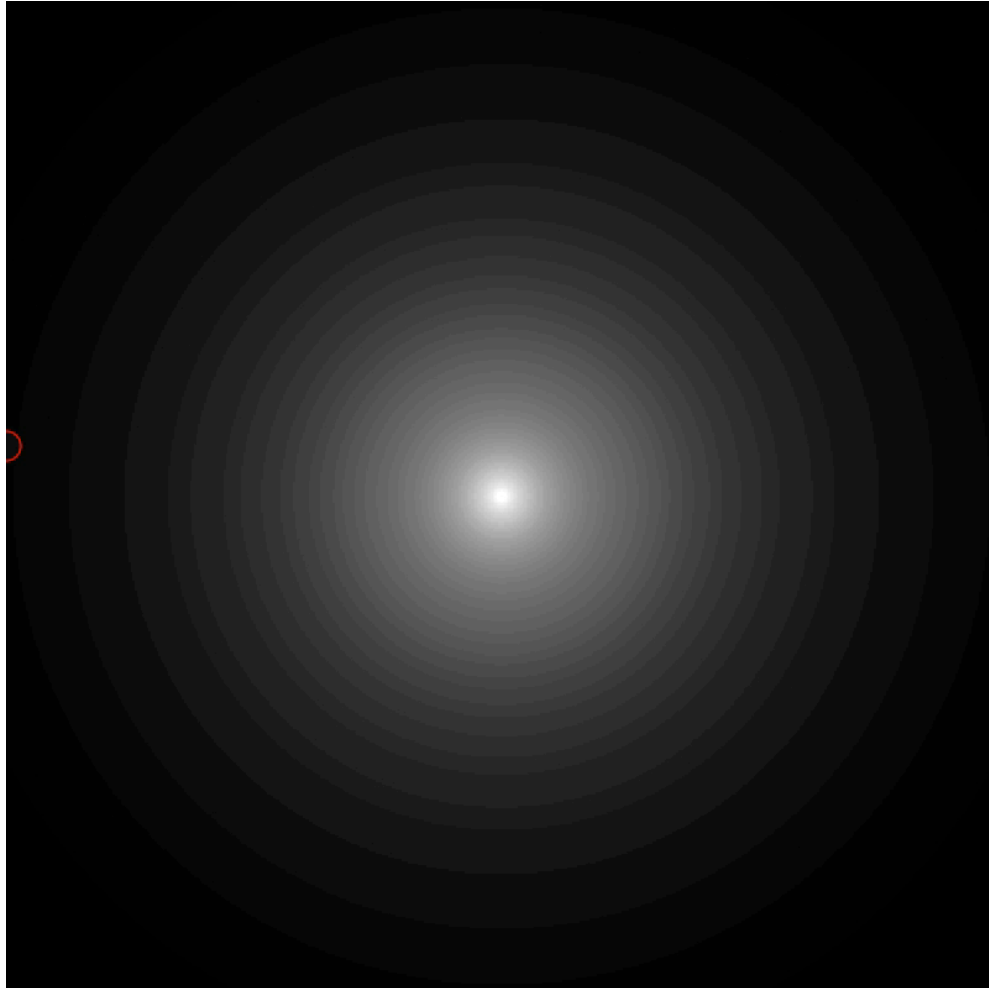
magnification =

$$A(u) = \frac{u^2 + 2}{u\sqrt{u^2 + 4}}$$

$$u = \sqrt{u_0^2 + \frac{(t - t_0)^2}{t_E^2}}$$



Larger  $t_E$  = Slower

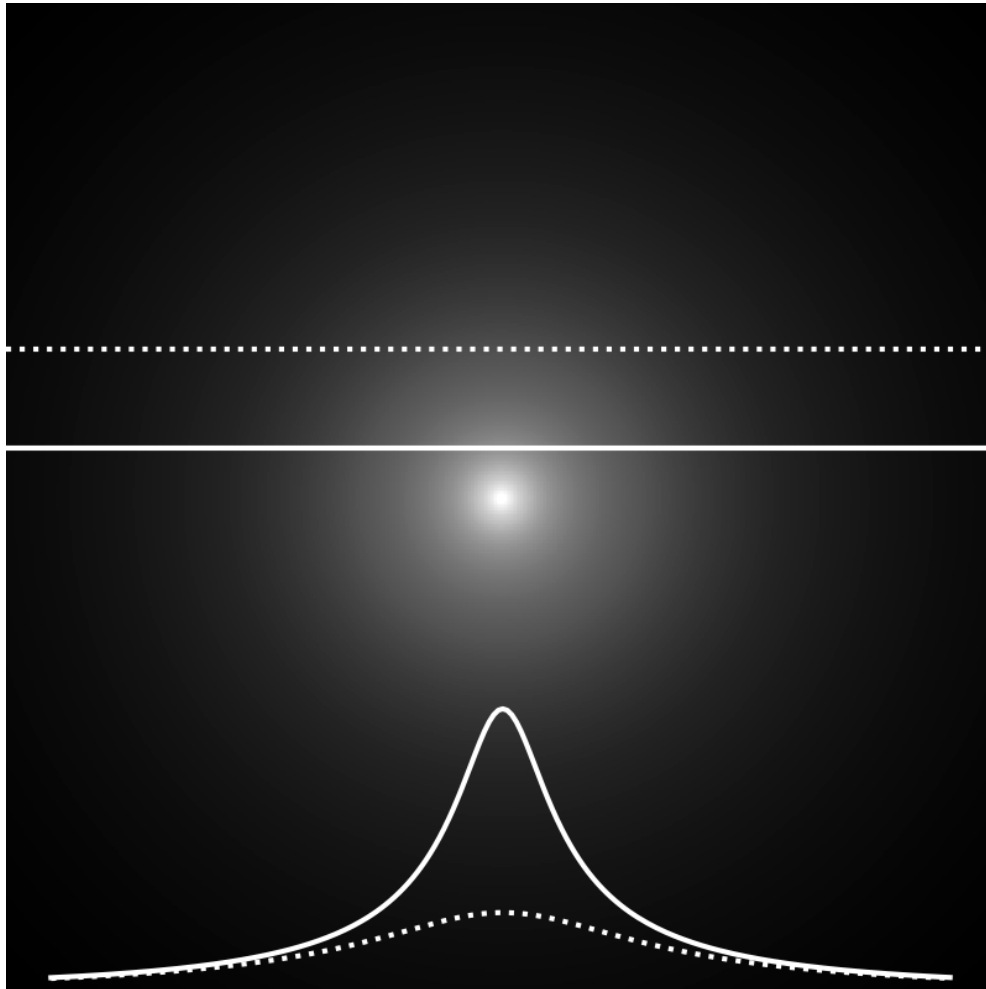


magnification =

$$A(u) = \frac{u^2 + 2}{u\sqrt{u^2 + 4}}$$

$$u = \sqrt{u_0^2 + \frac{(t - t_0)^2}{t_E}}$$

