

Measuring Black Hole Spin

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Astrostatistics Forum
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Overview

- ✧ Objects: **Stellar-mass BHs in X-ray binaries**
- ✧ Method: **Spin via fitting the X-ray continuum**
- Statistical Questions:
(digression : MCMC in XSPEC)

BH -XRB Picture

- ✧ BH

 - ✧ 5-15 M_{\odot}

- ✧ Companion Star

 - ✧ Tidally distorted

- ✧ Accretion Disk

 - ✧ Most efficient engine in the universe!

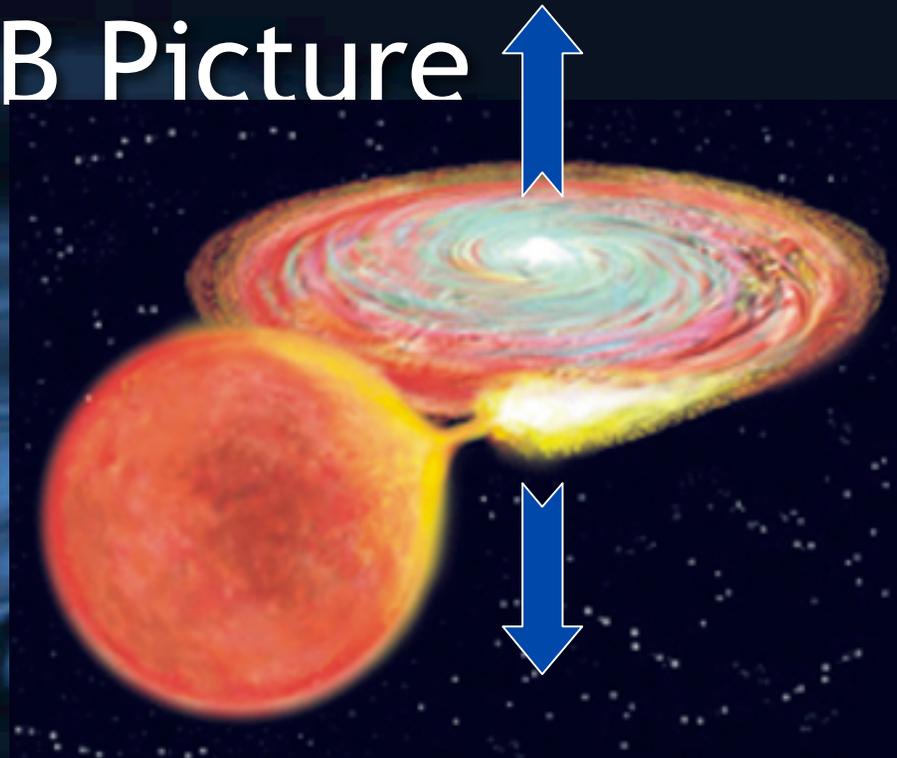
 - ✧ 5%-40% compared to 0.7%

- ✧ Corona

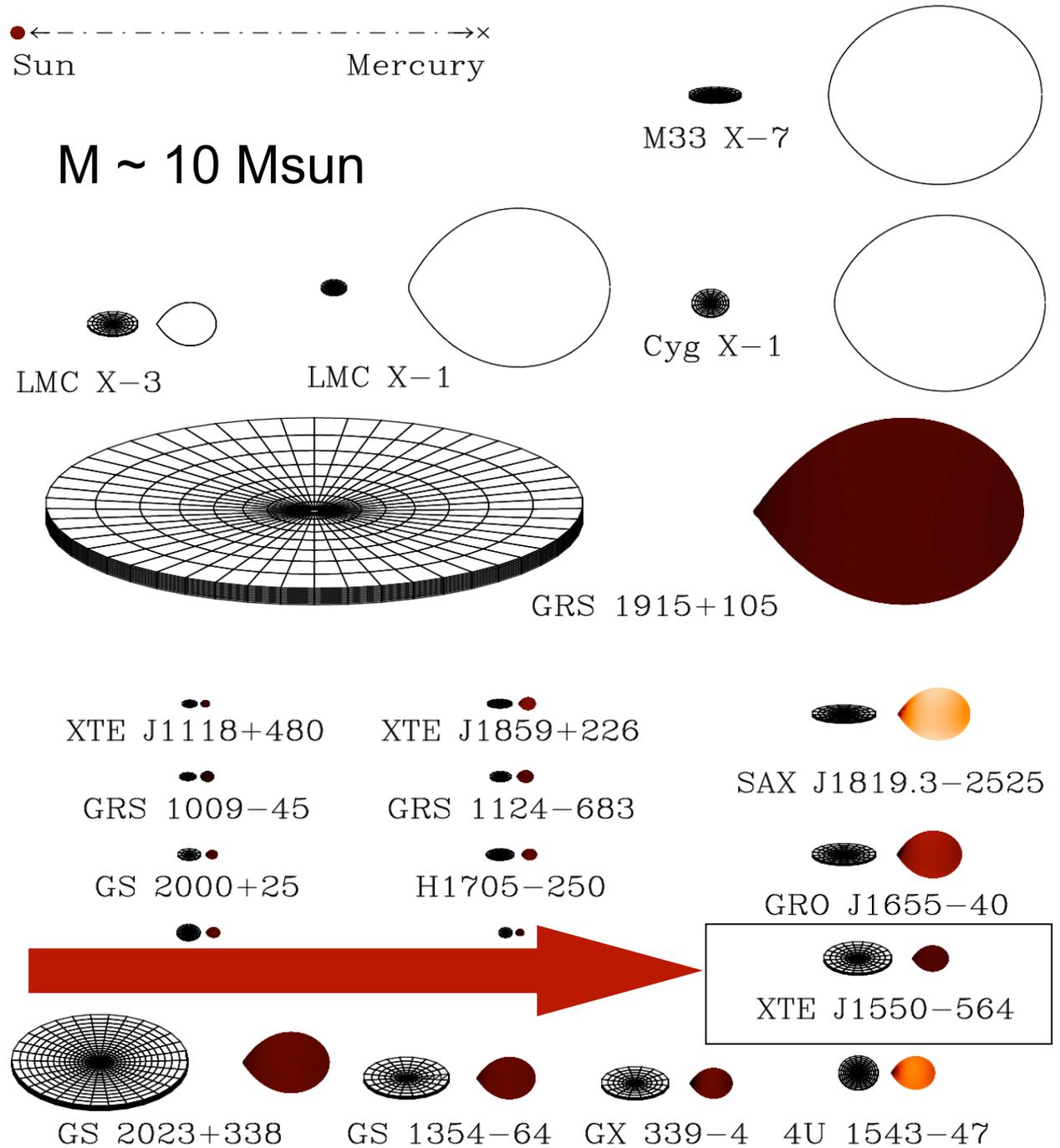
 - ✧ Hot ions in a cloud, surrounding the disk

