

HST - 0.01" 0.5"

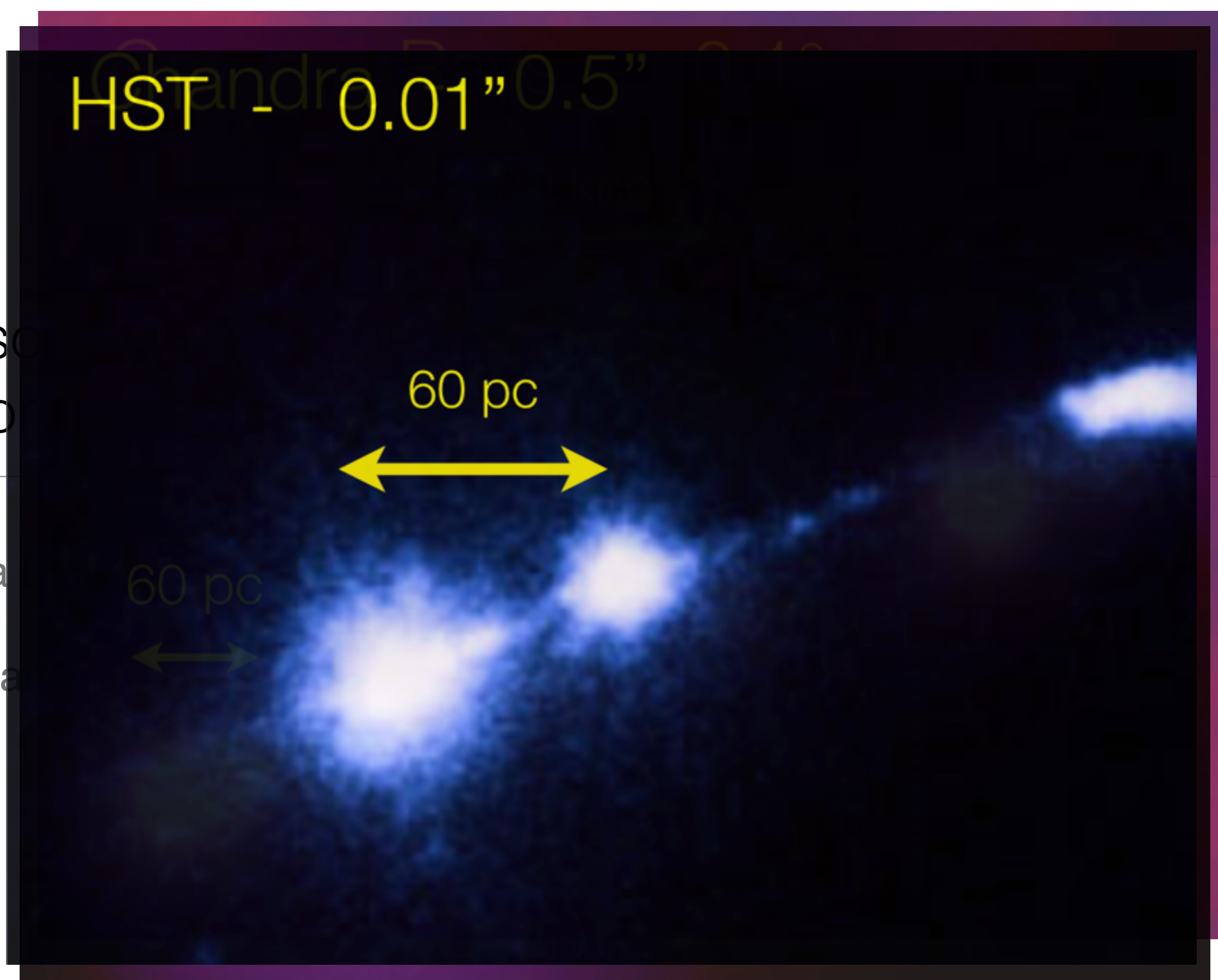
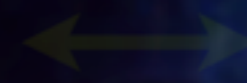
Reso
Stro

60 pc



Anna
Harva

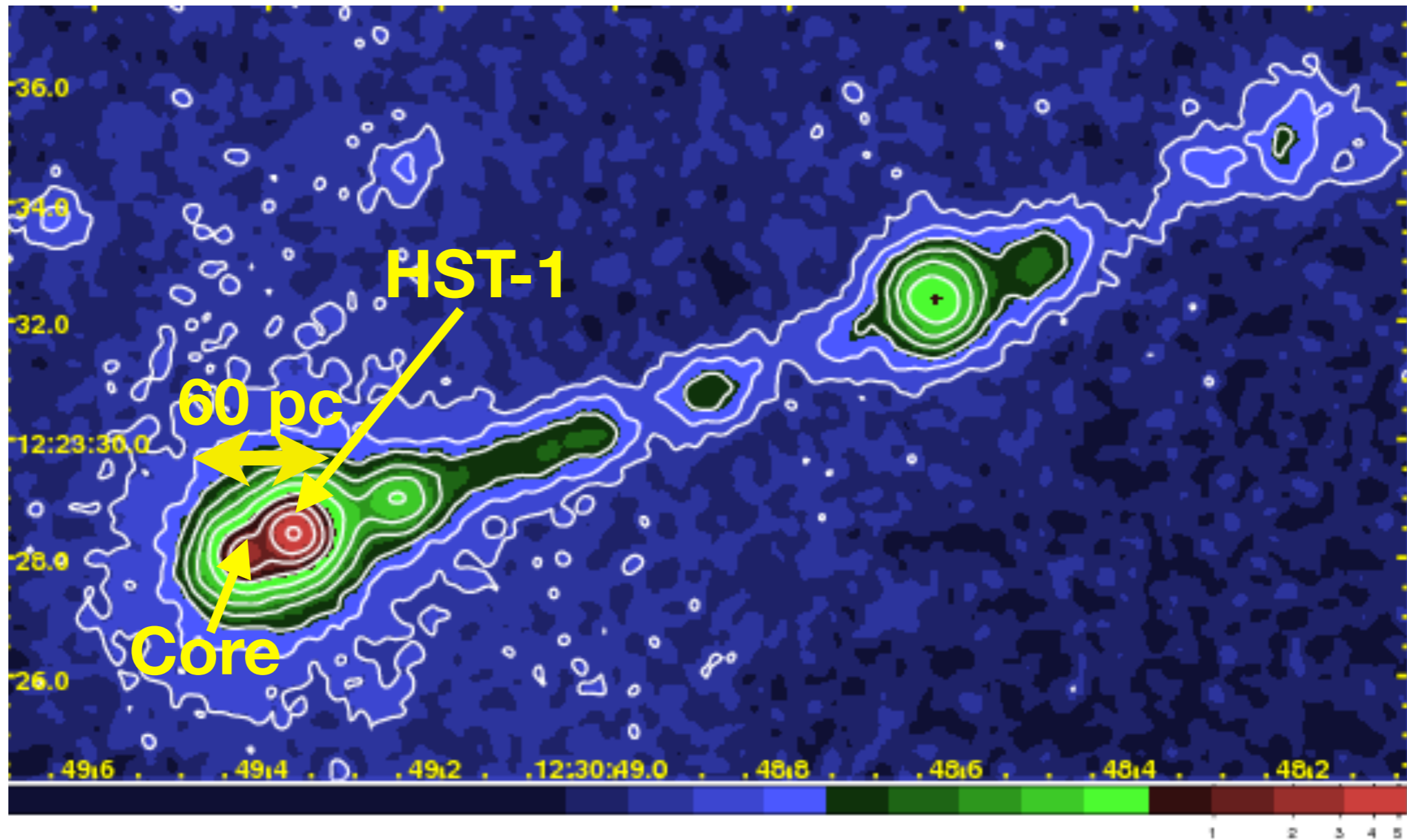
60 pc



X-Ray Jets - Lessons from Chandra

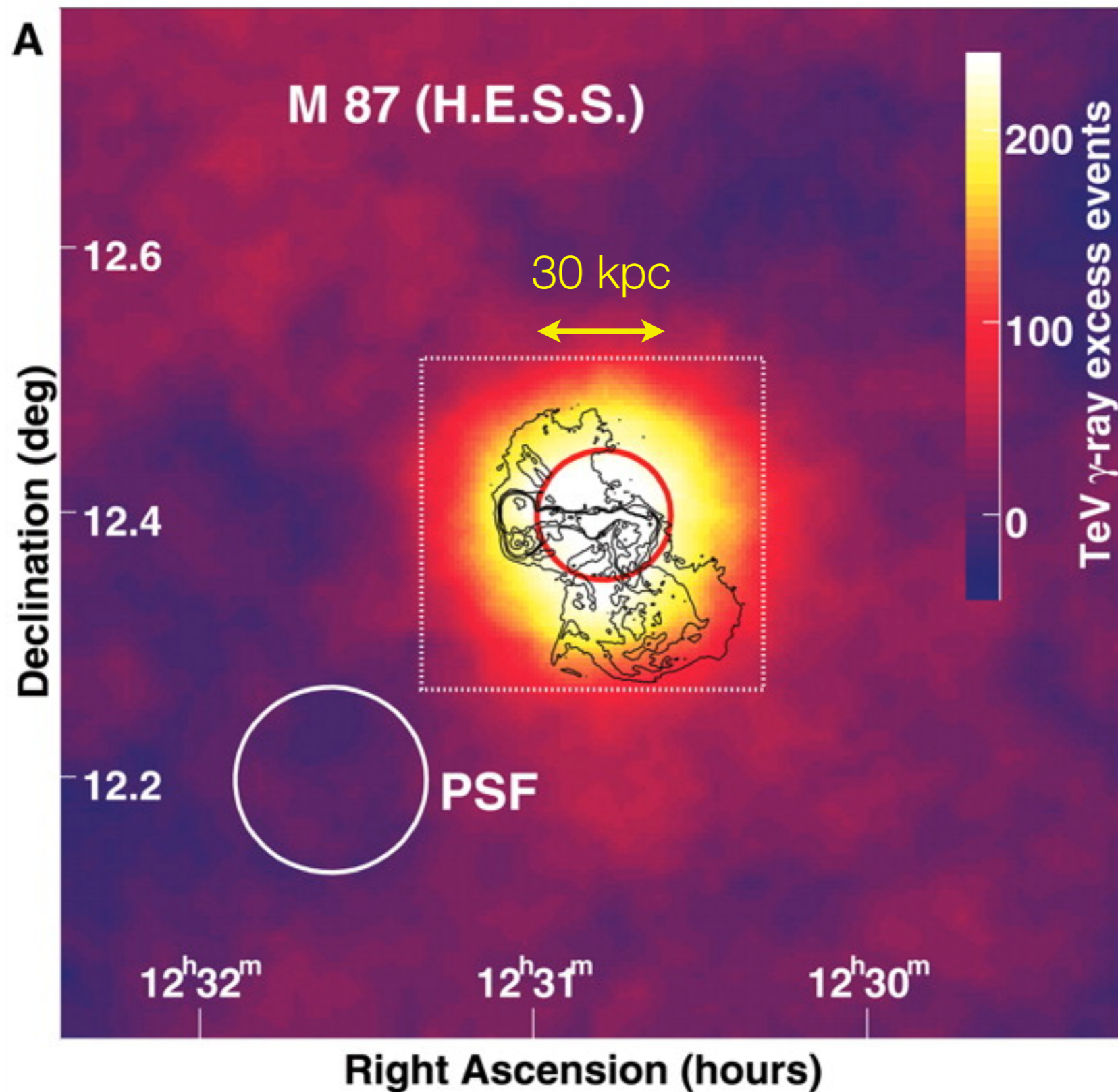
Increased x-ray emission by a factor of 50 from the HST-1 knot (Harris et al. 2006,2009)

Core and HST-1: Separation ~ 60 pc



Flares from knots along the jets

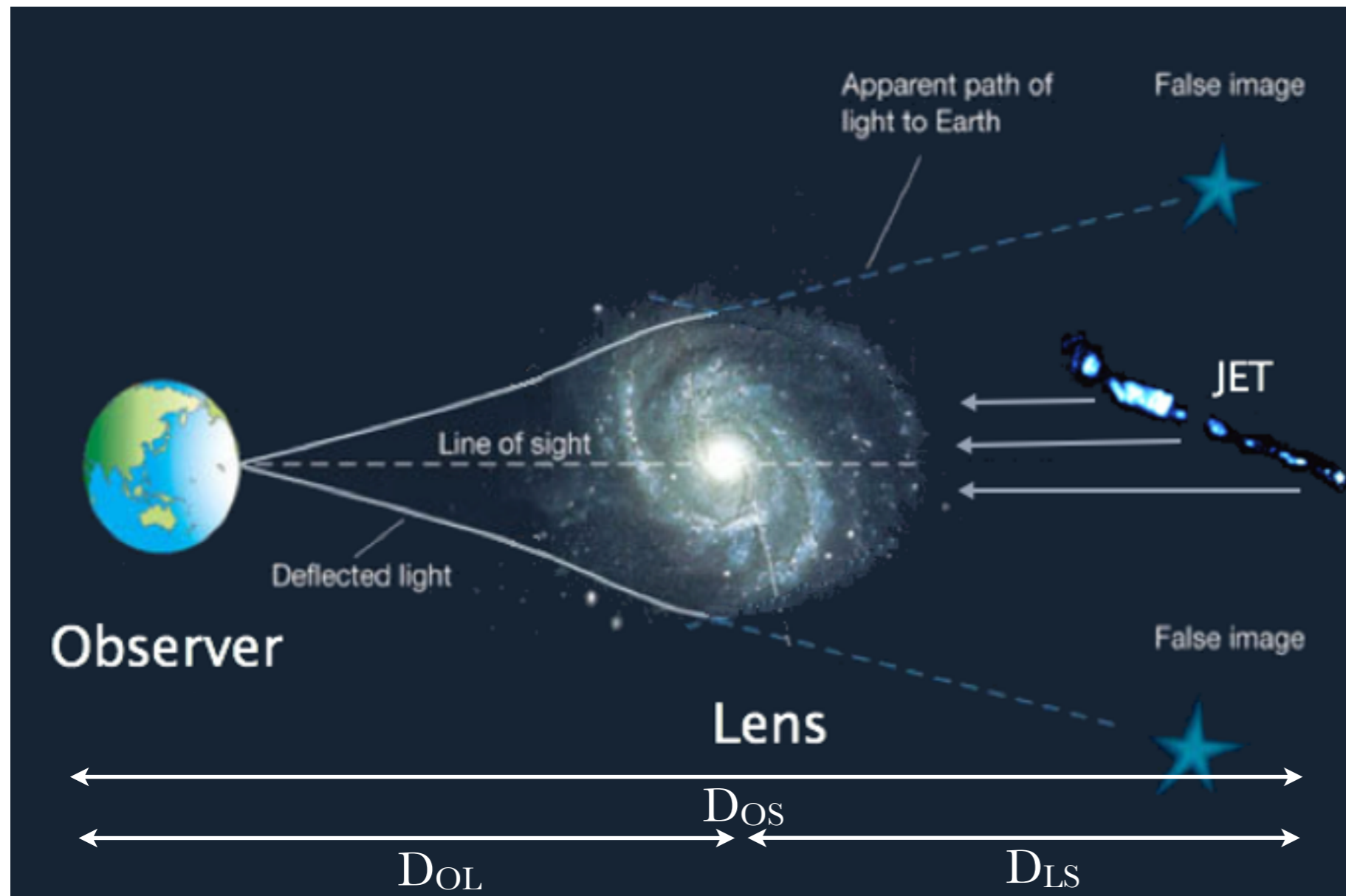
Ambiguity of Gamma-Ray Origin



Scientific Issues

- Frequency of M87-like variability
- Structure of gamma-ray jets
- Spatial origin of gamma-ray flares

M87 Gravitationally Lensed?