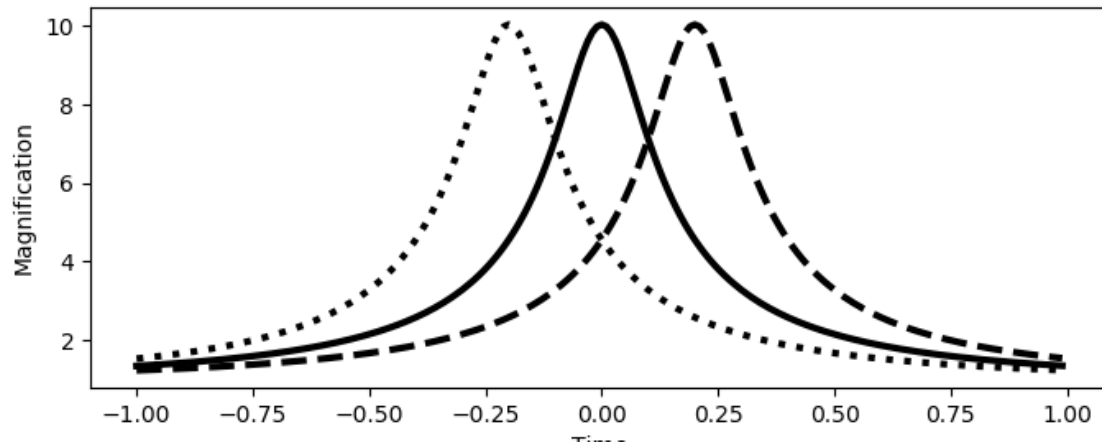
Larger  $u_0$  = Smaller Magnification



$$\text{magnification} = A(u) = \frac{u^2 + 2}{u\sqrt{u^2 + 4}}$$

$$u = \sqrt{u_0^2 + \frac{(t - t_0)^2}{t_E^2}}$$

$t_0$  shifts the light curve in time



magnification =

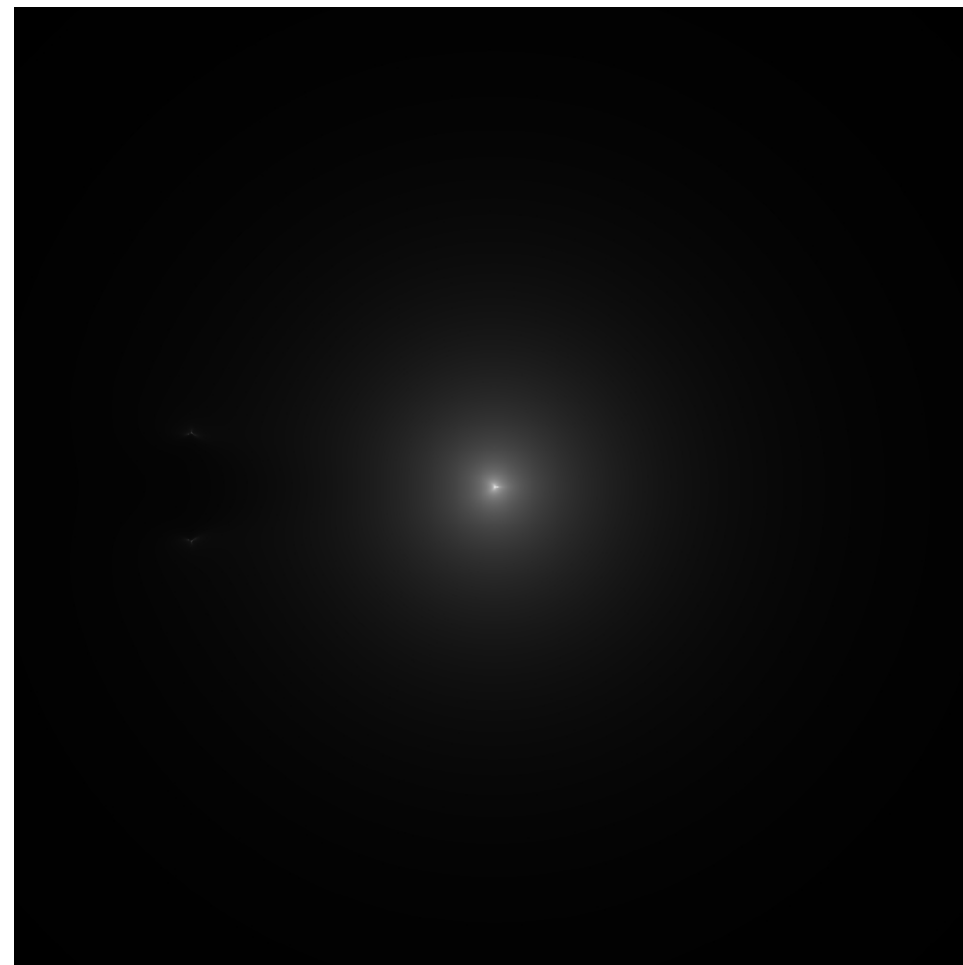
$$A(u) = \frac{u^2 + 2}{u\sqrt{u^2 + 4}}$$