- ✧ (Jets - Microquasars)

 - ✧ Beamed highly relativistic ejections (along the BH spin axis)



Number of BH binaries known = 21



Courtesy J. Orosz

Measuring Properties

✧ Optical Spectra

- ✧ Radial Velocities

- ✧ Mass Function

- ✧ Spectral Type of Companion Star \Leftrightarrow Temp

✧ Imaging

- ✧ Ellipsoidal Light Curves

- ✧ Genetic Fitting

 - ✧ (ELC = pikaia + black sheep)

✧ X-ray Spectra

- ✧ Accretion Disk Physics

Black Holes are Extremely Simple

✧ **Mass: M**

✧ **Spin: $J = a_* GM^2/c$ ($0 < a_* < 1$)**

✧ **(Electric Charge)**

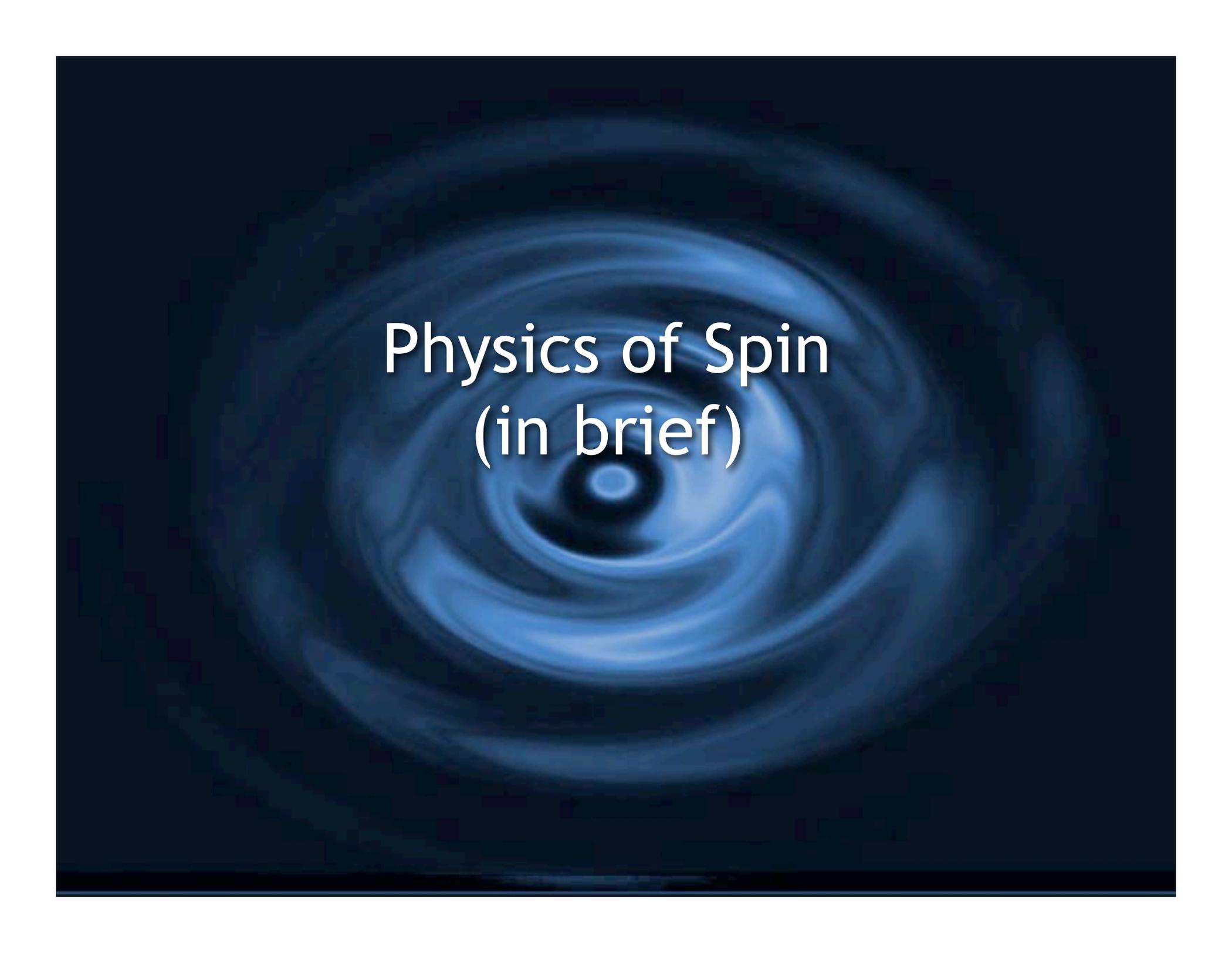
✧ Astrophysically, has no importance

21 BH masses have been measured

Obvious next frontier: Measure **BH spin a_***

Uses of Spin Data

- ✧ Test Jet Models
- ✧ Validate core-collapse GRB models
 - ✧ Collapsar: Enough J to form disk?
- ✧ Inform models of GR waveforms
 - ✧ Shafee et al. motivated first waveform work to include spin
- ✧ Test evolutionary model of binary black-hole formation
 - ✧ Were GRS 1915+105, GRO J1655-40?, etc. GRB sources?
- ✧ Understand disk QPOs
 - ✧ Both HF/LF in several systems, 2:1
- ✧ Modeling the growth of SMBH



Physics of Spin
(in brief)