Deflection angle:

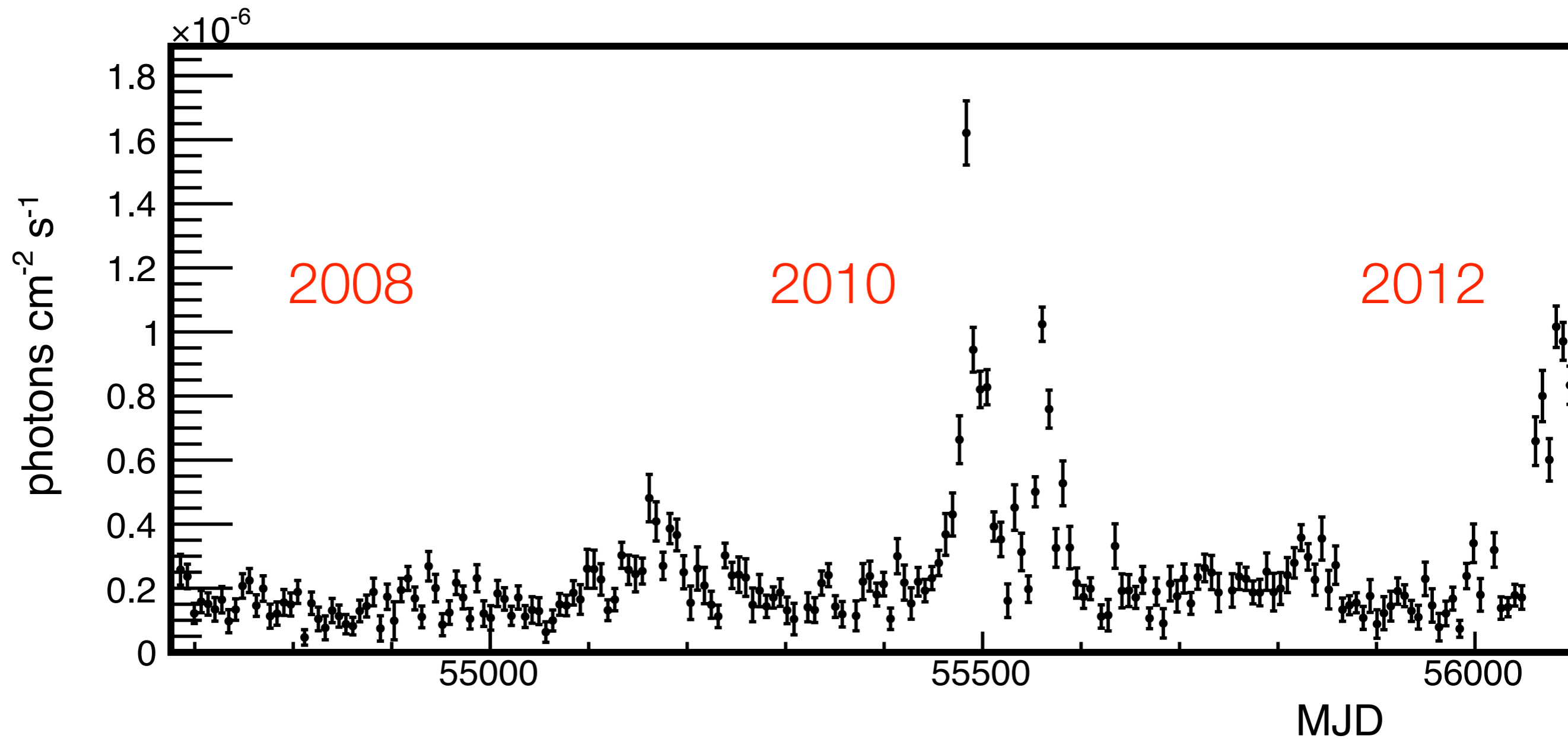
$$\alpha = \frac{4GM(r)}{c^2} \frac{1}{r}$$

Images separation - a few arcseconds
time delay
magnification ratio

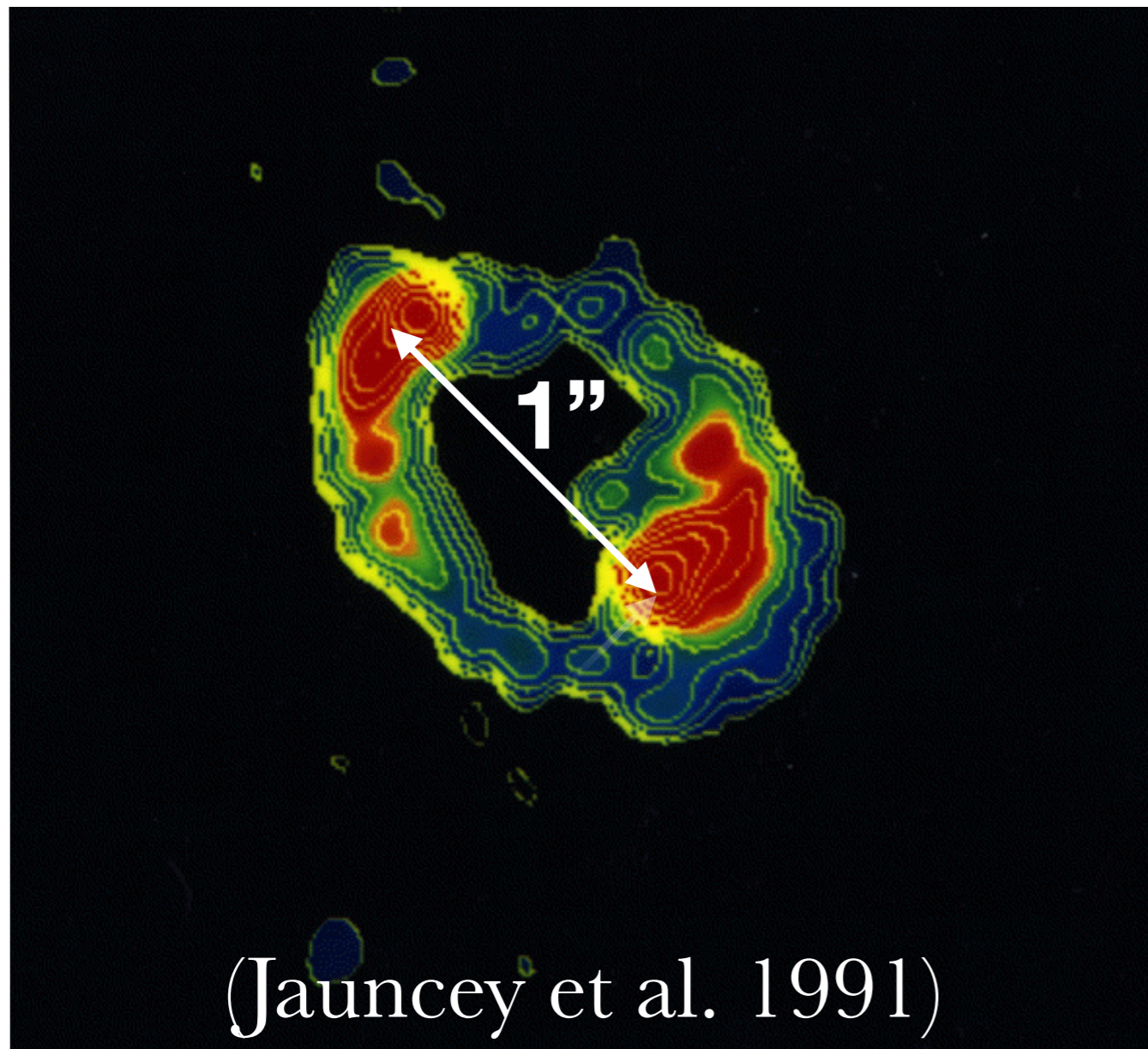
M87 as a Toy Model

- $z_s=1, z_l = 0.6$
- Einstein radius ~ 2.2 kpc ($0.45''$)
- 60 pc $\sim 0.01'' \sim 3\%$ Einstein radius
- Differences between the **core** and the **HST-1**:
 - **difference in time delay: ~ 2 days**
 - **difference in magnification ratio: ~ 0.2**

Temporal Resolution at Gamma Rays



Lensed Gamma-Ray Jets: PKS 1830-211



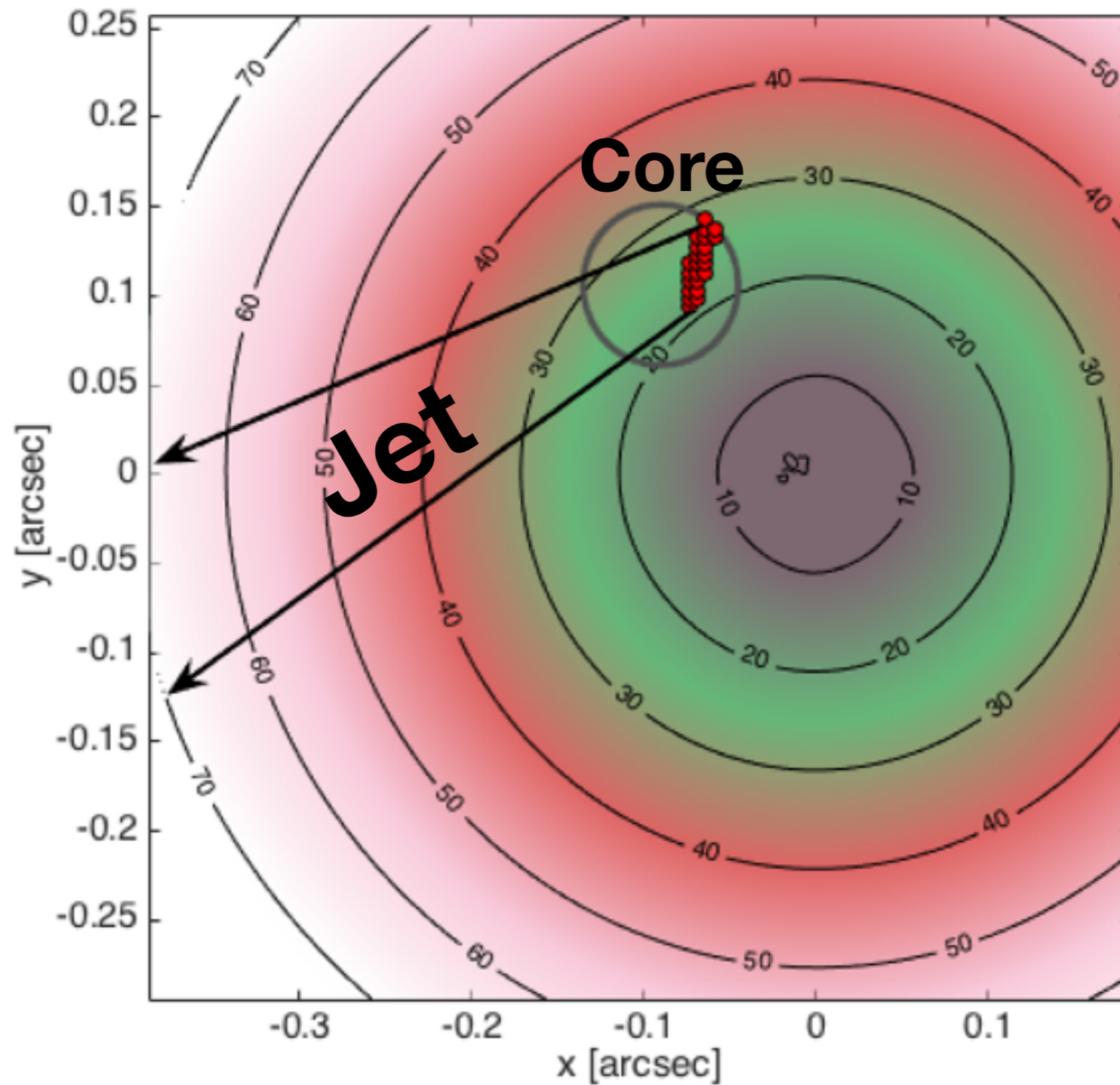
Source $z = 2.5$,
Lens $z = 0.9$

Radio Time Delay
 26 ± 5 days

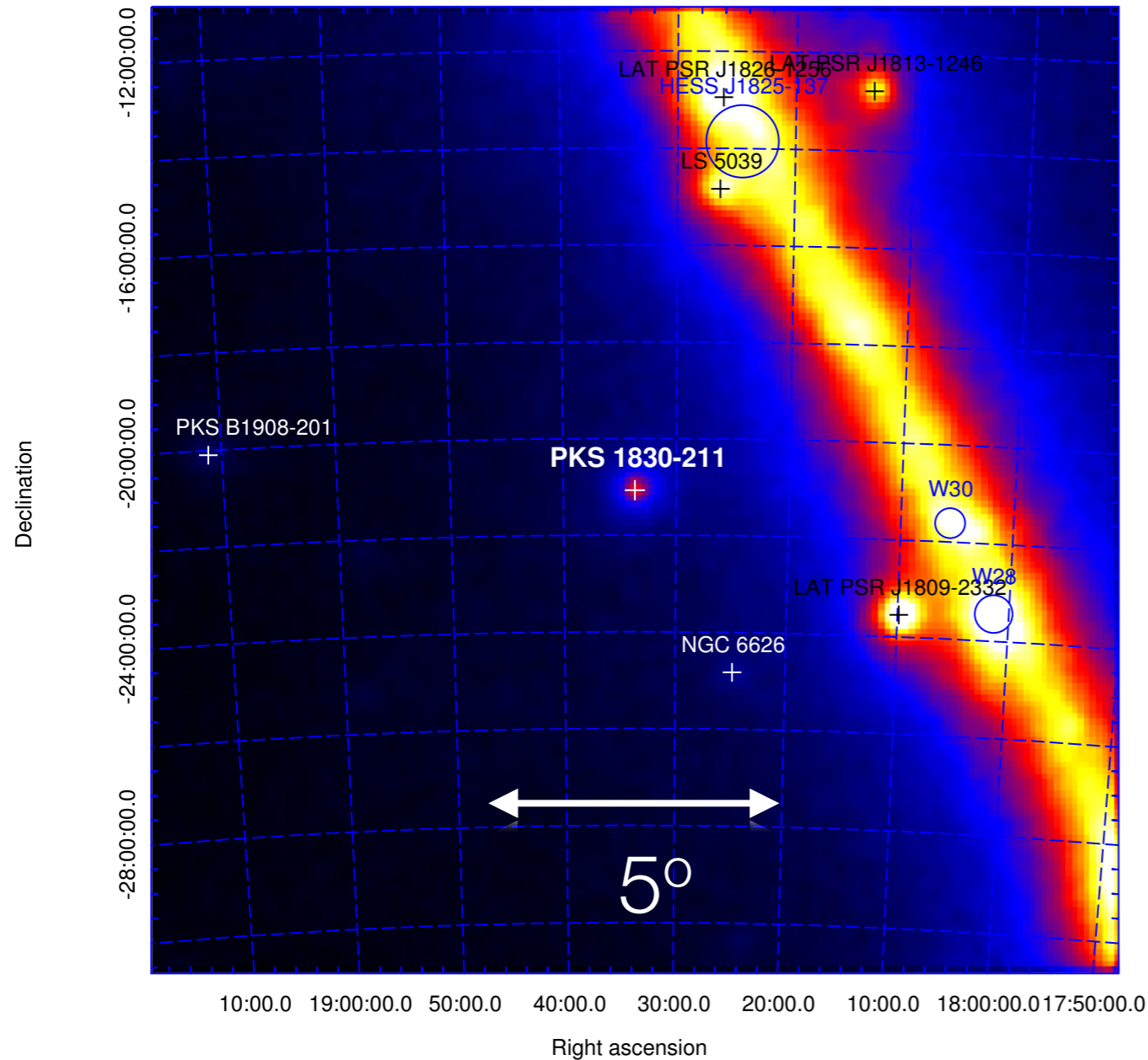
Magnification Ratio
 1.52 ± 0.05

(Lovell et al. 1998)

Properties of the Lensed System



Lensed Gamma-Ray Jets: PKS 1830-211

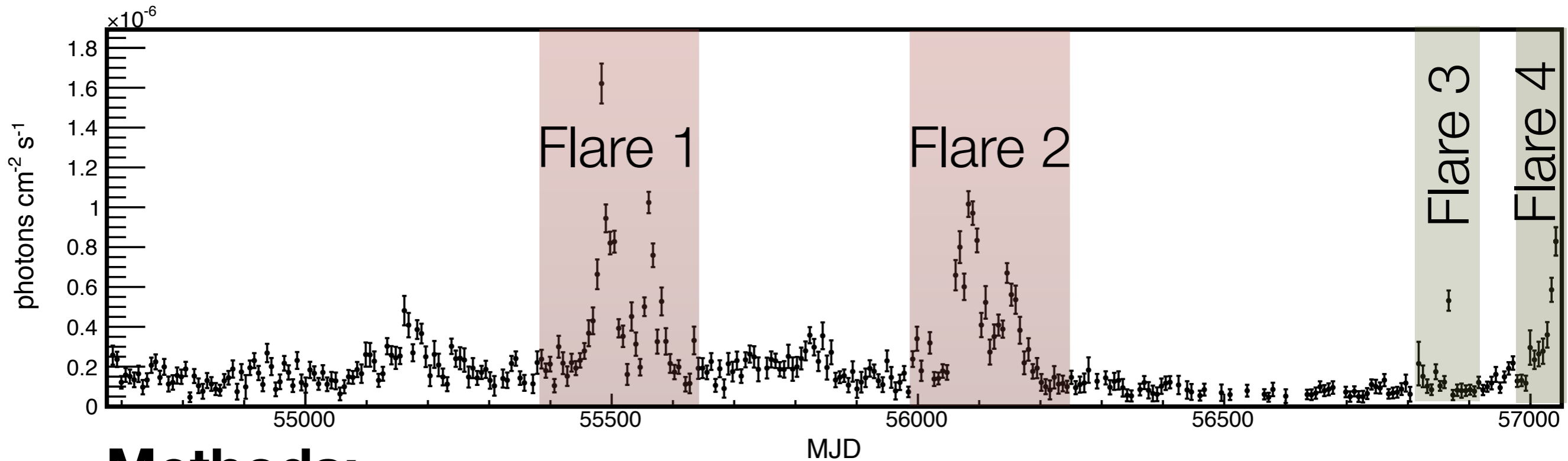


The first evidence of lensing at gamma-rays (Barnacka et al. 2011)