$$u = \sqrt{u_0^2 + \frac{(t - t_0)^2}{t_E}}$$

# Microlensing with 2-bodies: $s$ , $q$ , $\alpha$

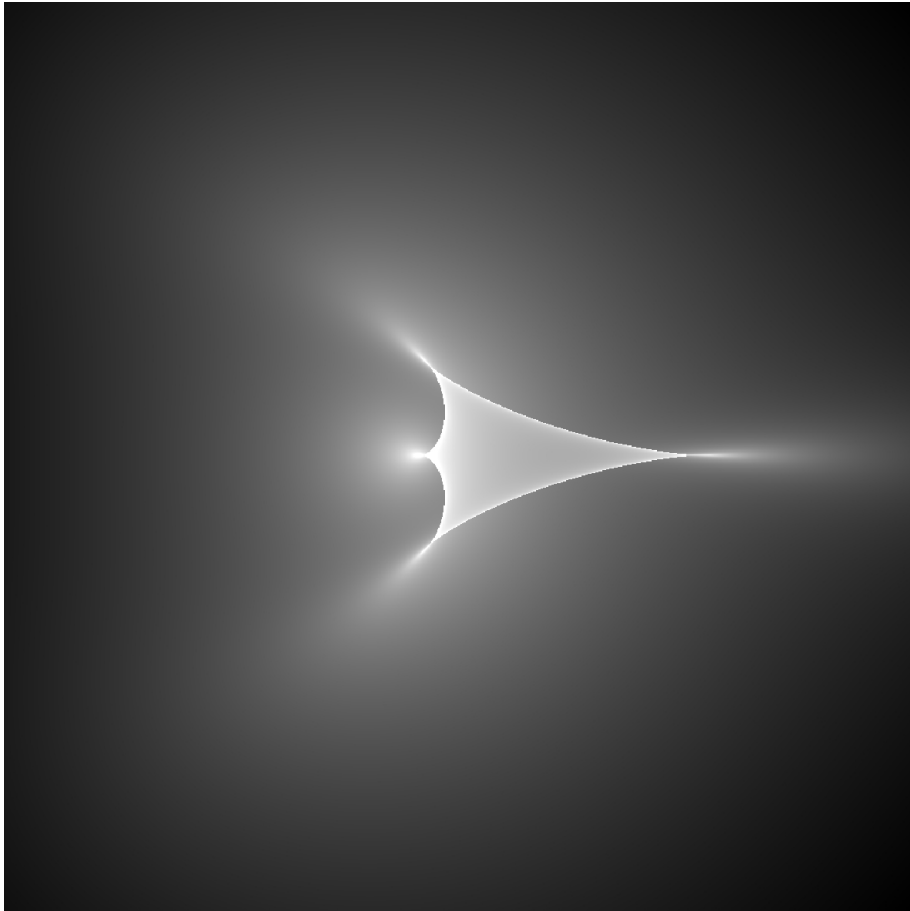


1-body



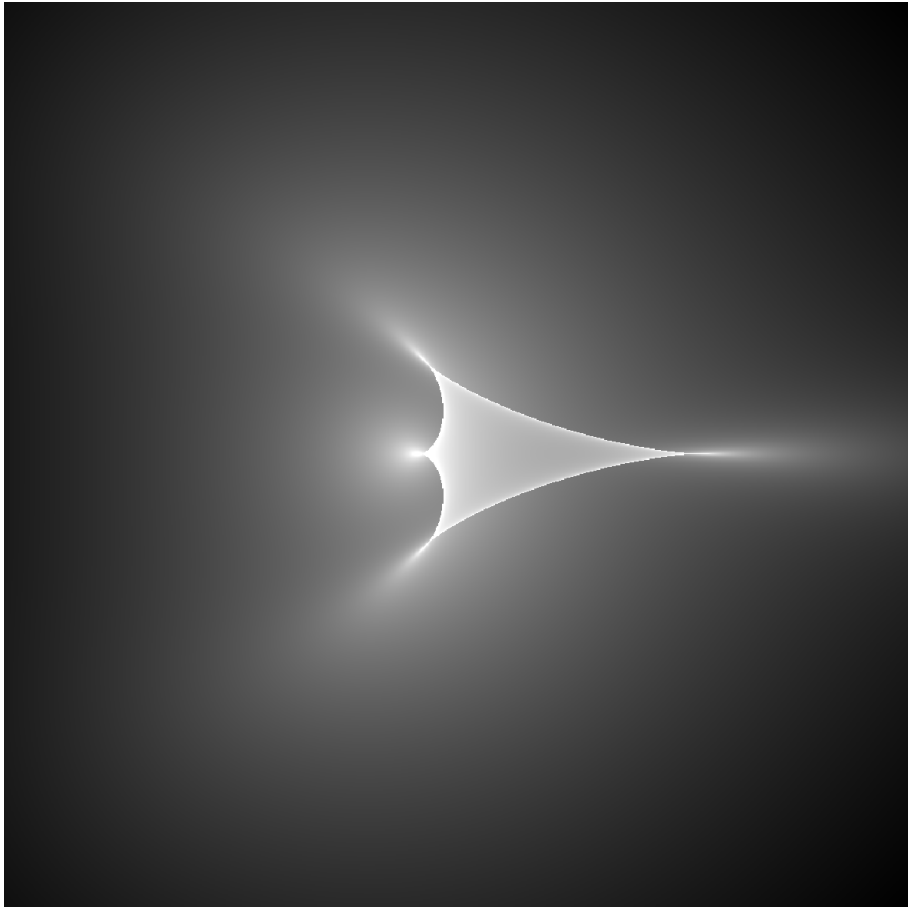