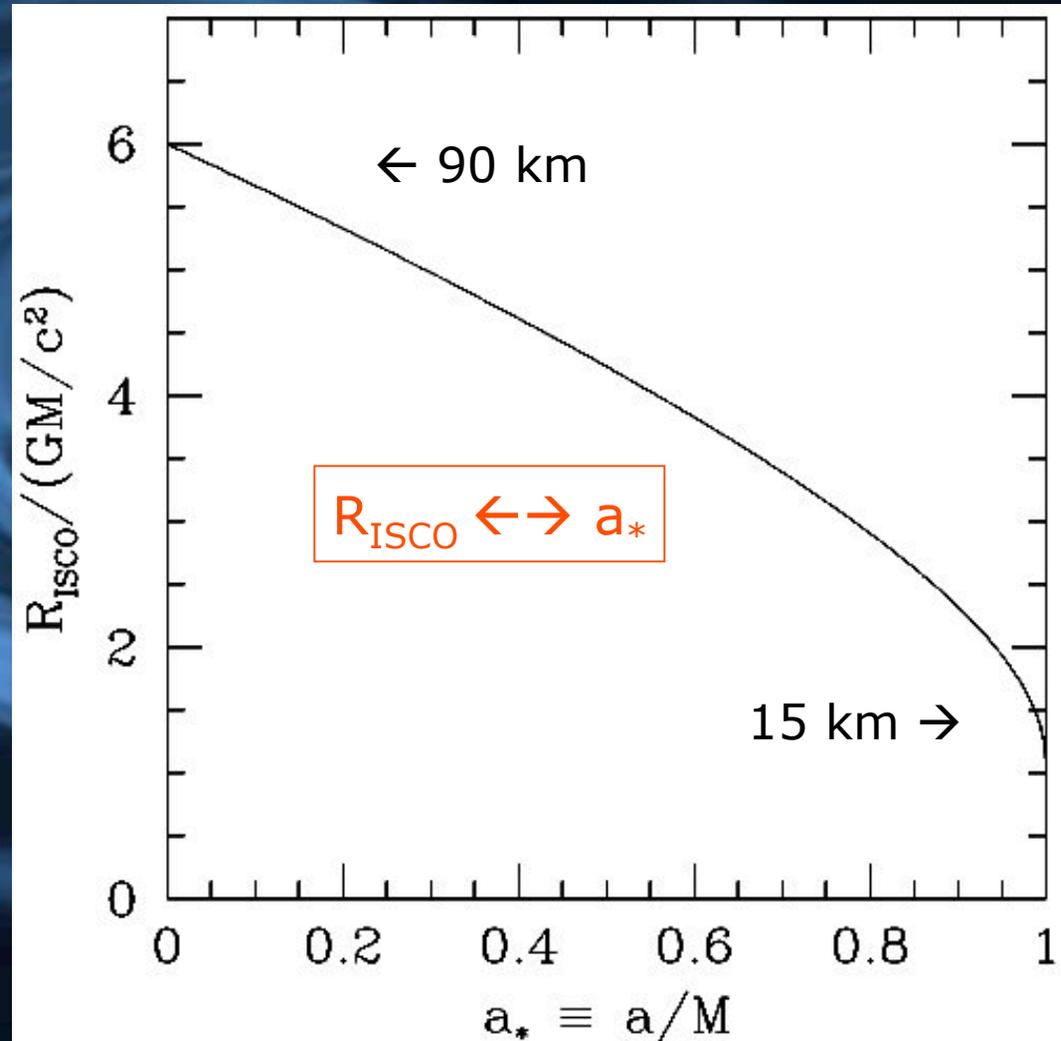
Two Foundations

- ✧ 1. ISCO (Innermost Stable Circular Orbit)
 - ✧ From General Relativity
- ✧ 2. Thermal Dominant State

First Foundation

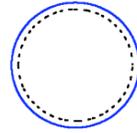
Innermost Stable Circular Orbit (ISCO)

- A disk terminates at R_{ISCO} and gas falls freely onto the BH inside this radius.
- Thus, disk emission has a “hole” of radius R_{ISCO} at center.
- If we measure the size of the hole, we will obtain a_*