Gamma-Ray Time delay 27.1 ± 0.45 days

**Gamma-ray Flares
Time Delays ?**

Gamma-ray Flares: Time Delays



- **Methods:**

- The Autocorrelation Function
- The Double Power Spectrum
- The Maximum Peak Method

Characteristic of the Signal

Power Law Noise

$$S(f) \propto 1/f^\alpha$$

$\alpha \sim 2$ - Red Noise: Flaring State

$\alpha \sim 1$ - Pink Noise: Quiescent State

$\alpha \sim 0$ - White Noise

Double Power Spectrum

a - time delay

b - magnification ratio

I Fourier Transform

$$f(t) + bf(t+a) \xrightarrow{FT} \tilde{f}(\nu) + b\tilde{f}(\nu)e^{-2\pi i\nu a}$$

$$\tilde{g}(\nu) = \tilde{f}(\nu)(1 + be^{-2\pi i\nu a})$$

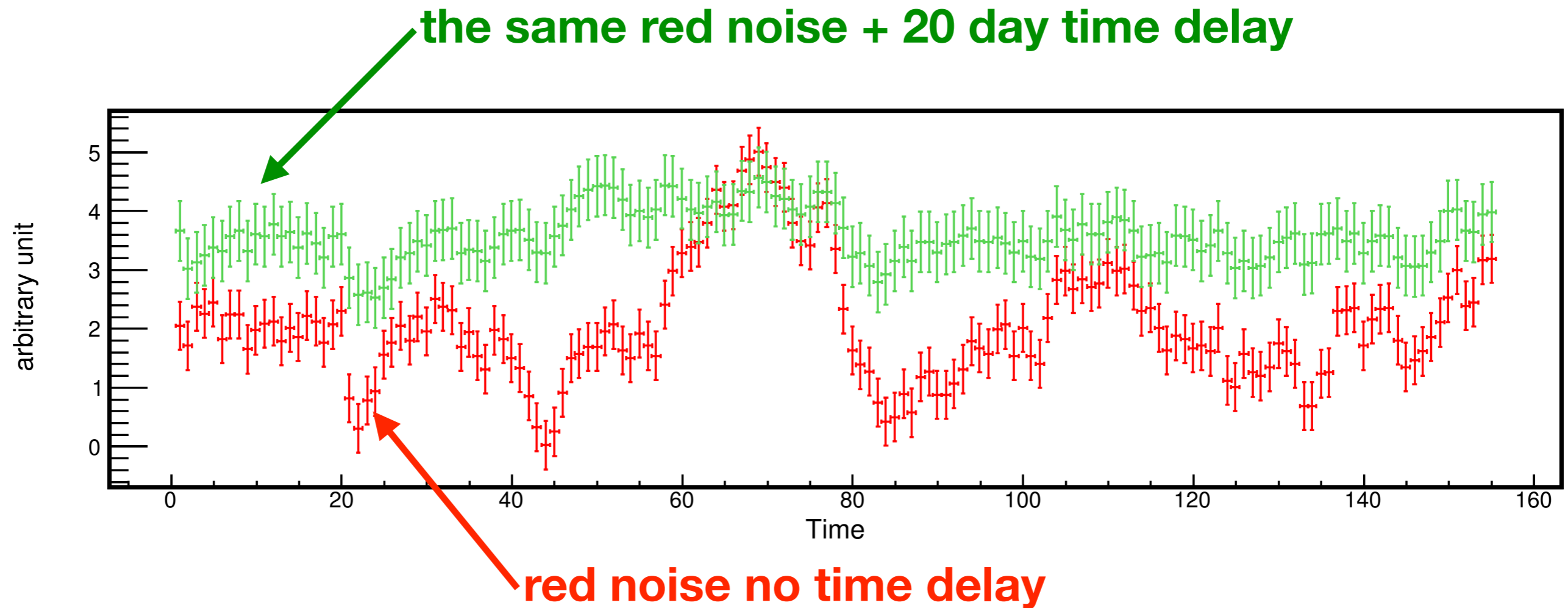
I Power Spectrum

$$P_\nu = |\tilde{g}(\nu)|^2 = |\tilde{f}(\nu)|^2(1 + b^2 + 2bcos(2\pi\nu a))$$

The measured Power Spectrum is the product of the “true” power spectrum of the source times a periodic component with a period equal to the inverse of the relative time delay “a”

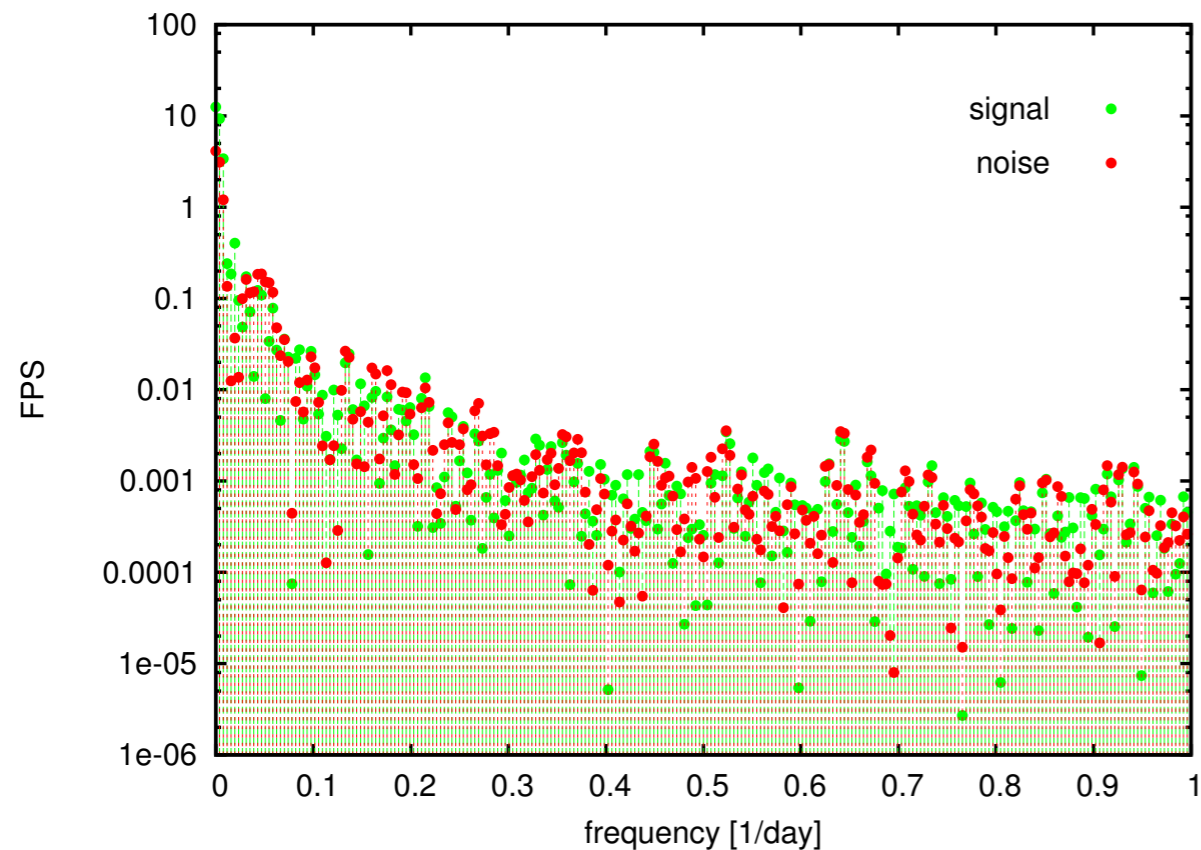
The cepstrum method (Bogert et al. 1963)

Double Power Spectrum - Monte Calo Simulations

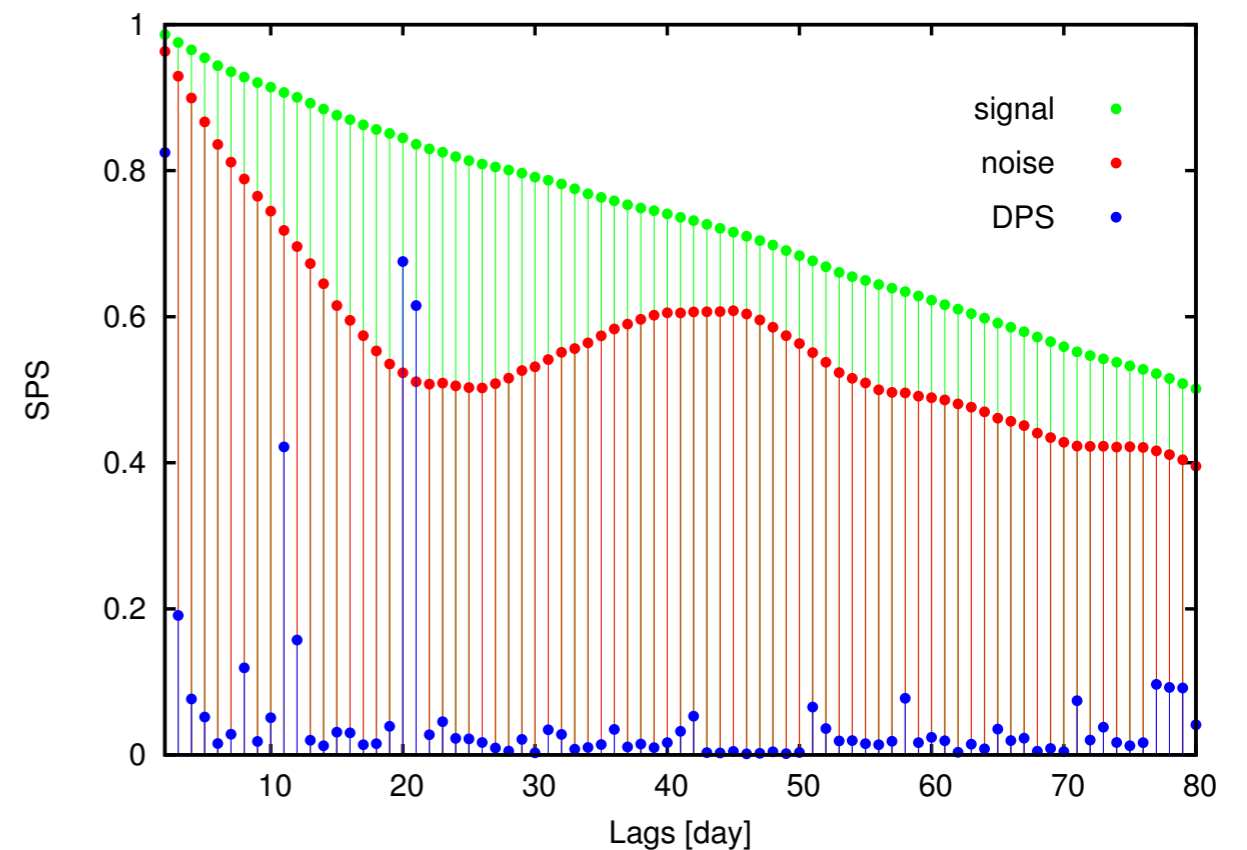


Double Power Spectrum - Monte Calo Simulations

I Power Spectrum



II Power Spectrum



Red - red noise, no time delay simulated, no signal processing

Green - red noise, 20 days time delay, no signal processing

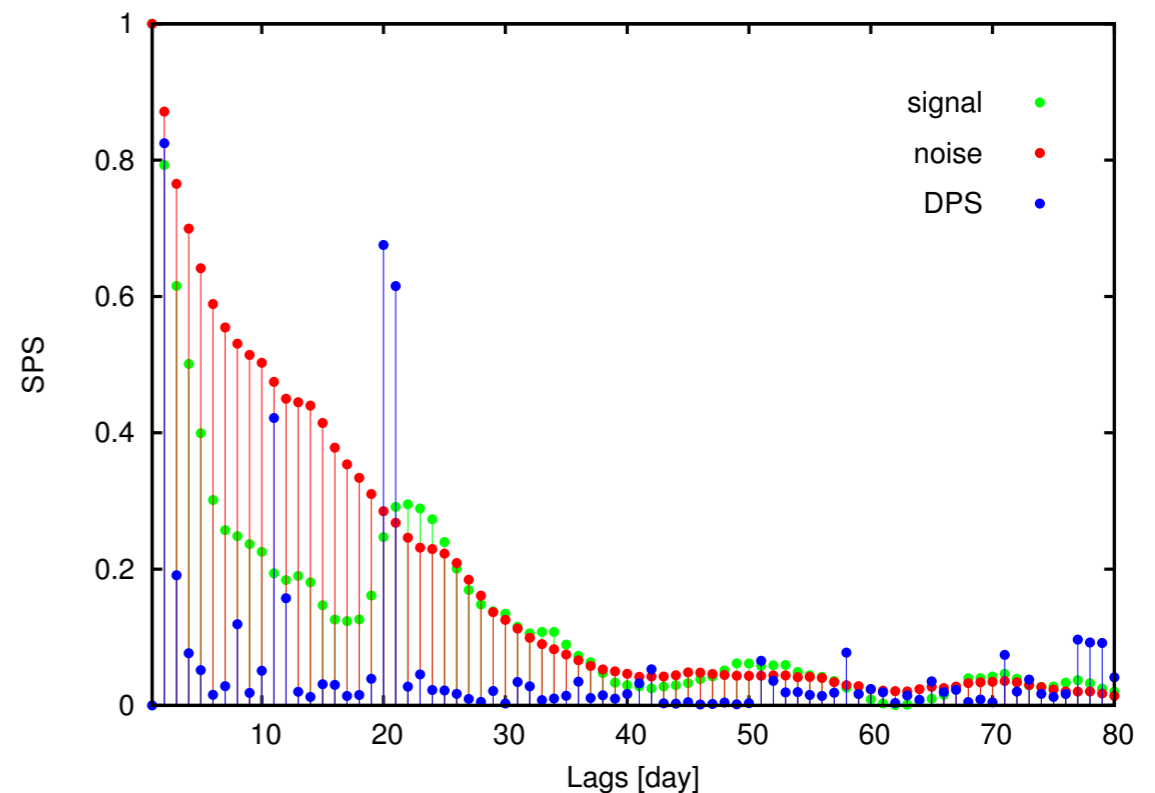
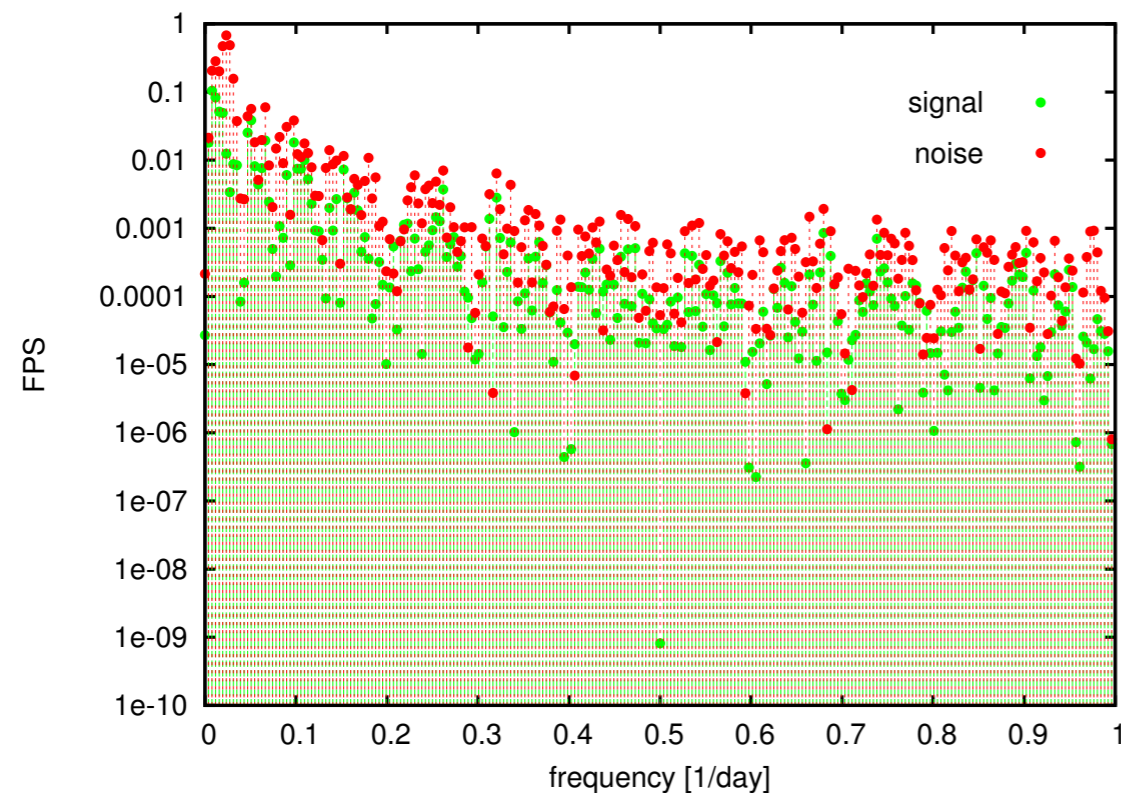
Blue - red noise, 20 days time delay, **after signal processing**