2-bodies

# Microlensing with 2-bodies: Caustics



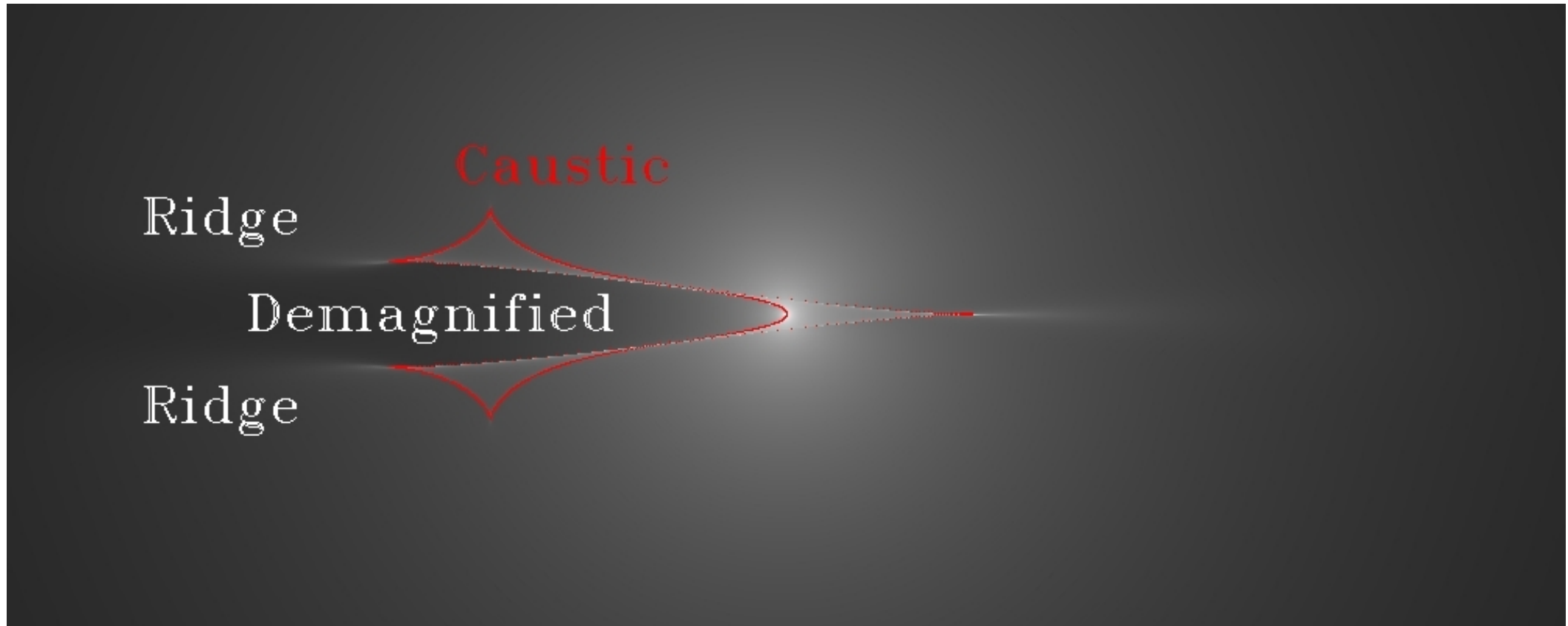
$$\text{magnification} = A(\mathbf{u}) = \frac{1}{|\det J|}$$