R_{ISCO} : Extreme-Kerr vs. Schwarzschild

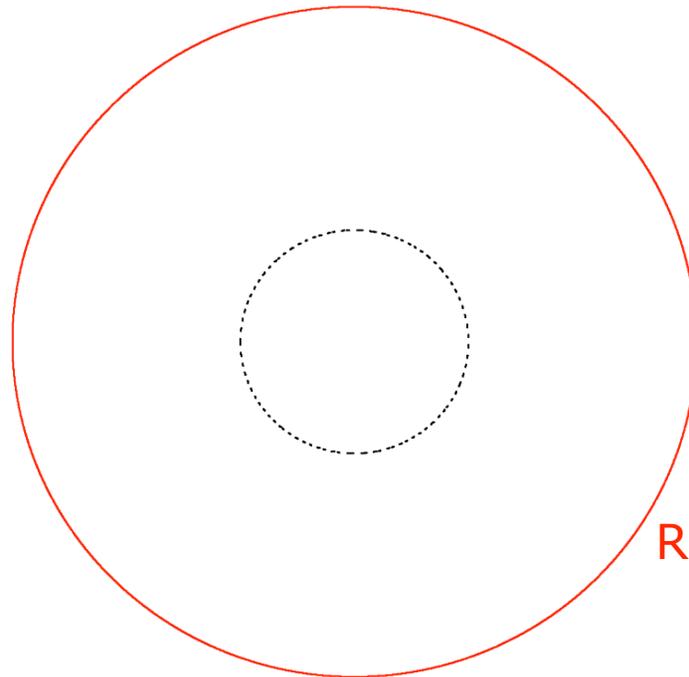
$$a_* = 1$$



$T \sim 2 \text{ keV}$
42%

$$R_{\text{ISCO}} = 15 \text{ km}$$

$$a_* = 0$$



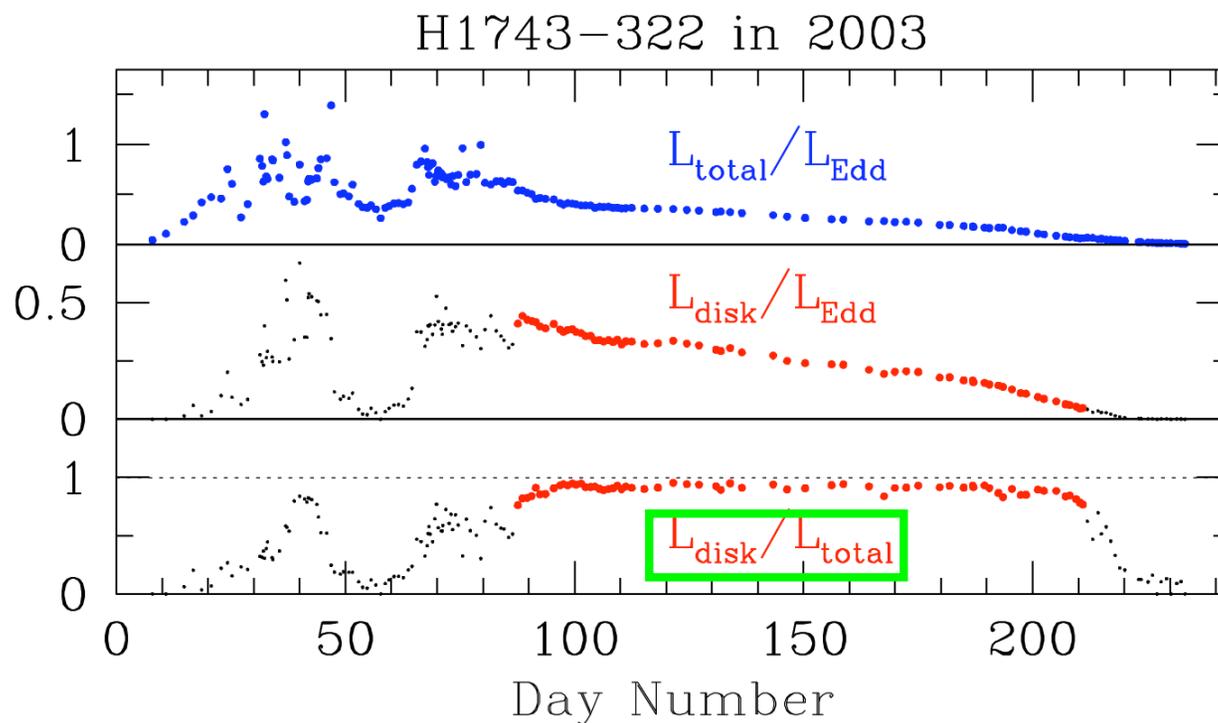
$T \sim 1 \text{ keV}$
6%

$$R_{\text{ISCO}} = 90 \text{ km}$$

Second Foundation

- ✧ The Thermal State :
- ✧ Thermal Disk Model
 - ✧ Describes a physical limit in which:
 - ✧ The accretion disk is thin ($H/R \ll 1$)
 - ✧ **The emission is dominated by a thermal component (set by a characteristic temperature)
 - ✧ (Shakura & Sunyaev alpha-disk prescription)

Second Foundation (cont.)

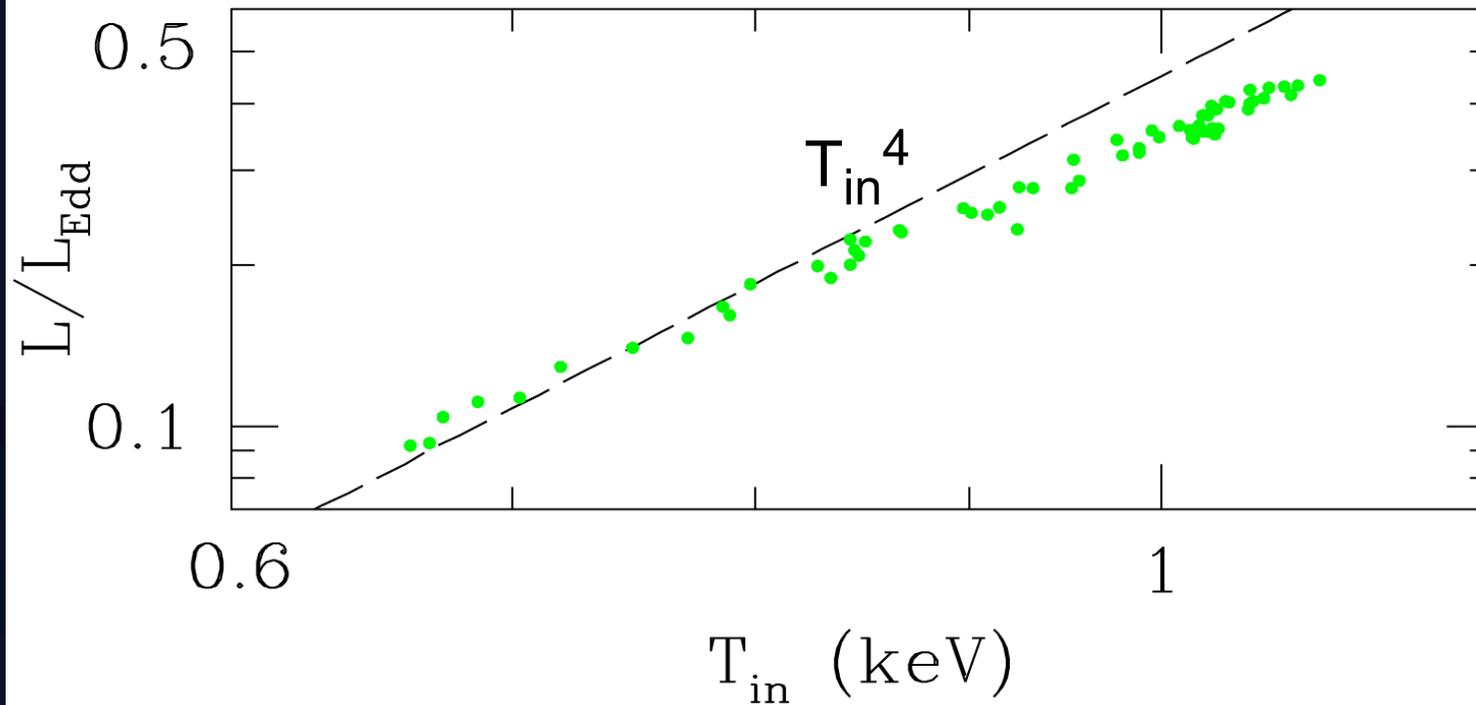


Thermal Dominant State

- $L_{\text{disk}} / L_{\text{total}} > 75\%$ (2-20 keV)
- No QPOs
- Power-law/Comptonization minimal

Remillard & McClintock 2006, ARAA, 44,49

Second Foundation (cont.)