Signal Processing - Step 1

Based on widely used methods: Oppenheimer & Schafer (1975), Brault & White (1971)

Step 1: The First Power Spectrum

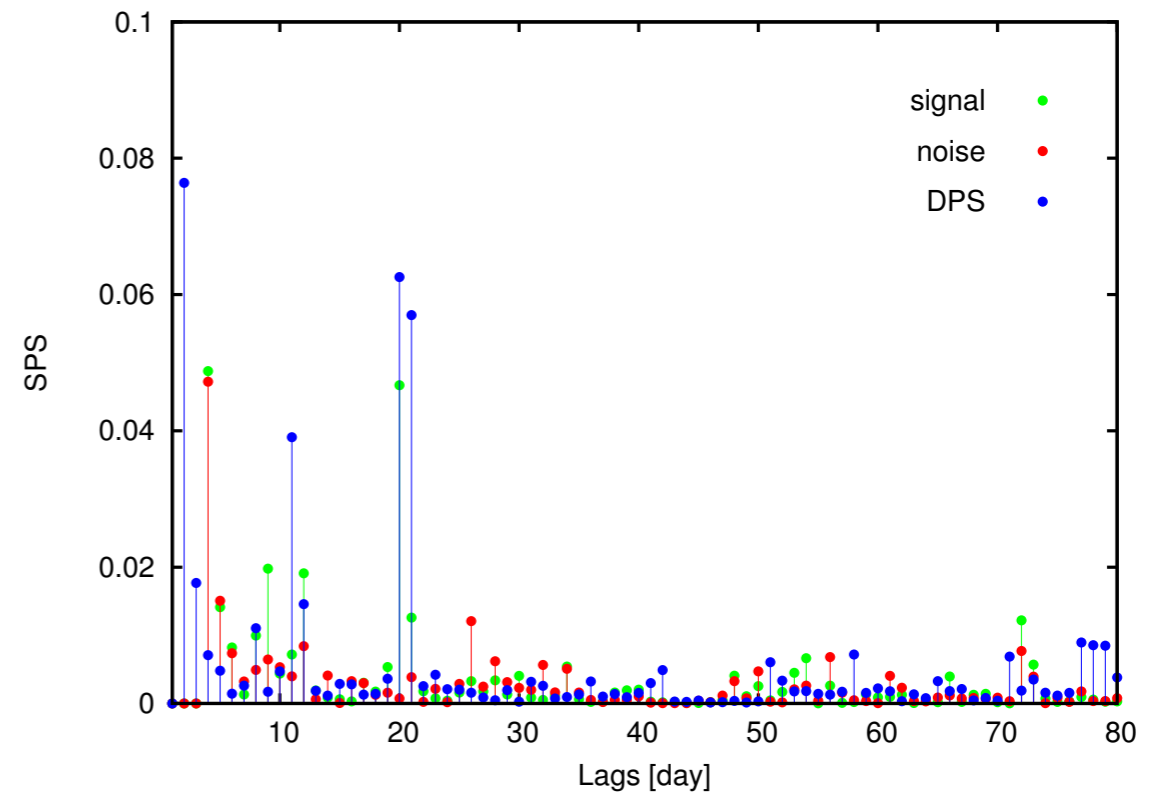
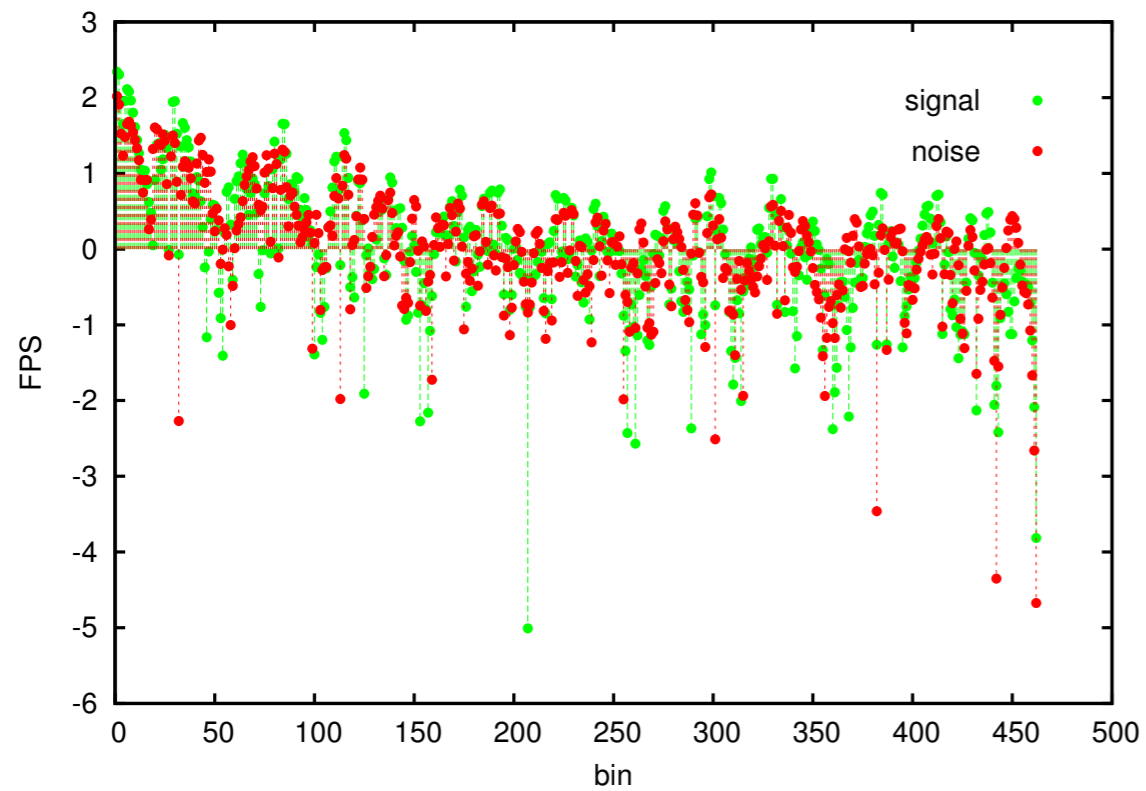
Mean Extraction and Windowing, Zero Padding, Doubling the Points



Signal Processing - Step 2

Step 2: The Second Power Spectrum

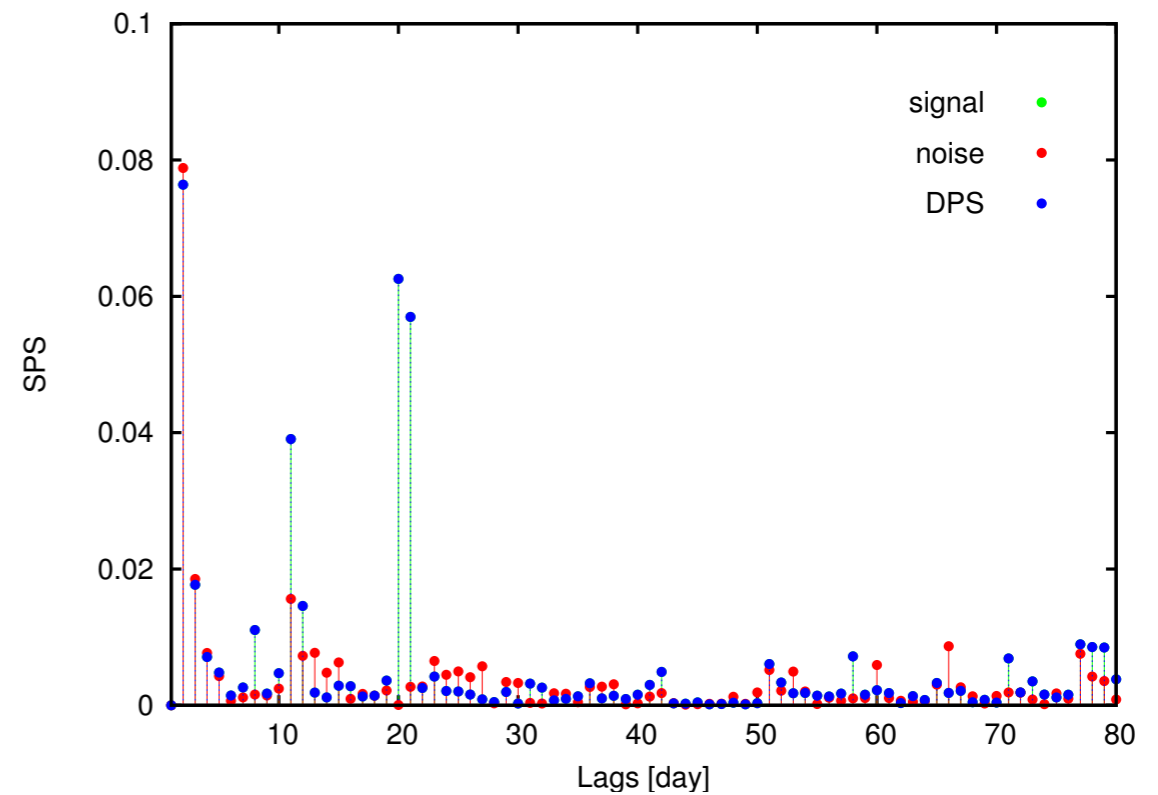
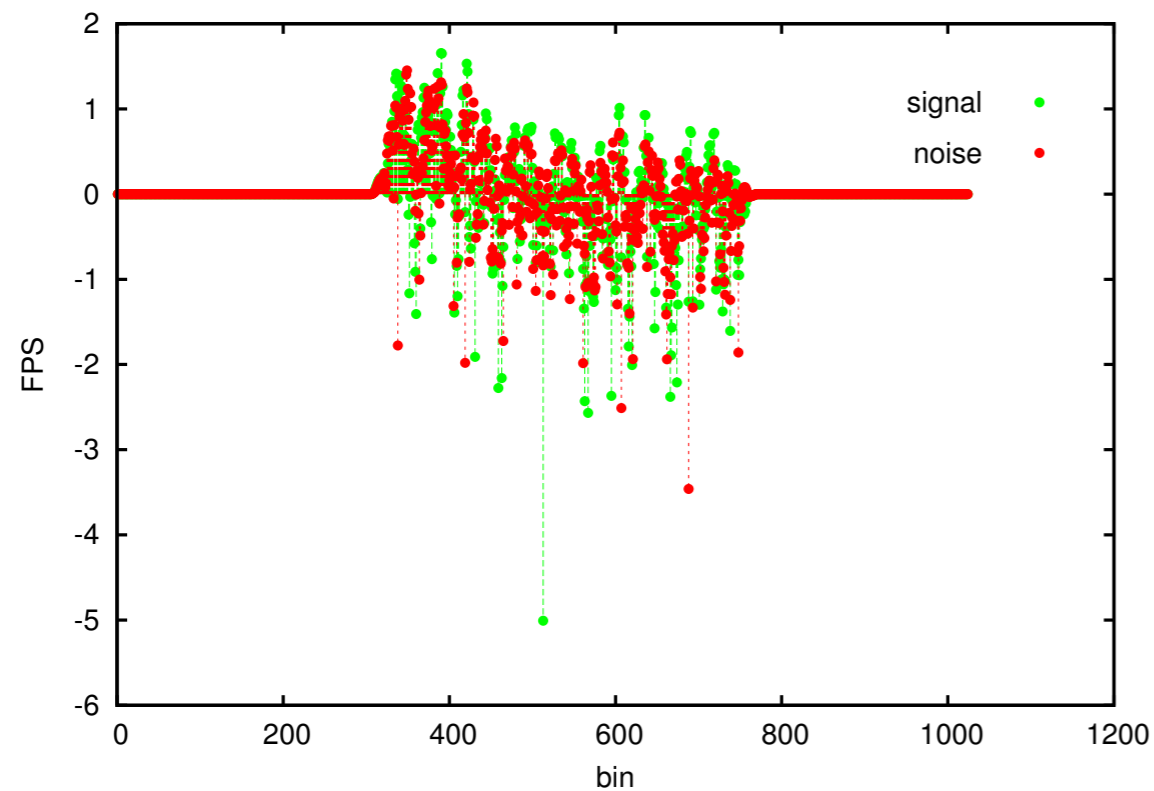
Flattening and Mean Extraction