# Microlensing with 2-bodies: Caustics

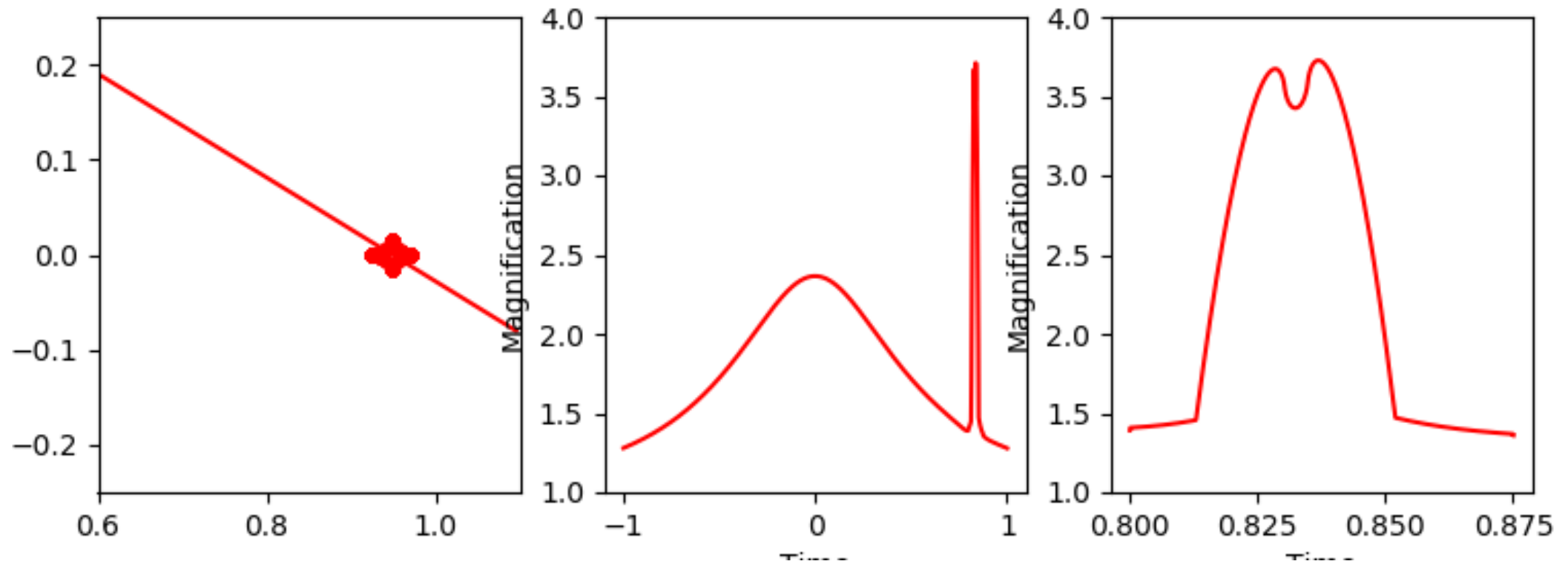


$$\text{magnification} = A(\mathbf{u}) = \frac{1}{|\det J|}$$

s, q affect the topology of the caustic

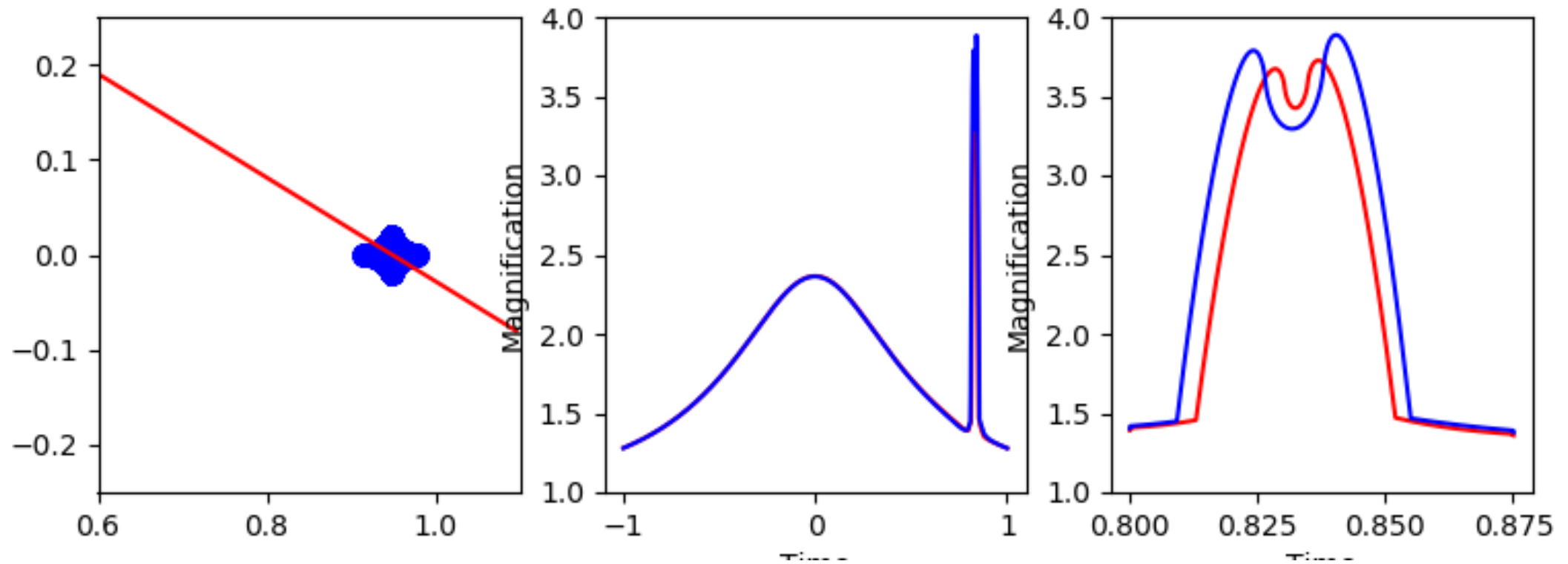


How do  $(s, q, \alpha)$  affect the light curve?