Kubota et al. 2001
Kubota & Makishima 2004
Kubota & Done 2004
Gierlinski & Done 2004

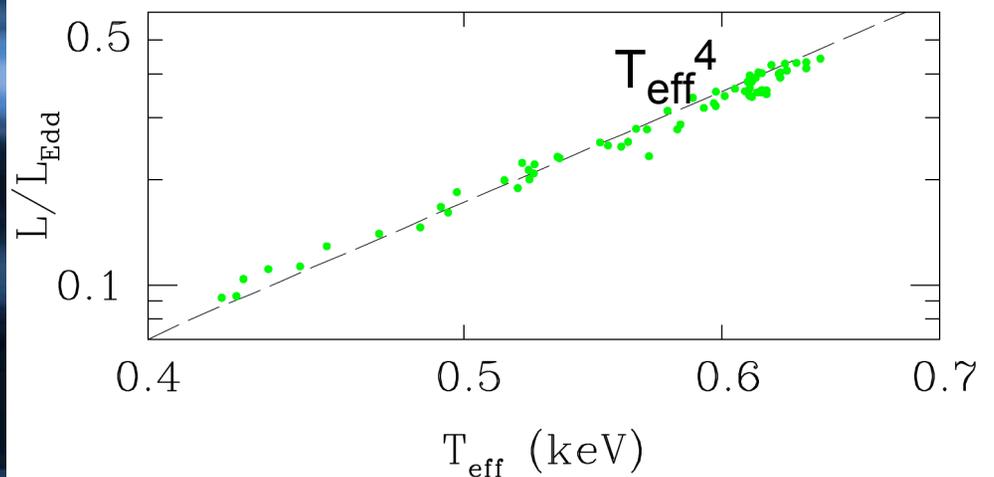
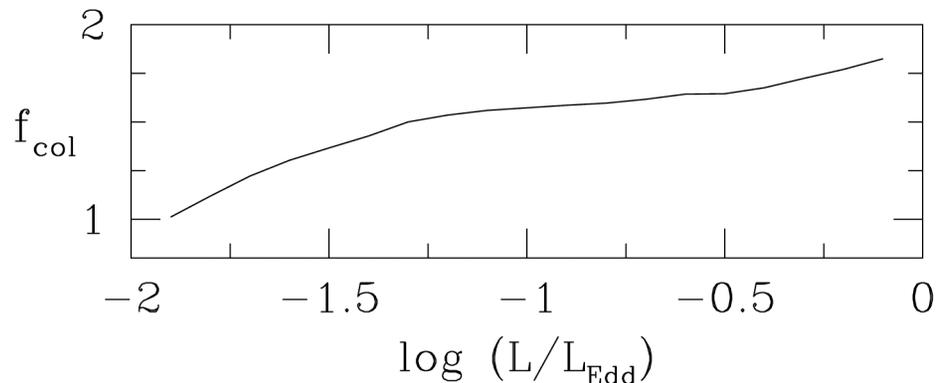
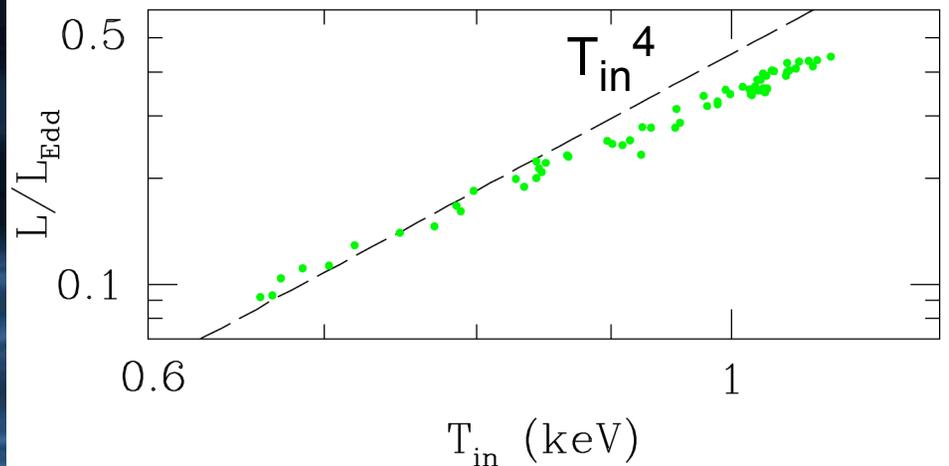
Second Foundation

Improvement from theory:

$$f_{\text{col}} = T_{\text{in}}/T_{\text{eff}}$$

Davis et al. 2005, 2006

Conclusion:
There exists a constant radius





Estimating Spin: Our approach

→ Fitting the X-ray continuum ←

Measuring the Radius of the Disk Inner Edge

- ✧ We want to measure the radius of the ‘hole’ in the disk emission
- ✧ Same principle as measuring stellar radius
- ✧ From F and T get angle of hole
- ✧ Knowing D and i
 R_{ISCO}
- ✧ From R_{ISCO} and M get a_*



Zhang et al. (1997) Gierlinski et al. 2001; Li et al. (2005);
Shafee et al. (2006); McClintock et al. (2006); Davis et al. (2006);...