Signal Processing - Step 3

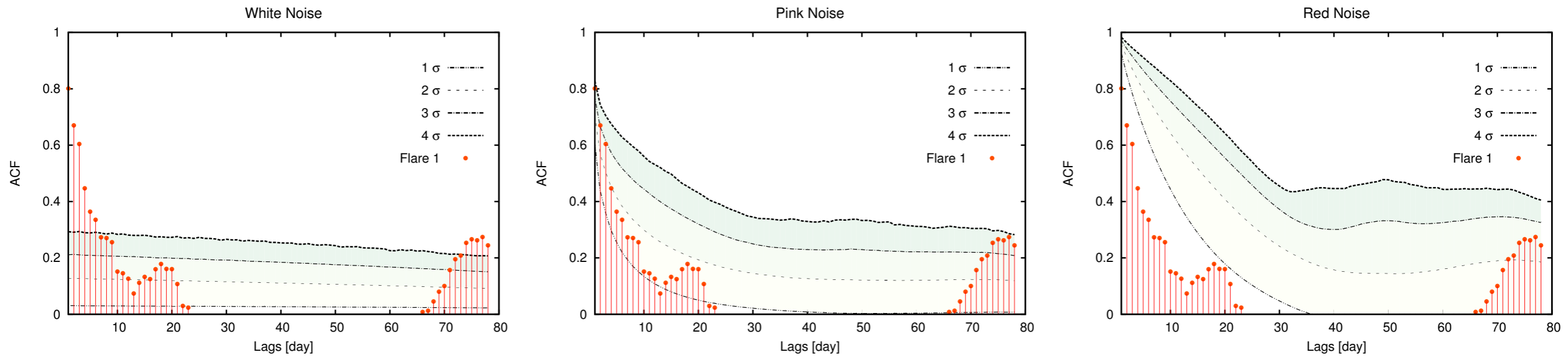
Step 3: The Second Power Spectrum

Windowing (Bingham window) and Zero Padding

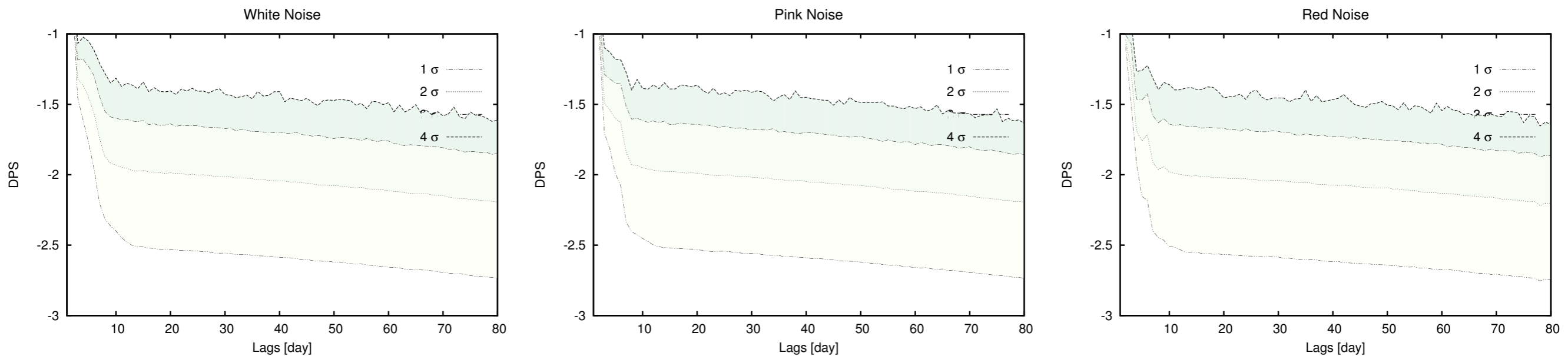


Monte Carlo Simulations - Significance Level

Autocorrelation Function

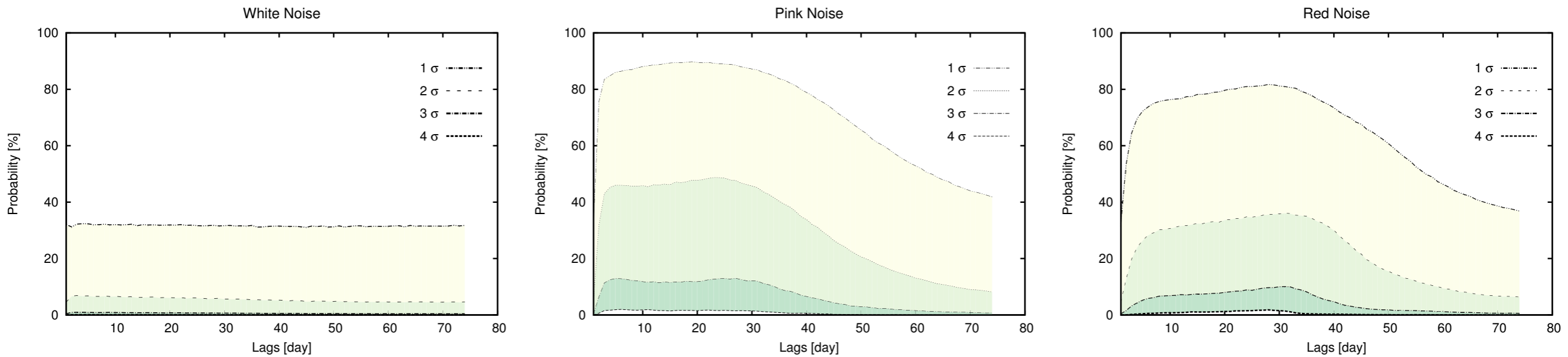


Double Power Spectrum

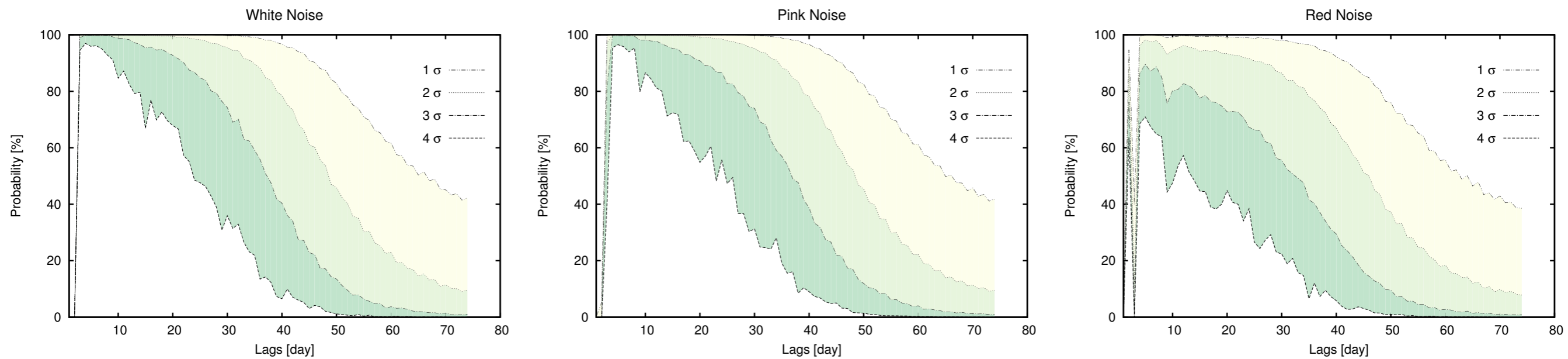


Detectability of the Time Delay

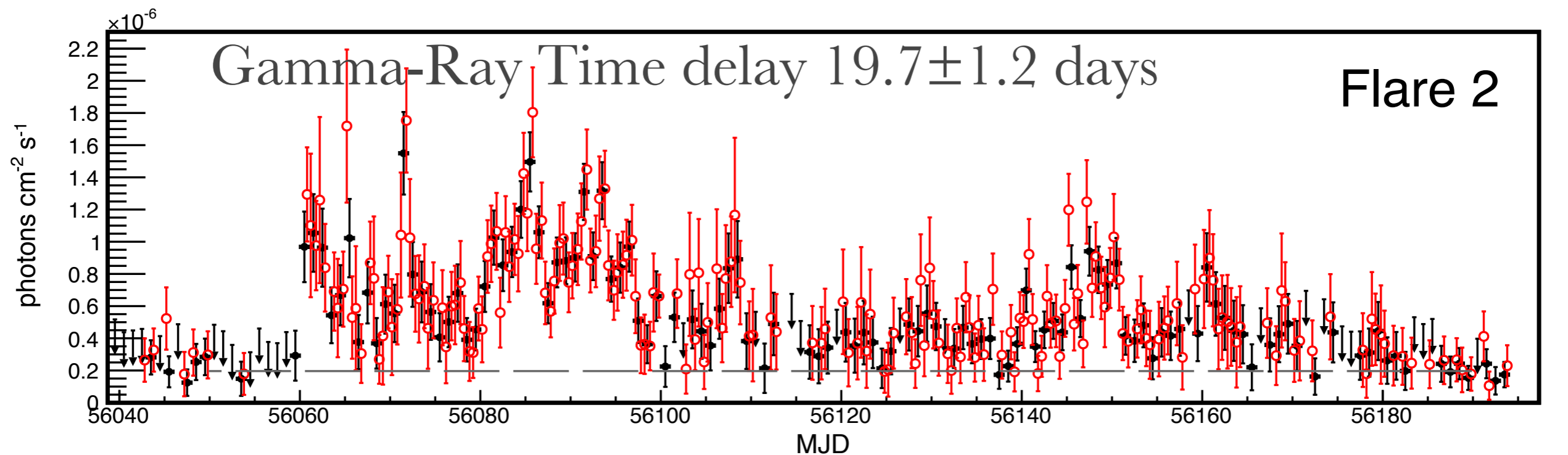
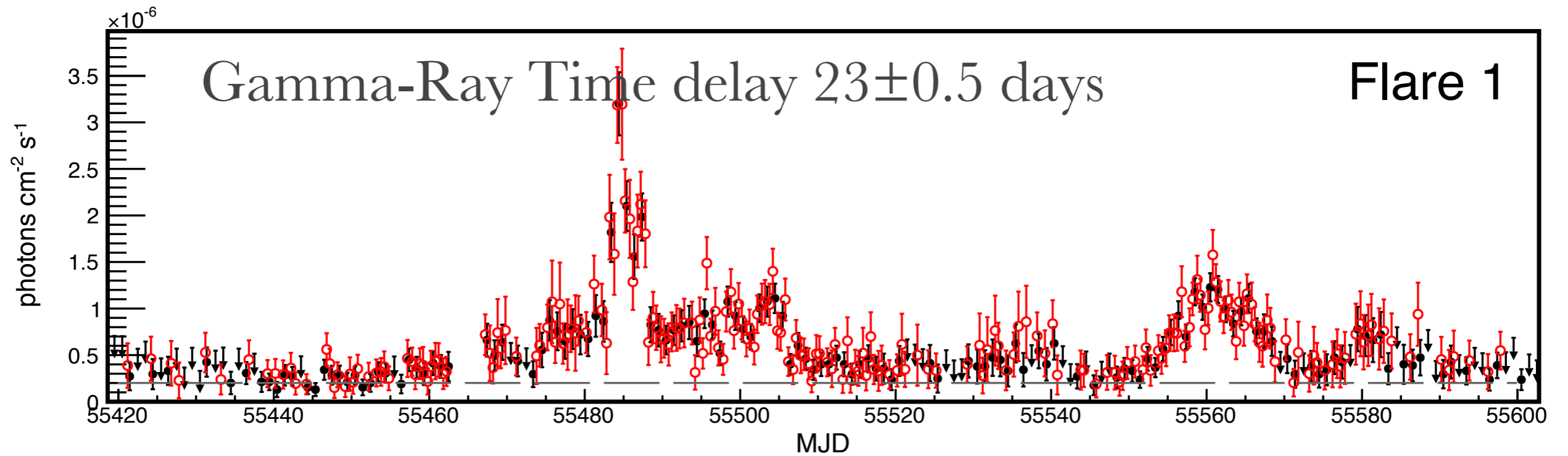
Autocorrelation Function



Double Power Spectrum

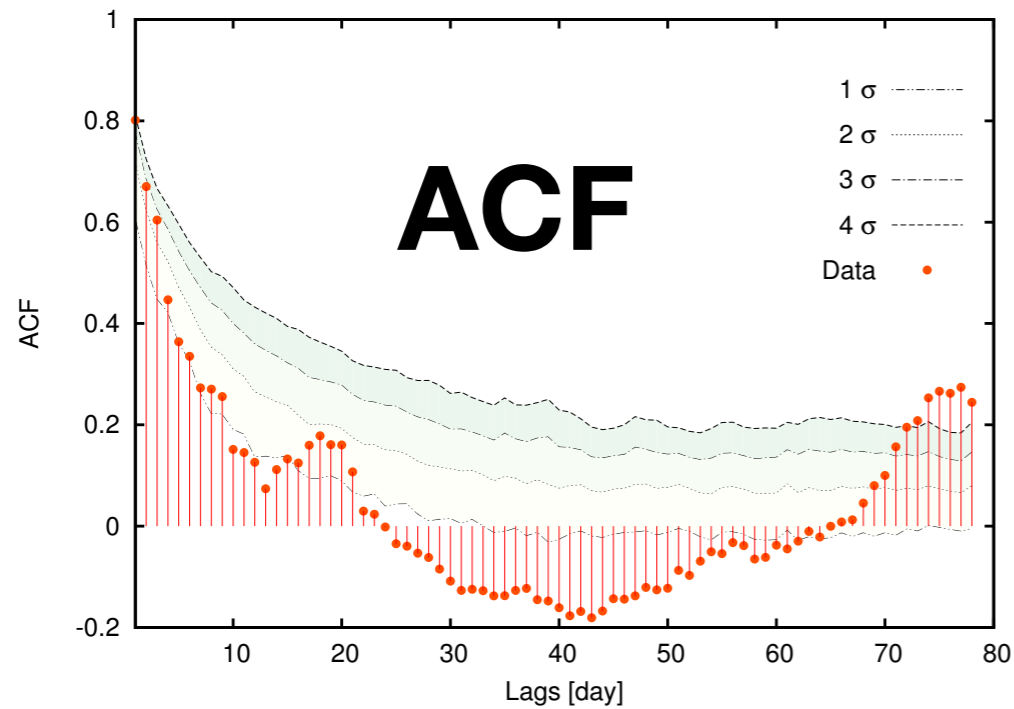


Gamma-ray Flare 1 and 2: Light Curves

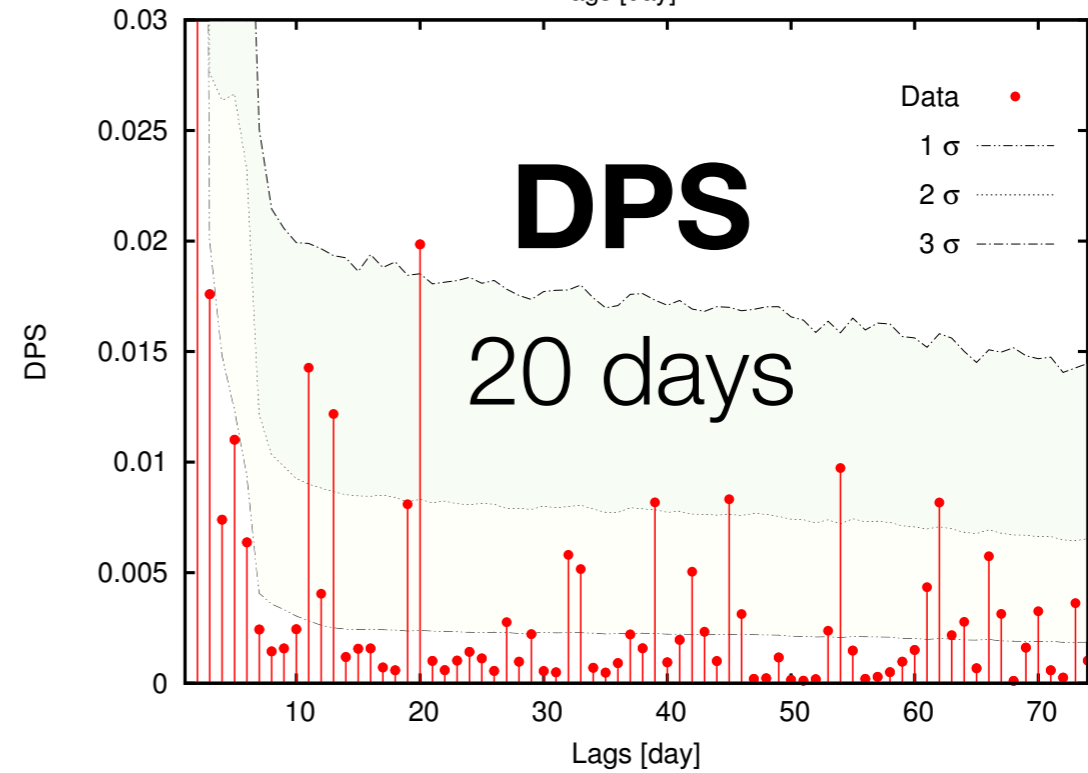
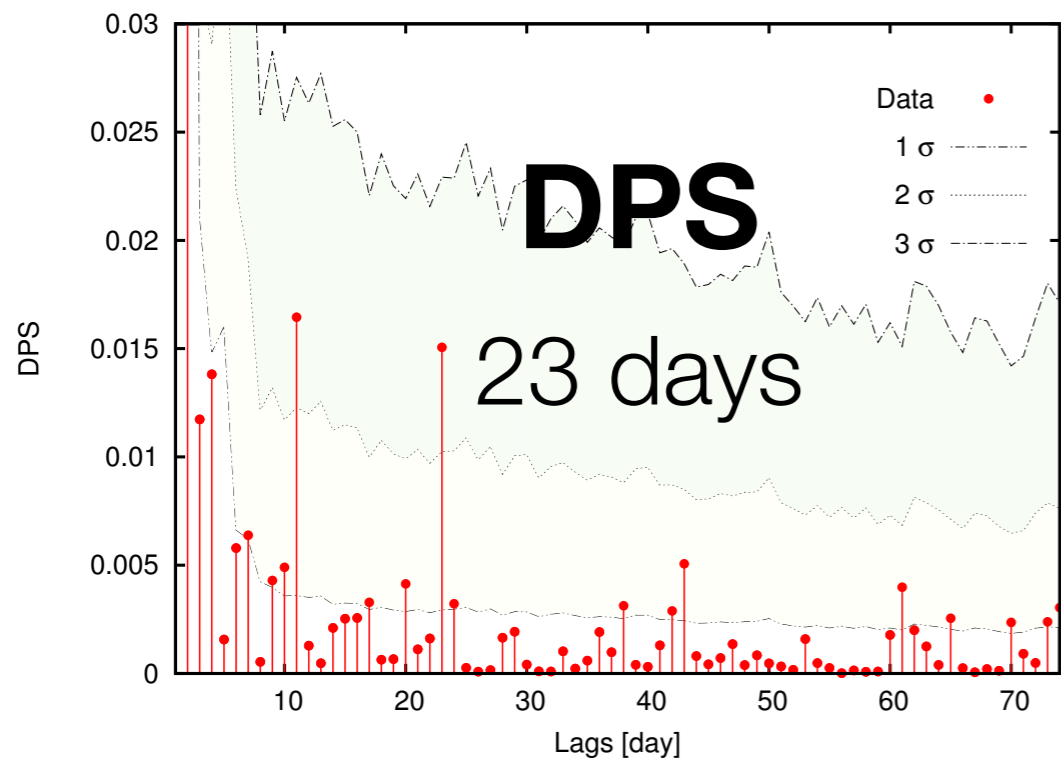
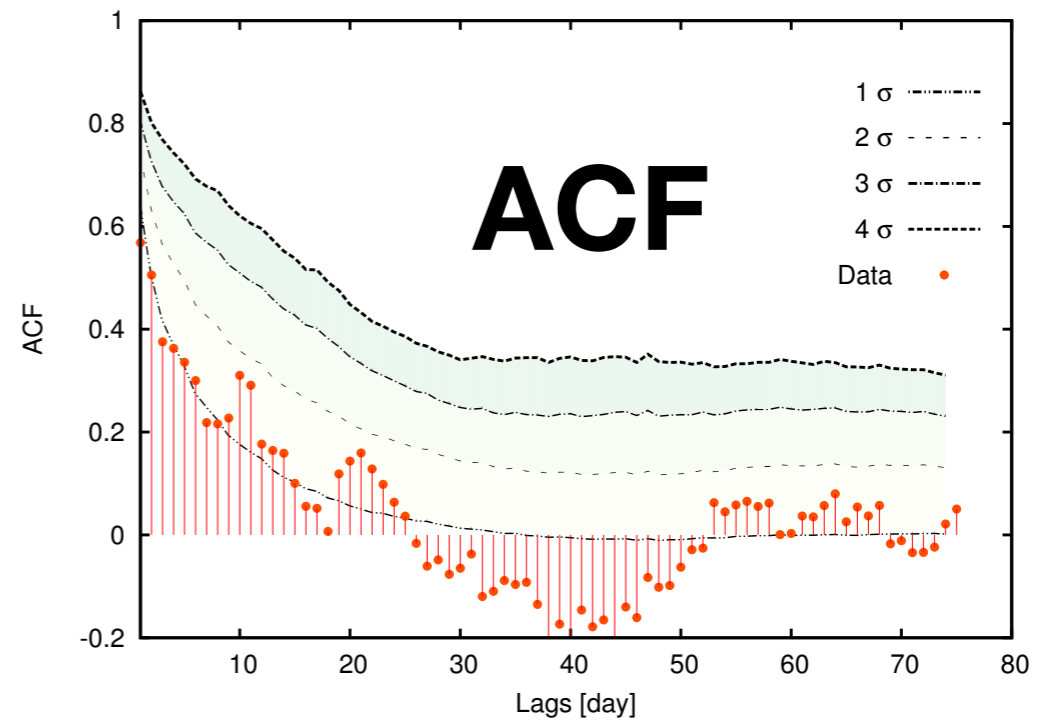