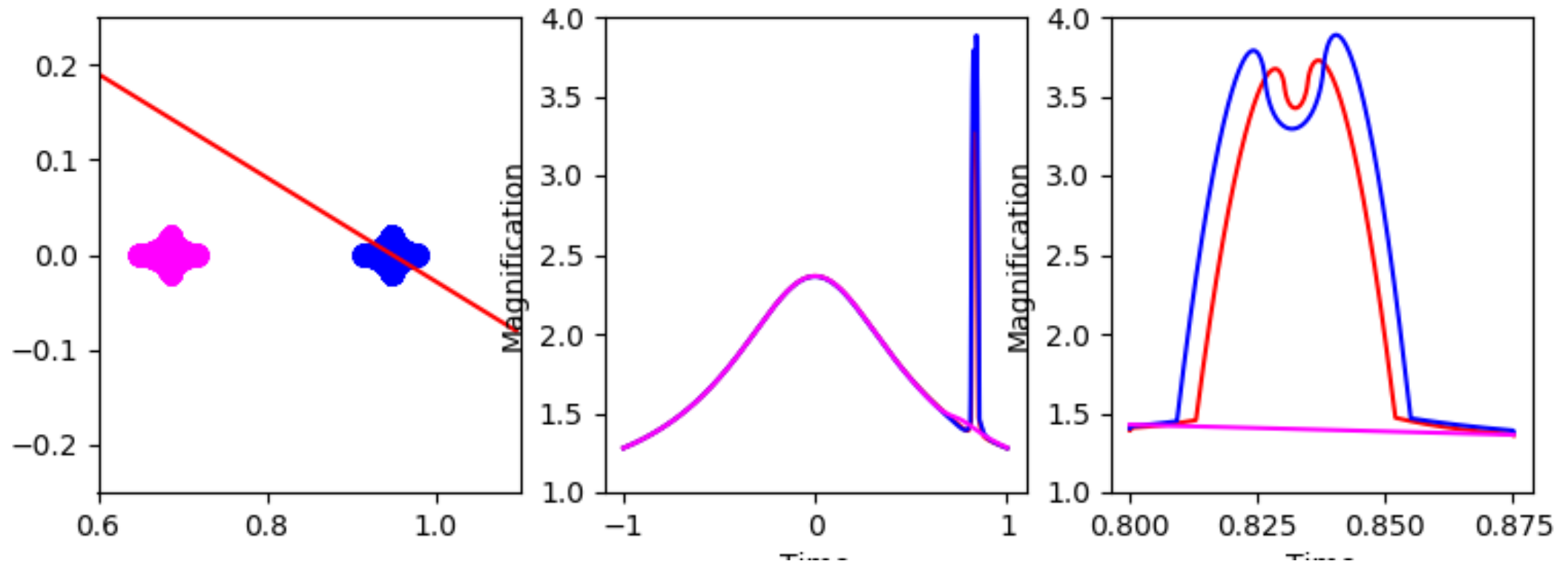




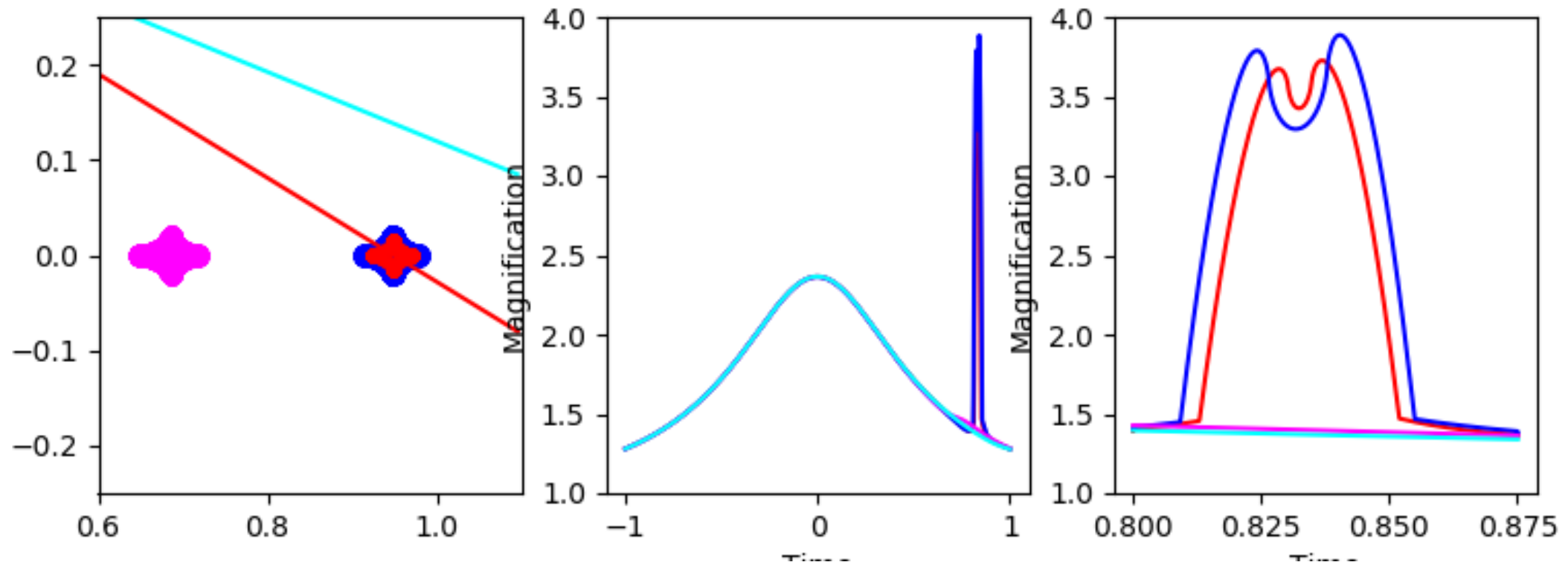
Bigger  $q$  = bigger caustic = bigger signal