Underlying Theory

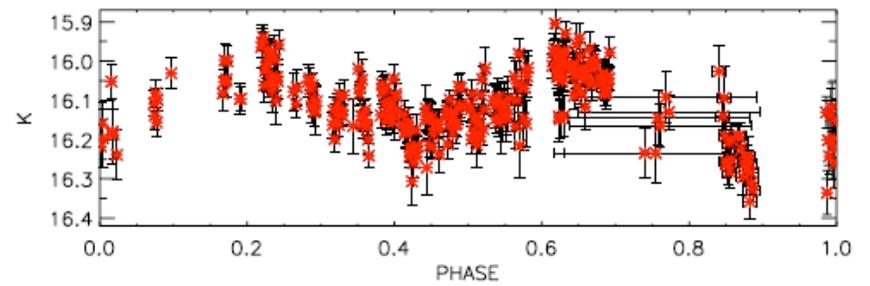
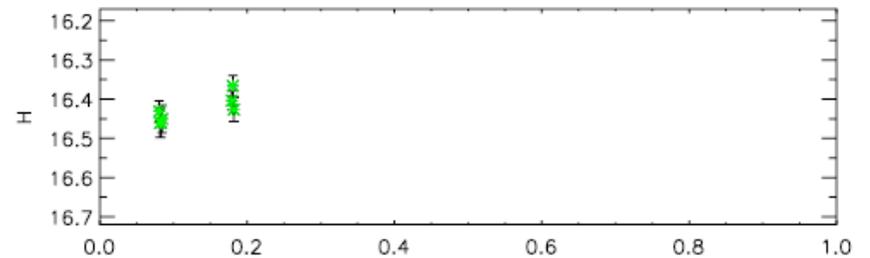
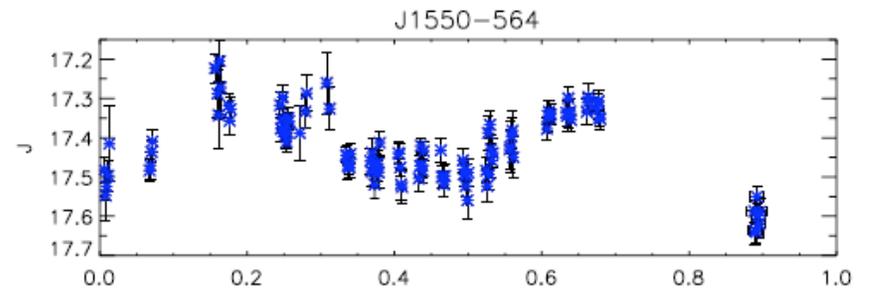
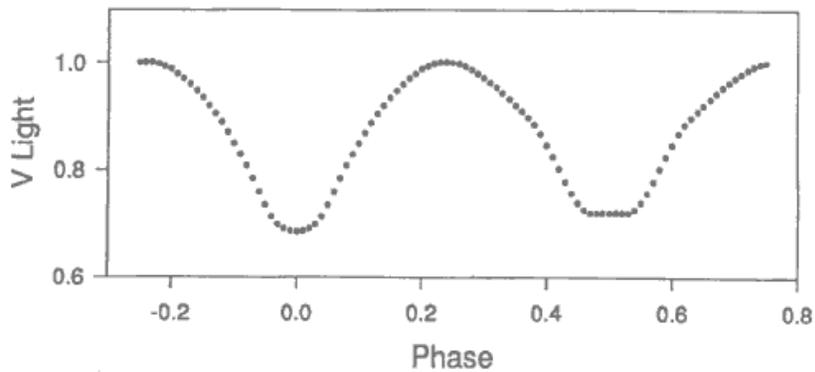
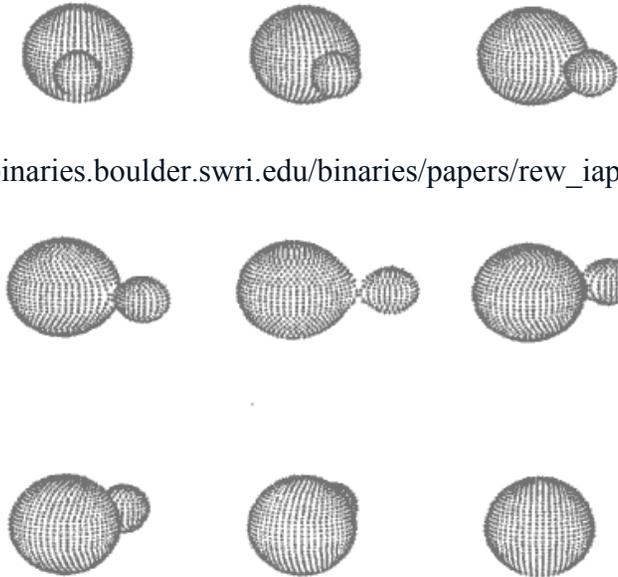
- ✧ Need accurate theoretical profiles of disk flux $F(R)$ and temperature $T(R)$
- ✧ **Answer: KerrBB** - a fully relativistic accretion disk model