Gamma-ray Flare 1 and 2: Time Delays

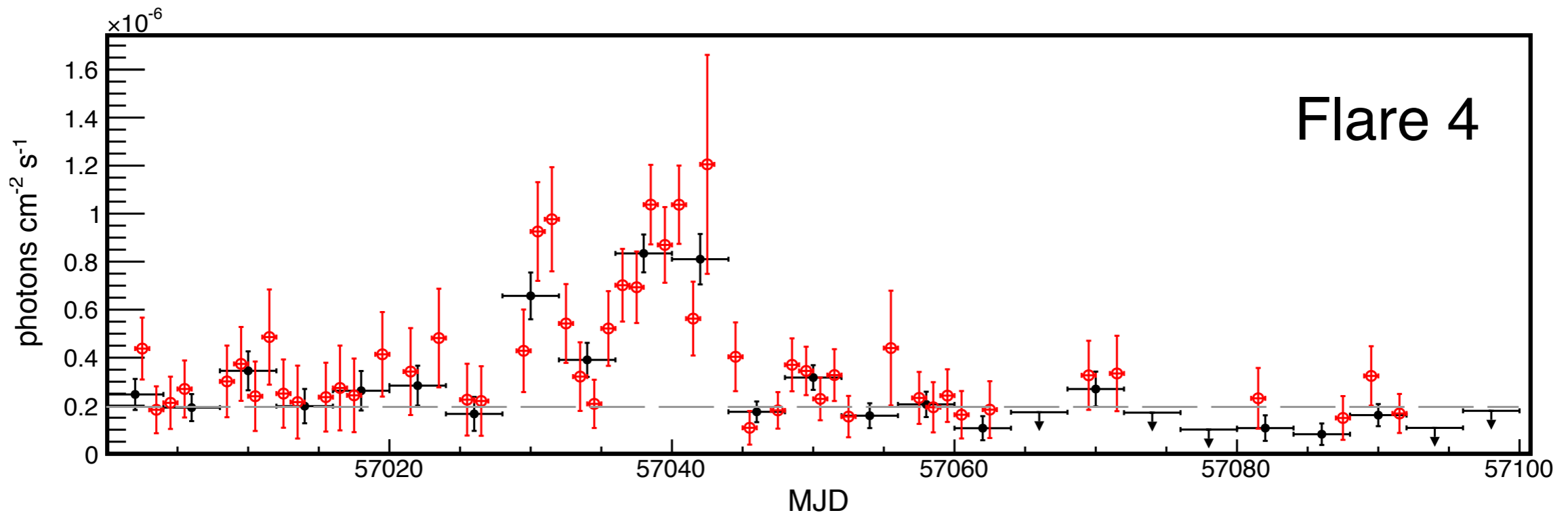
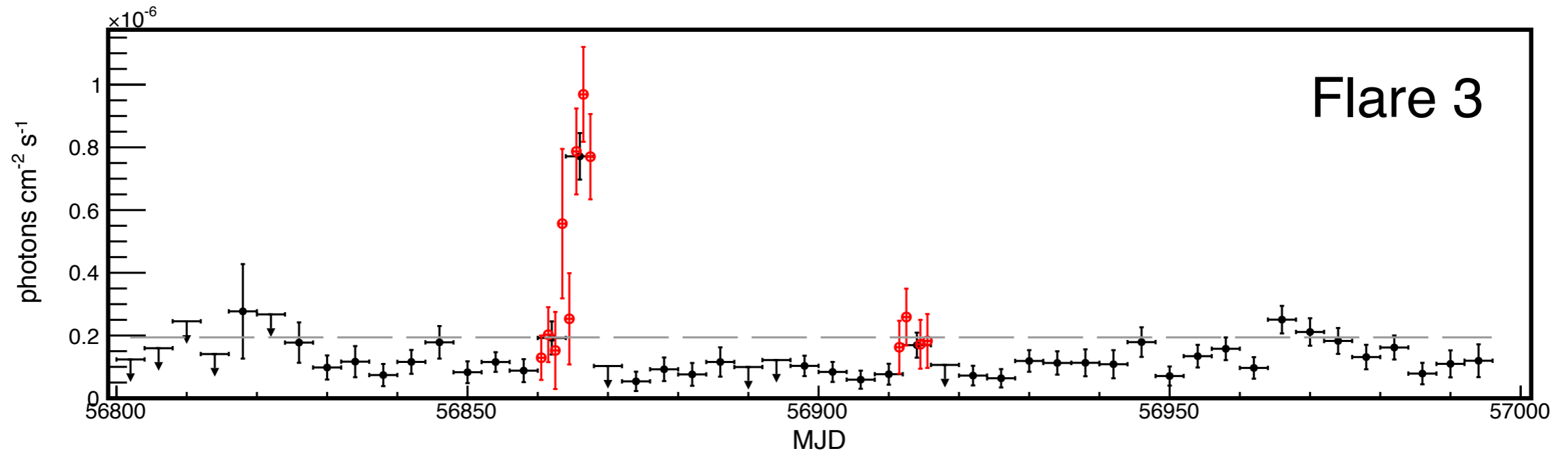
Flare 1



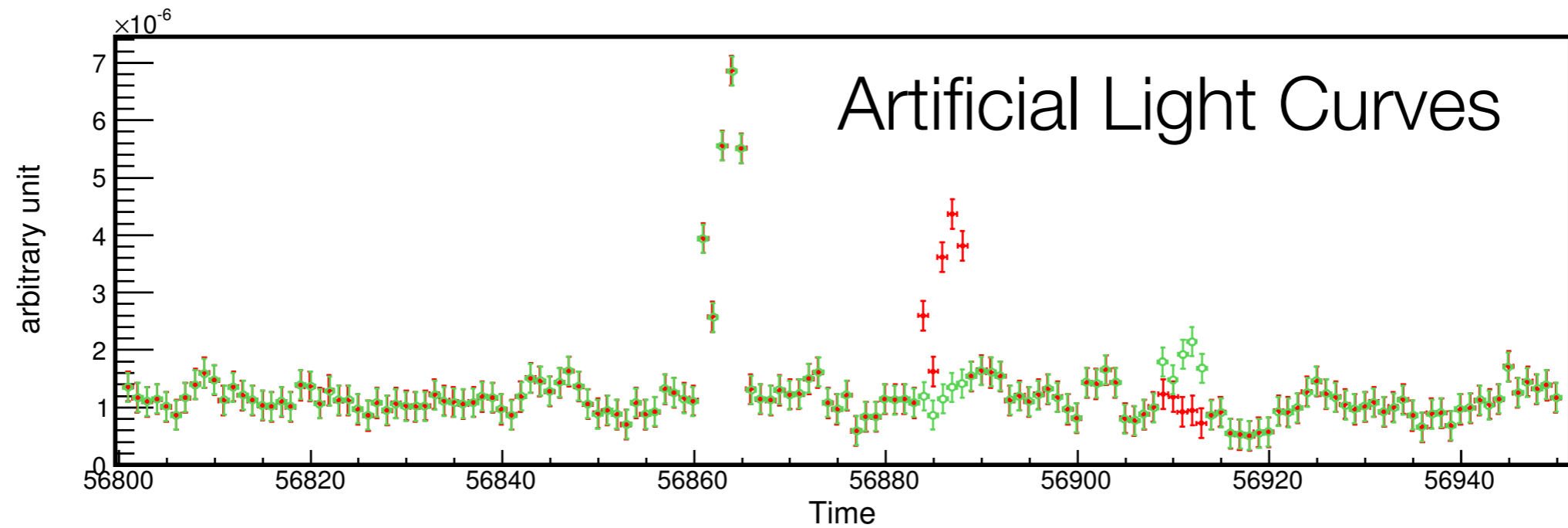
Flare 2



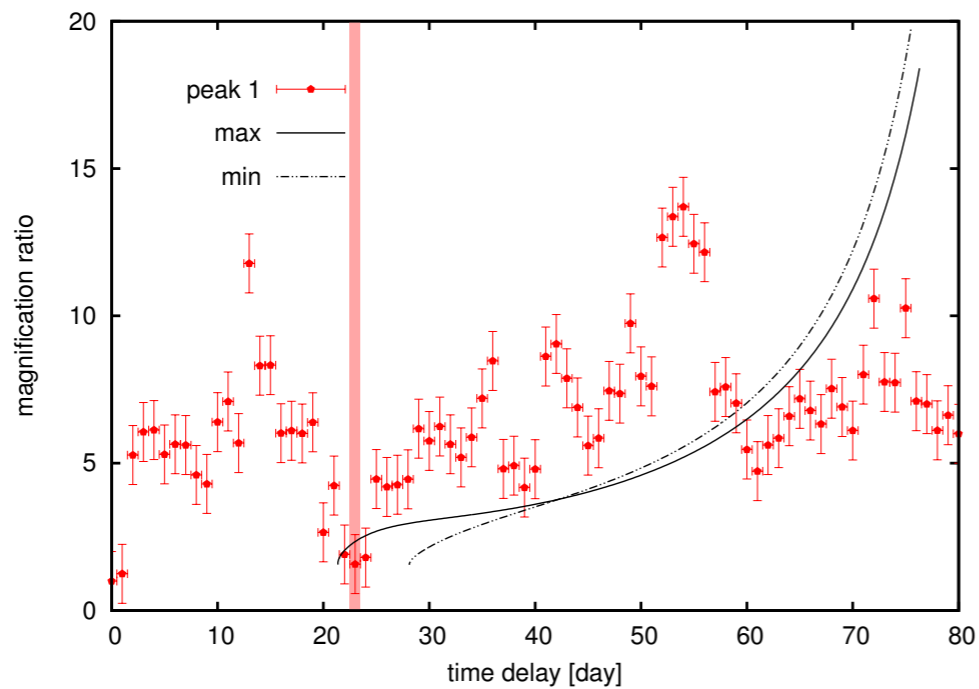
Gamma-Ray Flare 3 & Flare 4



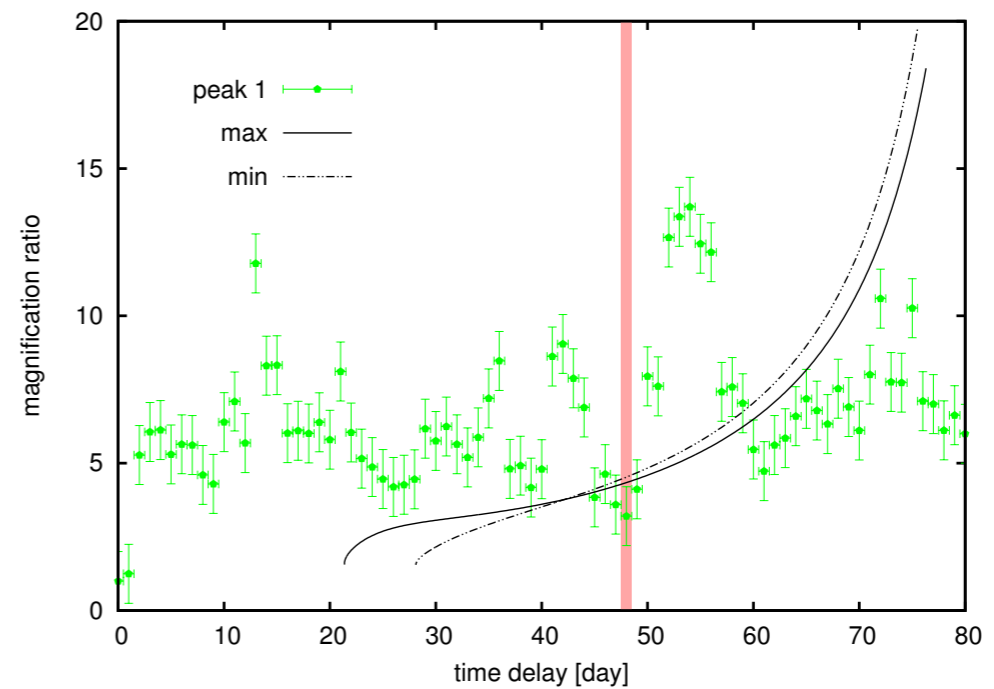
Maximum Peak Method - Monte Carlo



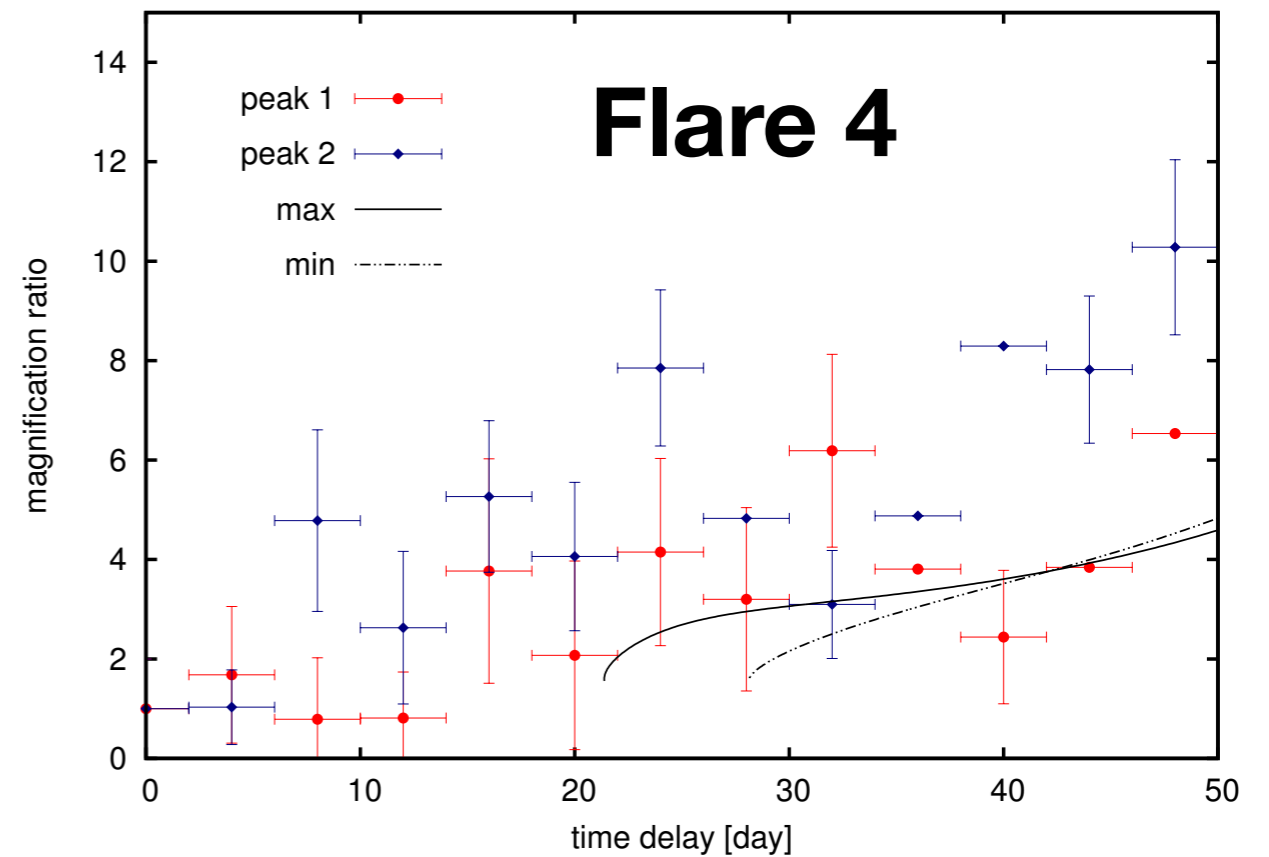
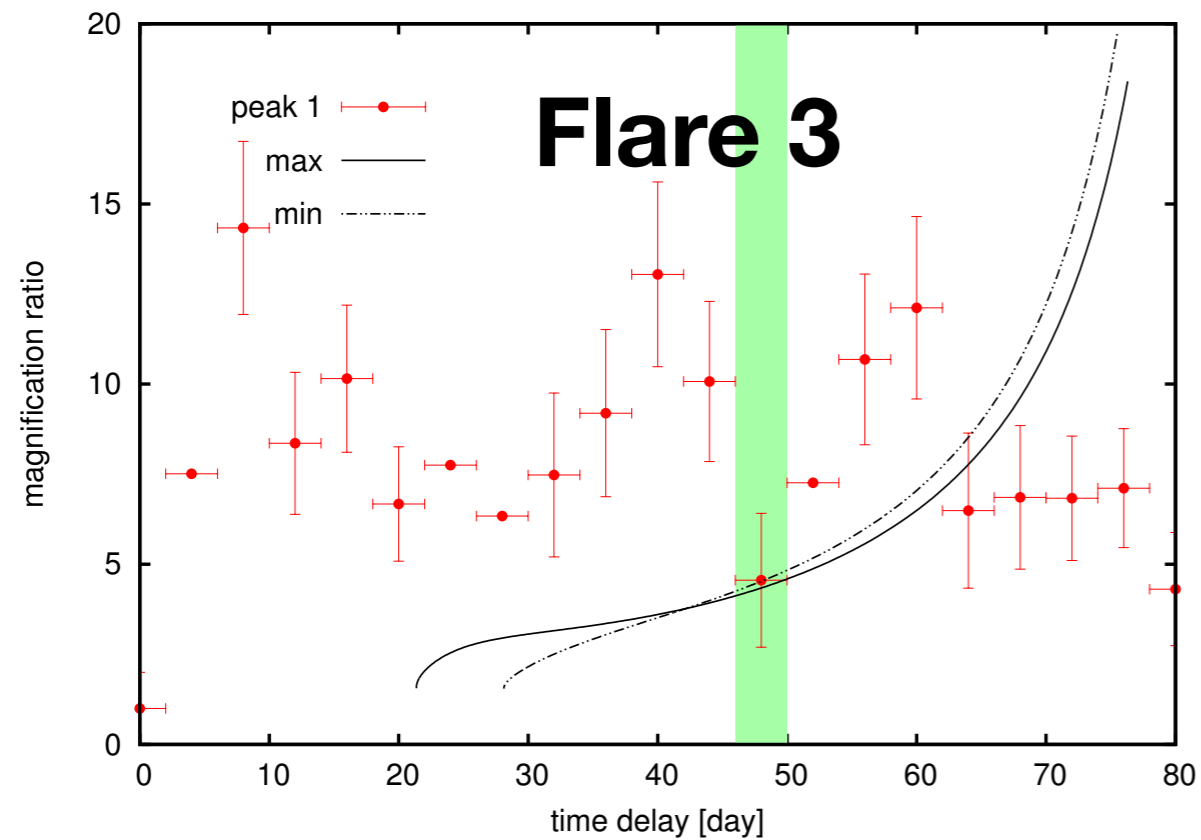
Time Delay ~ 24 days