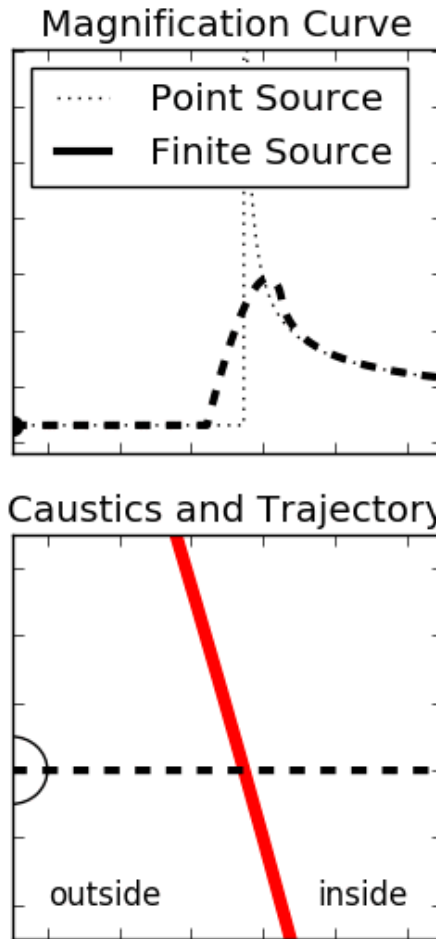
Smaller  $s$  moves the caustic  $\rightarrow$  no signal