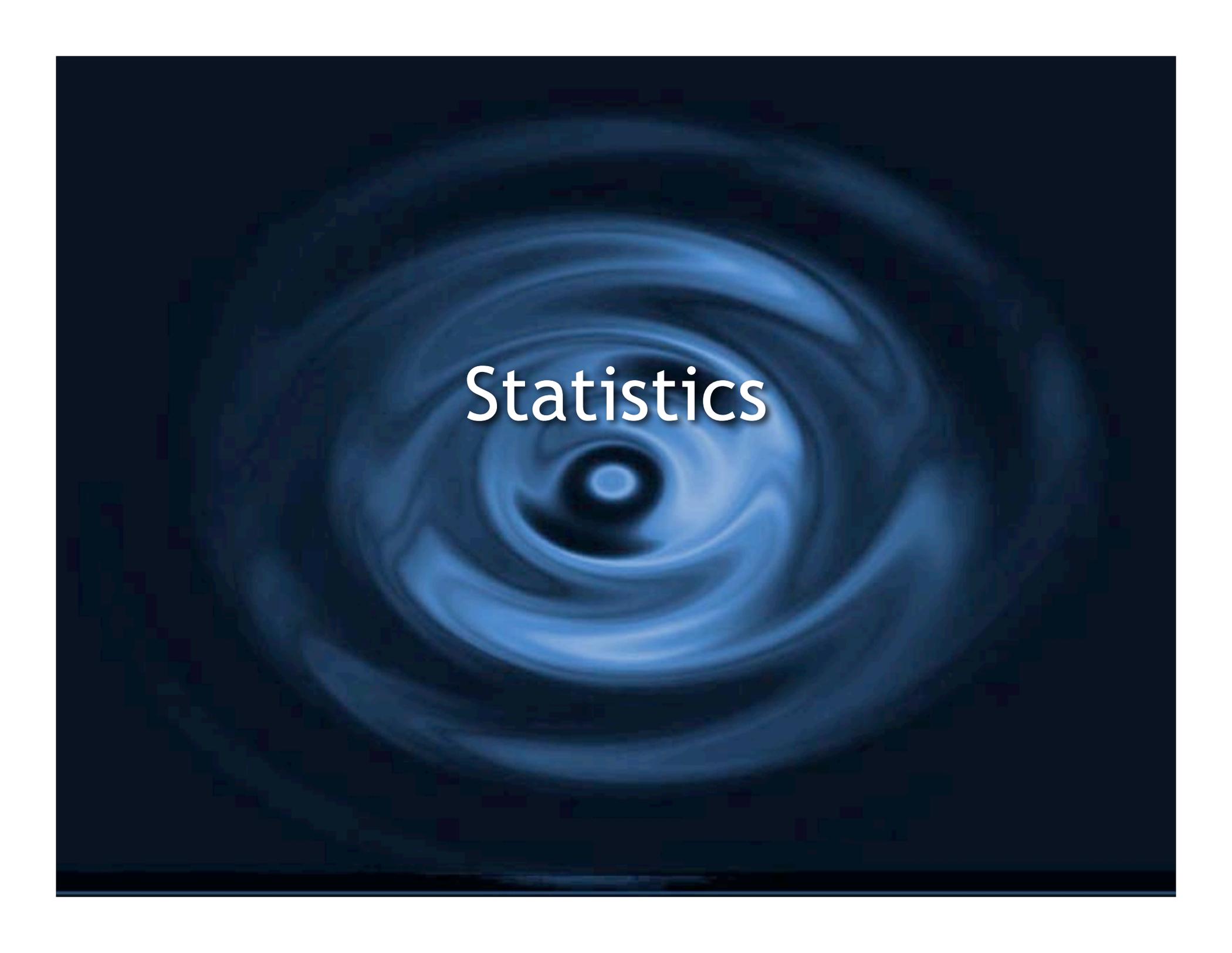
Only a_* and \dot{M} Determined from X-ray Spectrum

- ✧ M, D, i from ground-based observations
- ✧ f_{col} from disk atmosphere model
- ✧ **Zero torque** condition satisfied at ISCO for $L/L_{\text{edd}} < 0.3$
- ✧ Fit for a_* and \dot{M} ($\dot{M} \Leftrightarrow L/L_{\text{edd}}$) only
T & flux $\rightarrow a_*$ & \dot{M}