Time Delay ~ 48 days

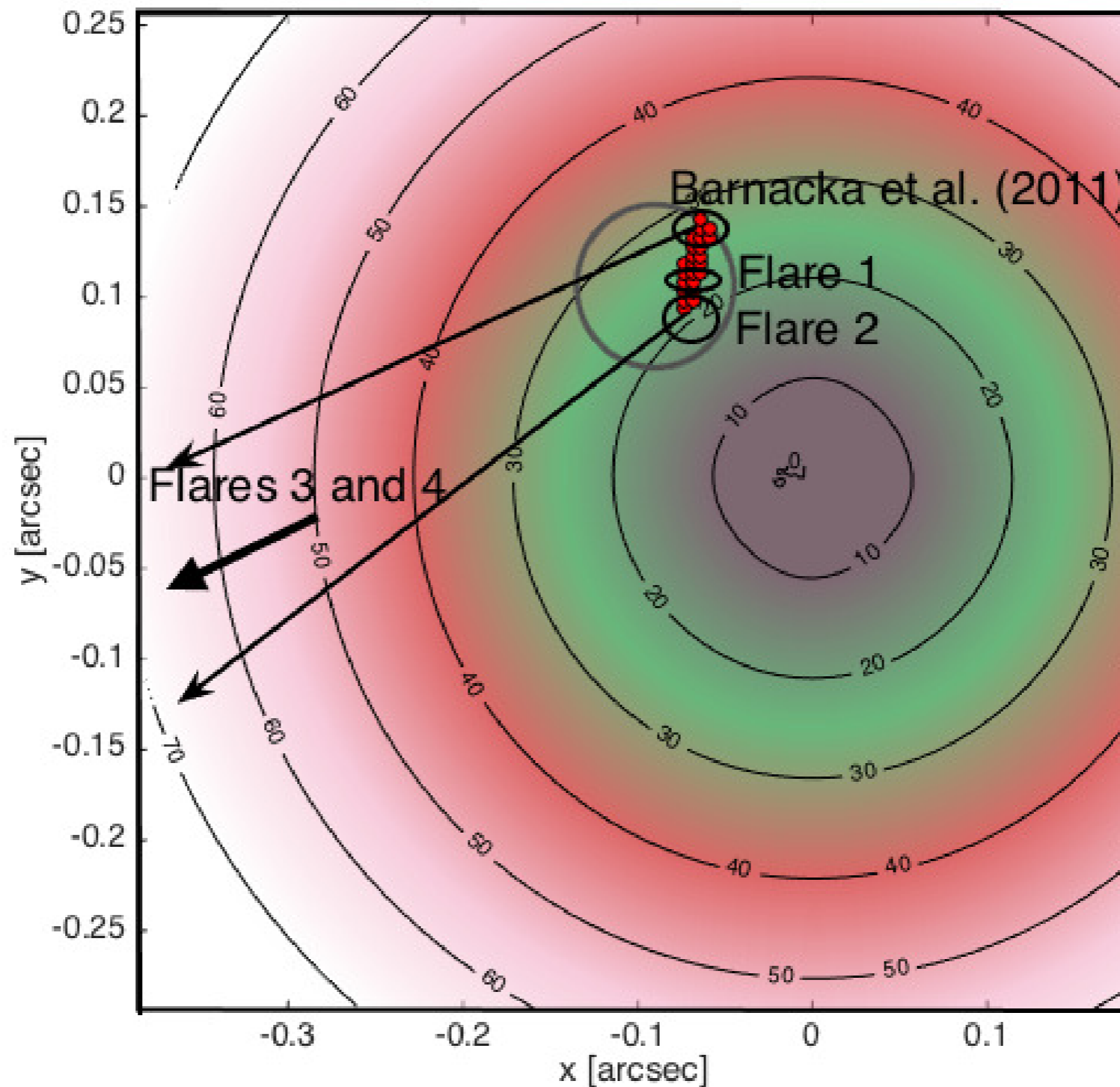


Maximum Peak Method - Data



Time Delay \geq 50 days

Spatial Origin of Gamma-ray Flares



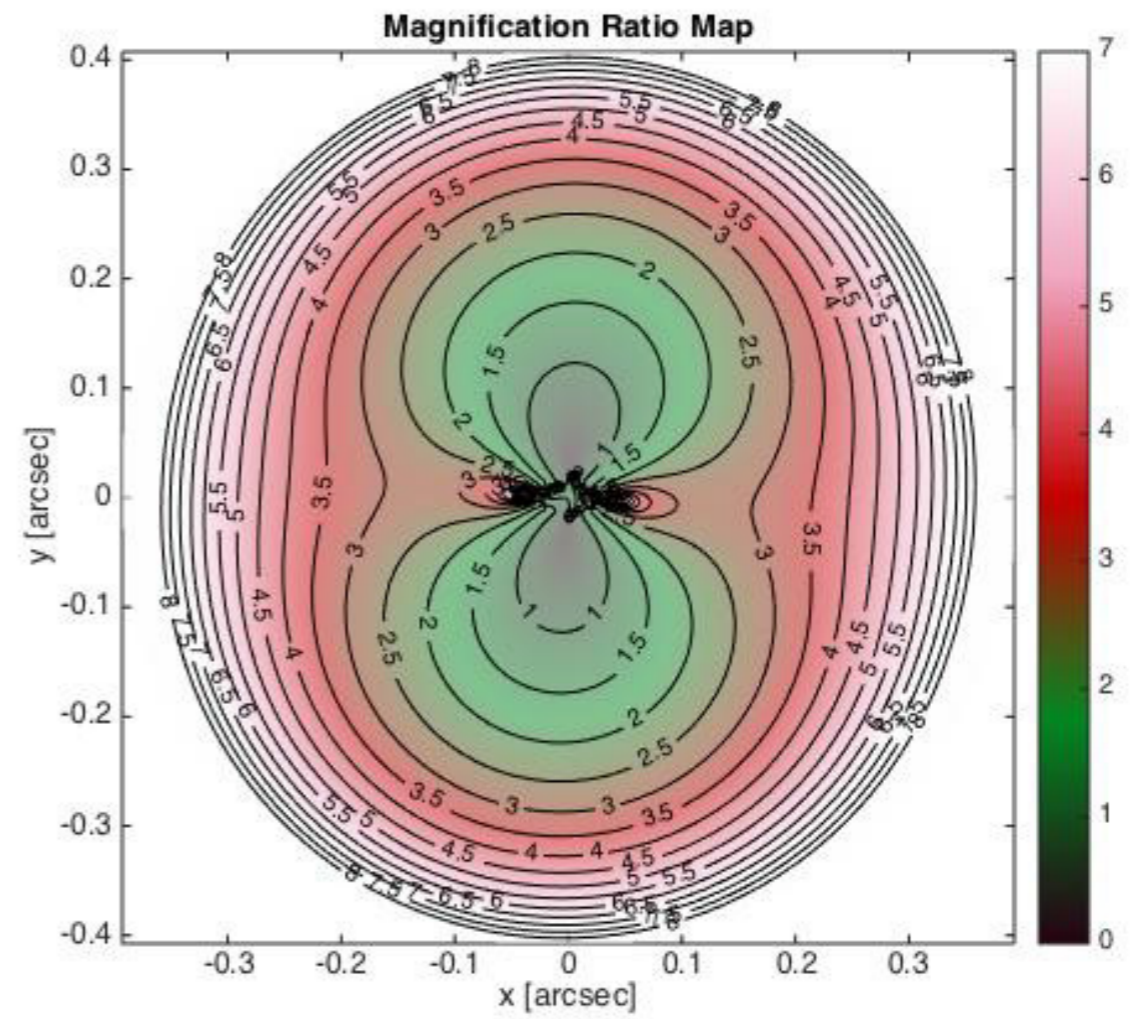
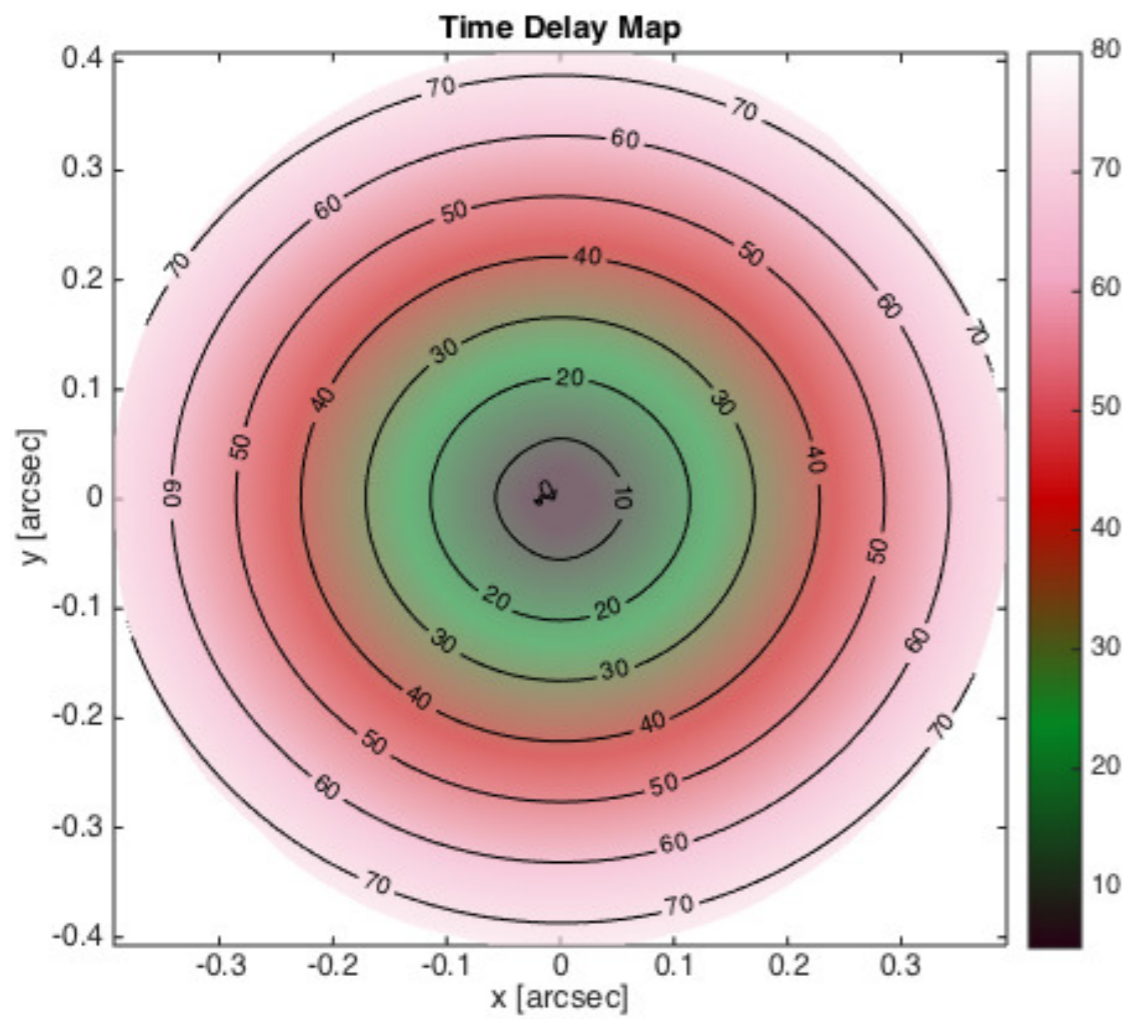
Barnacka, A., et al. (April, 2015: [arXiv:1504.05210](https://arxiv.org/abs/1504.05210))

Summary

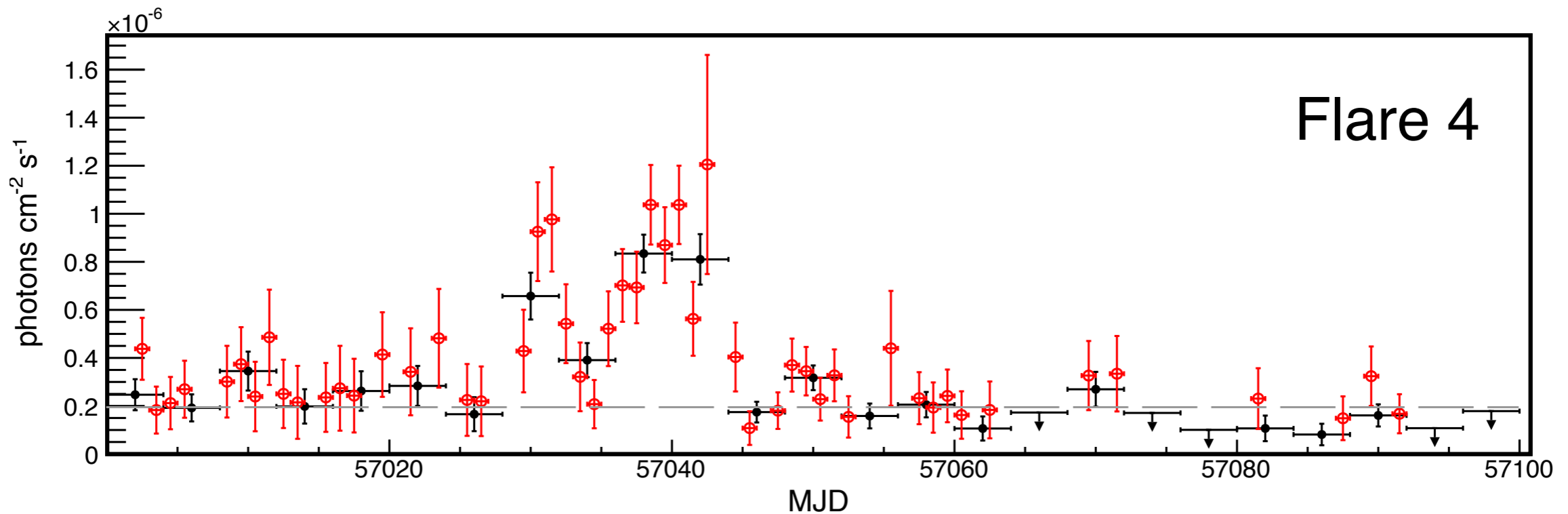
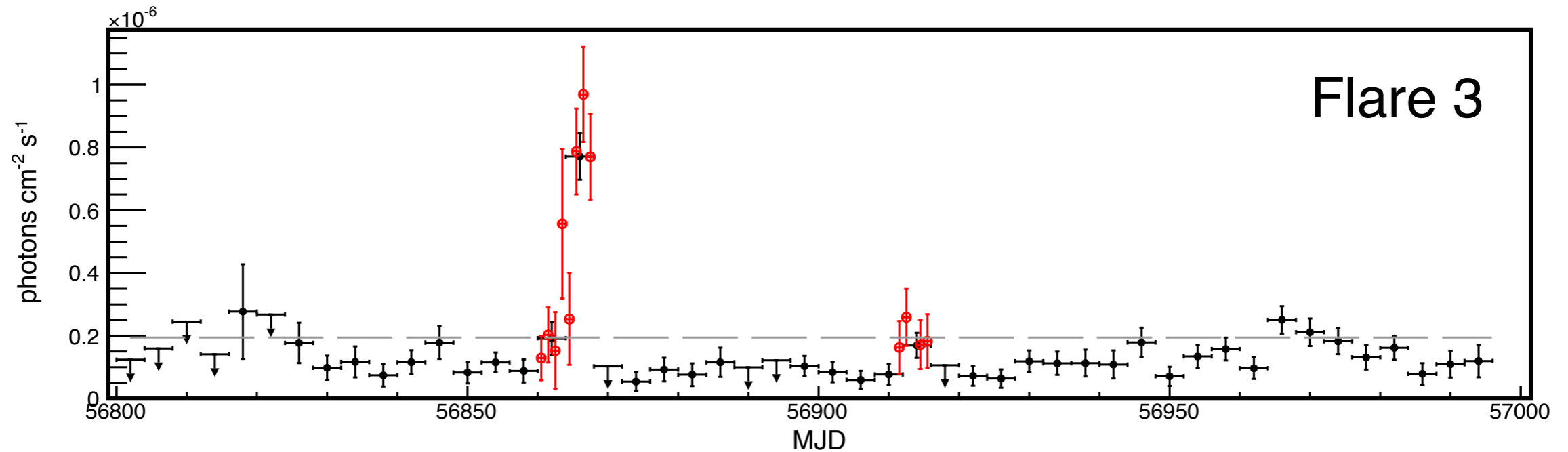
- **Strong Lensing:**
 - **Powerful Tool to Resolve High Energy Universe**
 - **Effective Spatial Resolution $\sim 0.02''$ - improvement $\times 10,000$**
- 