Larger alpha moves source path  $\rightarrow$  no signal



$\rho = \text{source size} \rightarrow \text{integrated magnification}$



$f_{\text{source}}, f_{\text{blend}}$  = The flux parameters

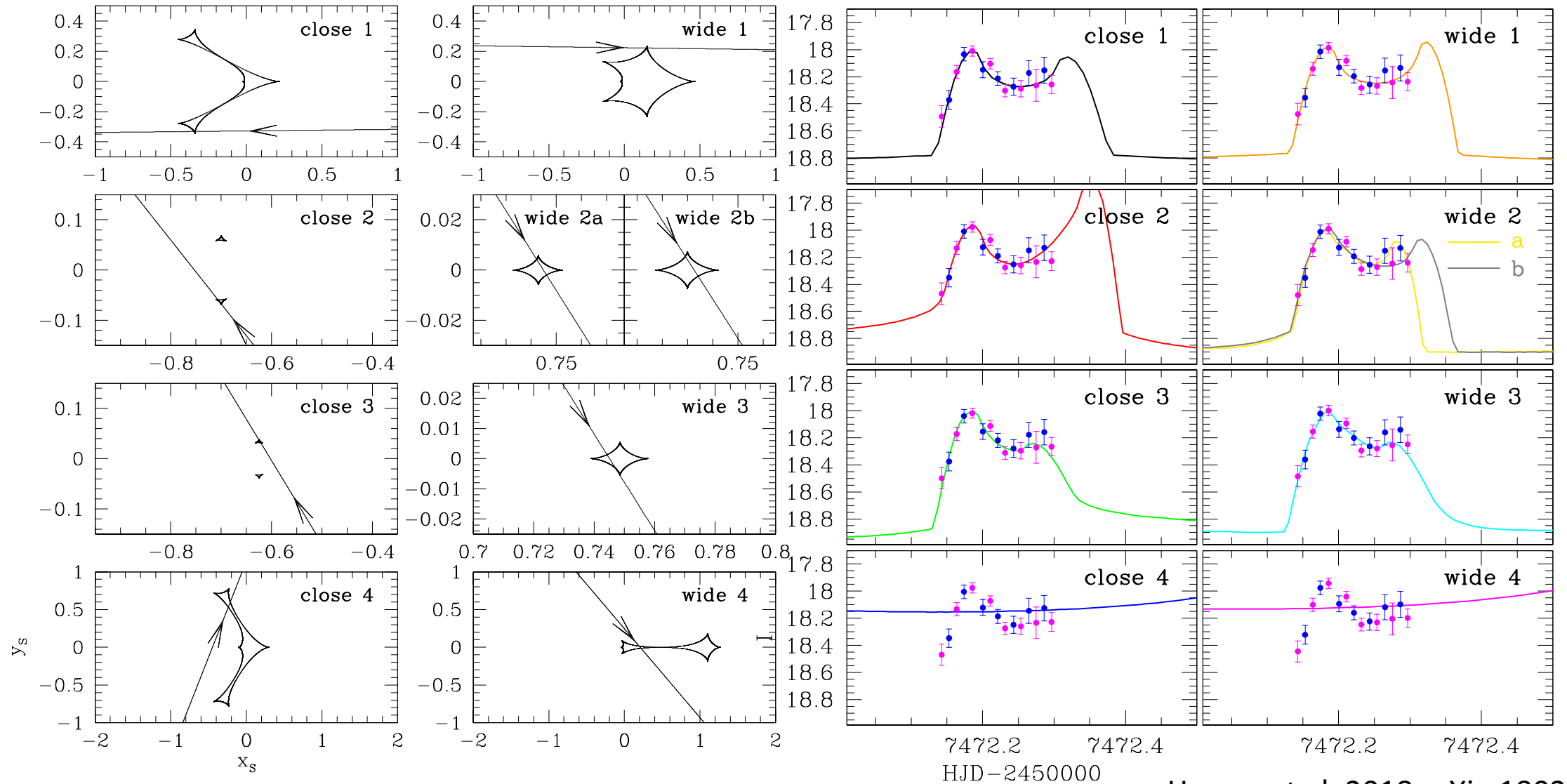
$$f_{\text{observed}} = f_{\text{source}} A(t) + f_{\text{blend}}$$

$$W149_{\text{observed}} = 18 - 2.5 \log_{10}(f_{\text{observed}})$$

# Other Physics

- Parallax = non-inertial observer frame, e.g. the Earth accelerates  
( $\pi_{E_N}$ ,  $\pi_{E_E}$ )
- Lens motion = two gravitationally bound bodies orbit each other  
( $ds_{dt}$ ,  $d\alpha_{dt}$ )
- Multiple source stars
  - 2 luminous sources
  - Orbital motion of the source

# Finding the Global Minimum: Multiple Minima



Given the complexity of the likelihood space, what are the best techniques for finding the global minimum?



# Resources

- Data Challenge Website: <http://microlensing-source.org/data-challenge-guidelines/>
- Codes for Generating Microlensing Models:
  - MulensModel: <https://github.com/rpoleski/MulensModel>
  - pyLIMA: <https://github.com/ebachelet/pyLIMA>
- Background on Microlensing:
  - Website: <http://microlensing-source.org/>
  - Review Articles:
    - Gaudi 2010 in Exoplanets edited by S. Seager
    - Gaudi 2012, ARA&A, 50, 411
    - Yee 2014 Section 7 of Exoplanet Detection Techniques in Protostars and Planets VI, ed. Beuther, Klessen, Dullemond, and Henning
  - Mathematics:
    - Schnieder & Weiss 1986, A&A, 164, 237
    - Dominik 1999, A&A, 349, 108