Backup Slides

Lensing Maps

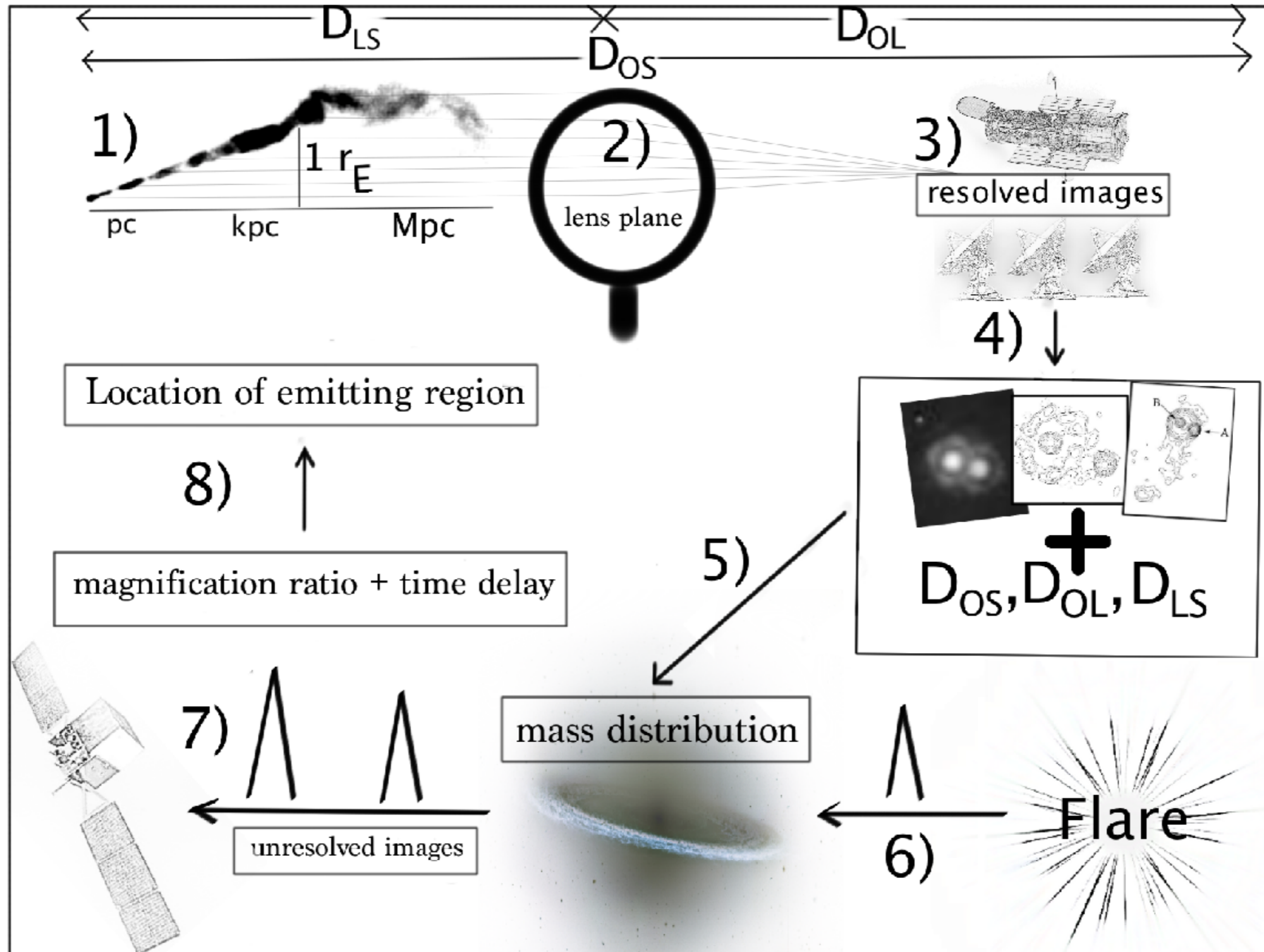


Gamma-ray Flare 3 and 4: Time Delays

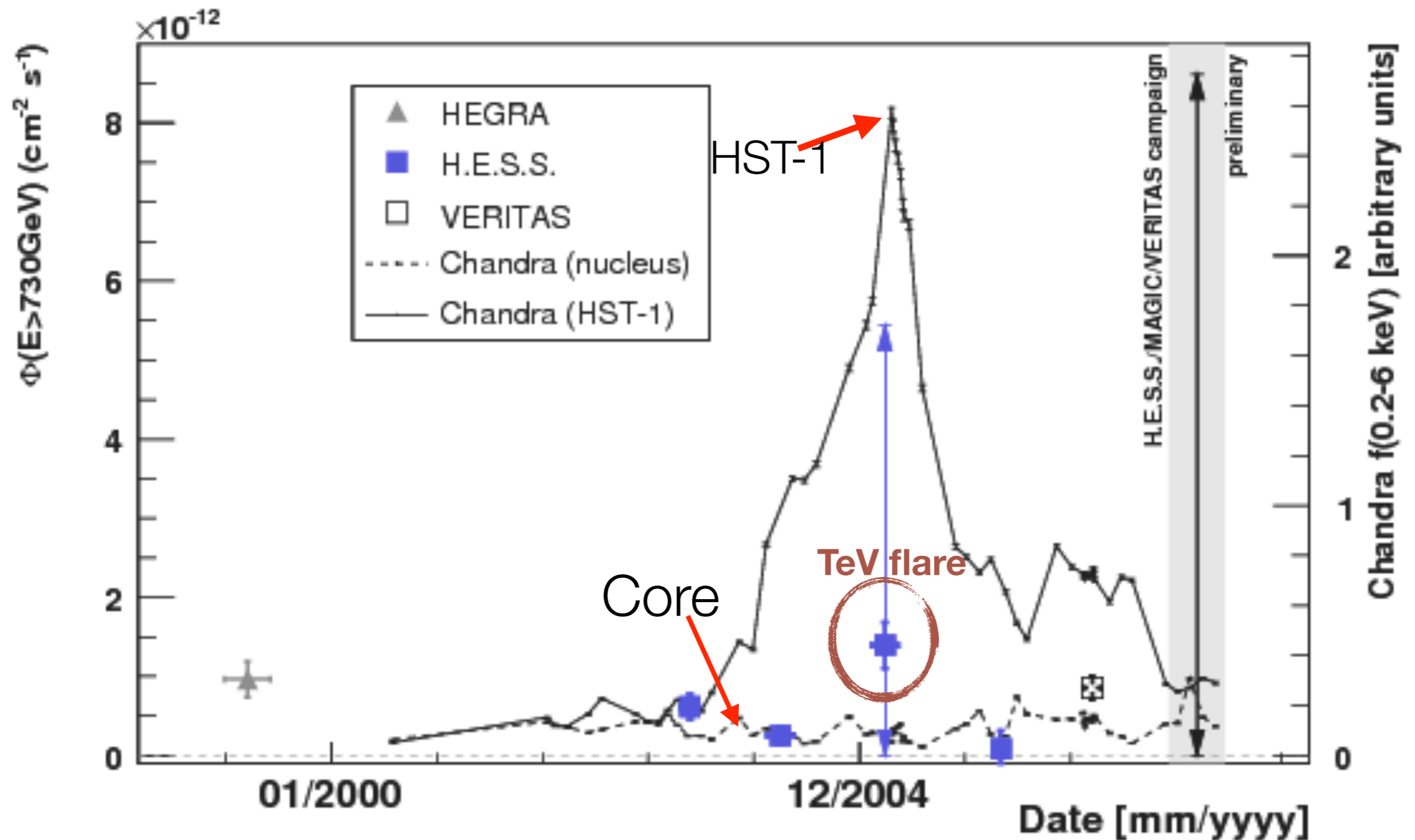


Gamma-Ray Time delay > 50 days

Application of strong lensing

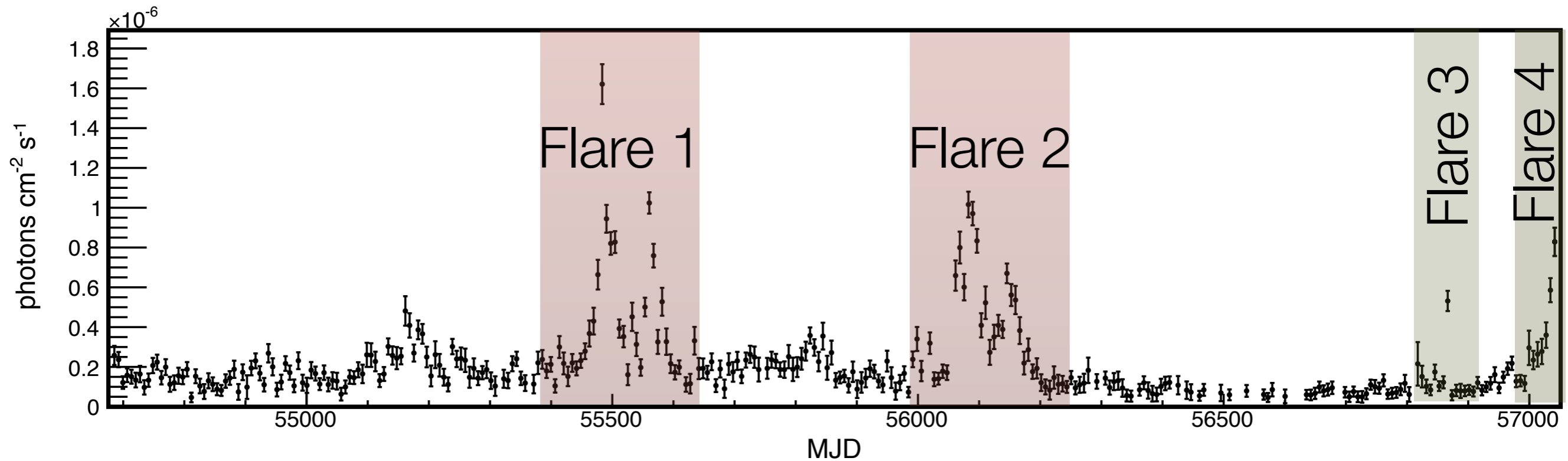


Spatial Origin of Gamma-Ray Flares



Credit: MAGIC and VERTIAS and H.E.S.S. Collaborations (2009)

Gamma-ray Flares: Time Delays

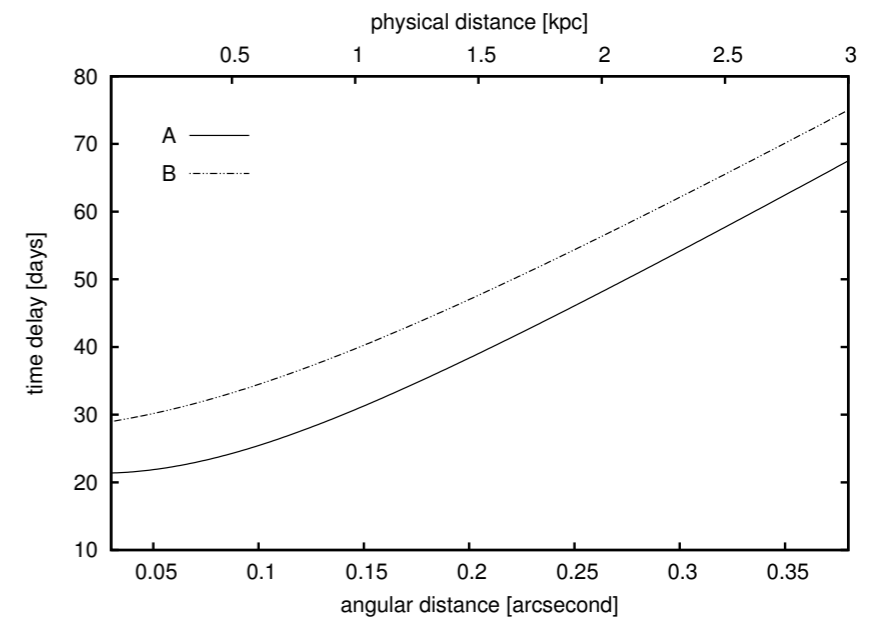
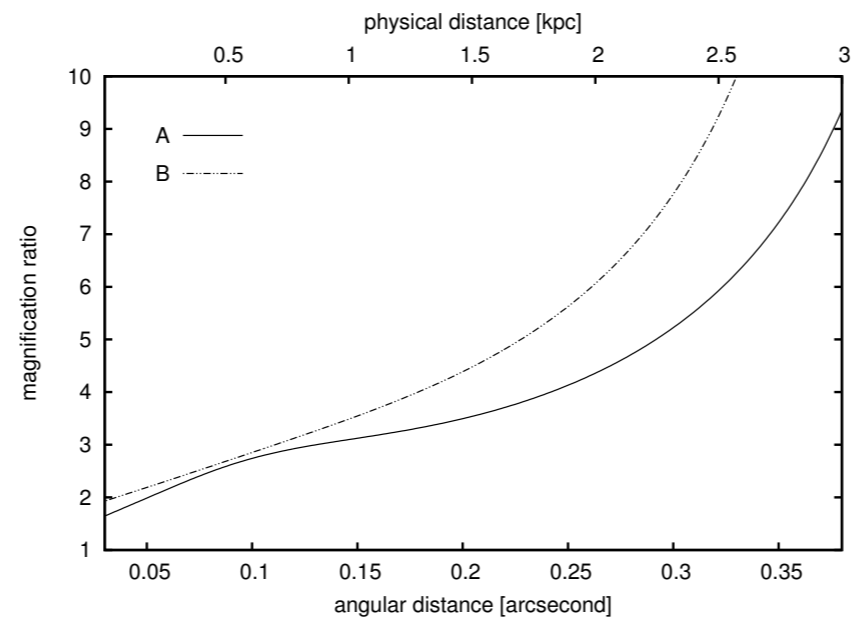
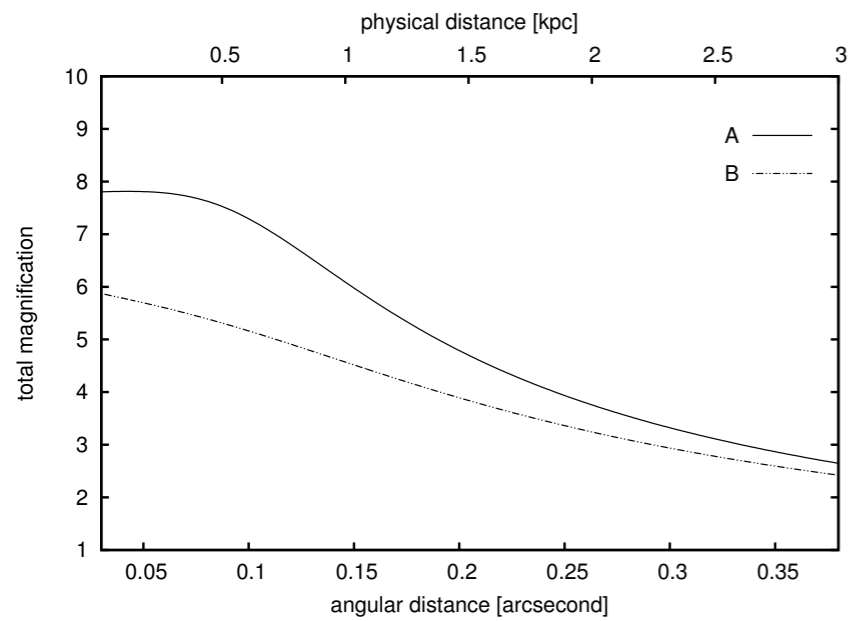


23 ± 0.5 days

19 ± 1.2 days

> 50 days

Lensing Parameters Along the Jet



Position of the Core