Ellipsoidal Light Curves

http://binaries.boulder.swri.edu/binaries/papers/rew_iapp_94



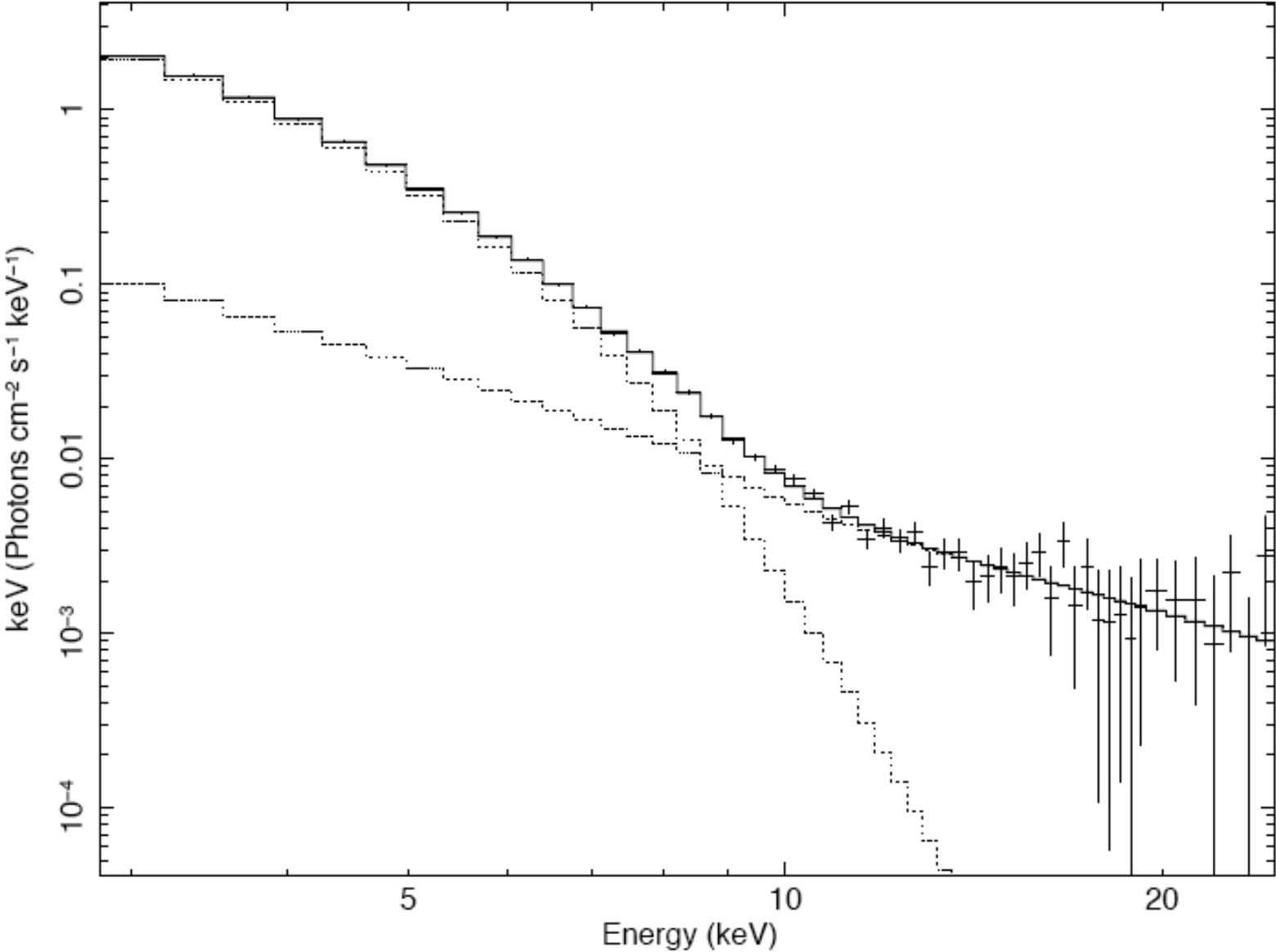


Statistics

Spectral Fitting

- ✧ ~130 RXTE X-ray spectra fit with XSPEC
 - ✧ Fitting absorption on top of a thermal disk component (to derive spin) and a power law
 - ✧ Free parameters:
 - ✧ kerrbb: a_* , \dot{M}
 - ✧ smedge: energy, optical depth
 - ✧ powerlaw: normalization, slope
 - ✧ Fixed parameters:
 - ✧ kerrbb: M , i , D , boundary torque, normalization, and flags for returning radiation & limb darkening
 - ✧ smedge: energy width, spectral index
 - ✧ phabs: N_{H} (derived from Chandra spectra)

Unfolded Spectrum



Spectral Fitting - (ctd)

✧ Questions:

✧ To MCMC or not to MCMC?

✧ Only fitting for two primary parameters and ~4-6 secondary parameters giving 40-50 d.o.f.

✧ **Is it worth the computational expense to find the global minimum if good fits are obtained?**

✧ A Common Complaint

✧ Interpretation of Cash statistic

✧ ****ONLY for Poisson errors?**

✧ The idea of $\chi_{\nu}^2=1$ being preferred is intuitive (as opposed to 0). Does Cash have a similarly immediate interpretation?

Comparing Distinct Models

- ✧ To compute the hardening factor, f , we have to compare our fully relativistic model of a multi-color disk to a partially-relativistic model that includes the relevant atomic physics
- ✧ These models are fundamentally different
- ✧ What is the best way to do this?

BHSPEC vs. KERRBB

✧ KerrBB

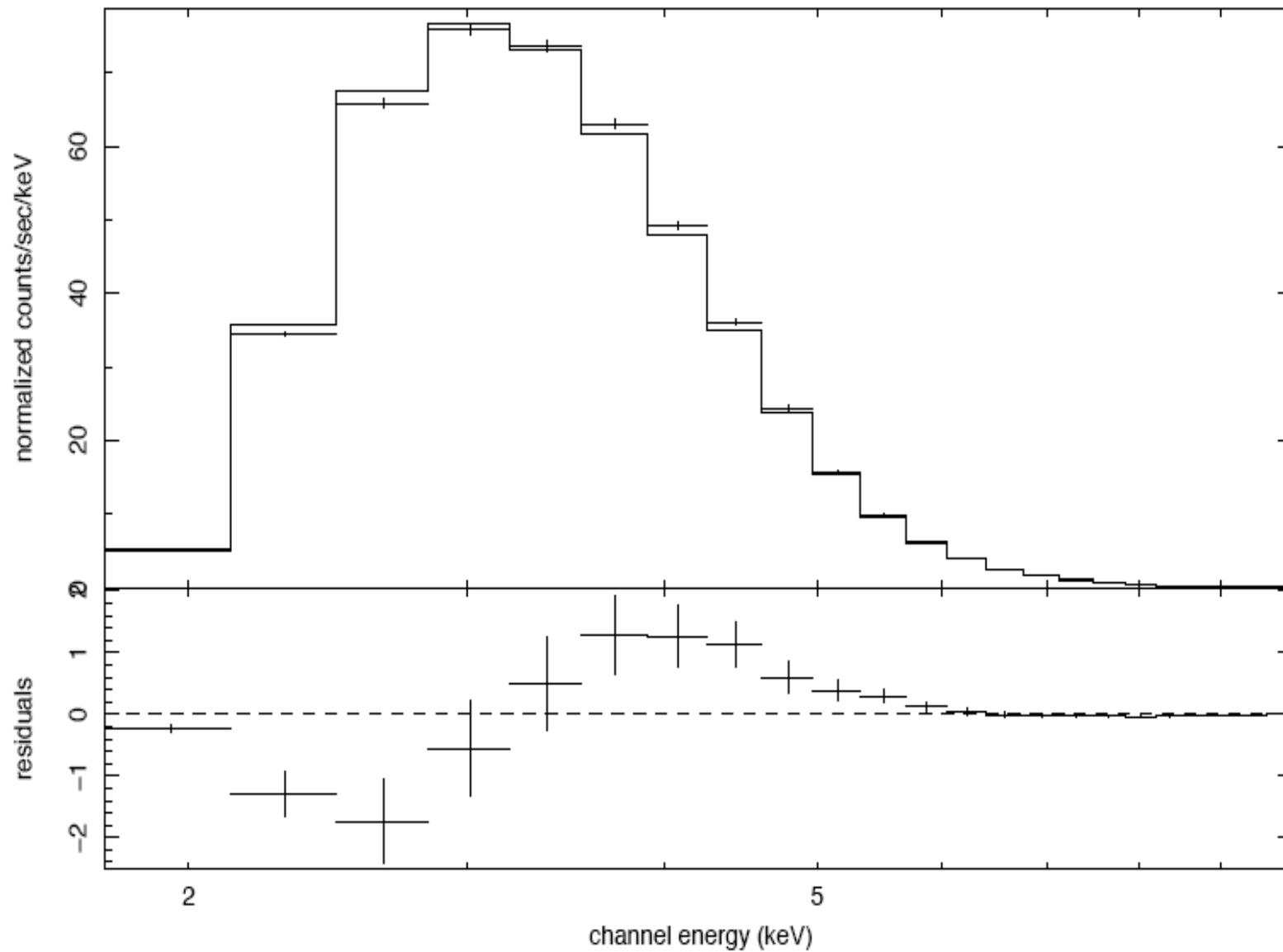
- ✧ Assumes blackbody rings, no radiative transfer
 - ✧ (no electron scattering or atomic absorption)
- ✧ Includes gravitational redshift, doppler boosting, limb darkening, returning radiation, Lense-Thirring frame dragging, can account for non-zero torque boundary condition

✧ BHSPEC

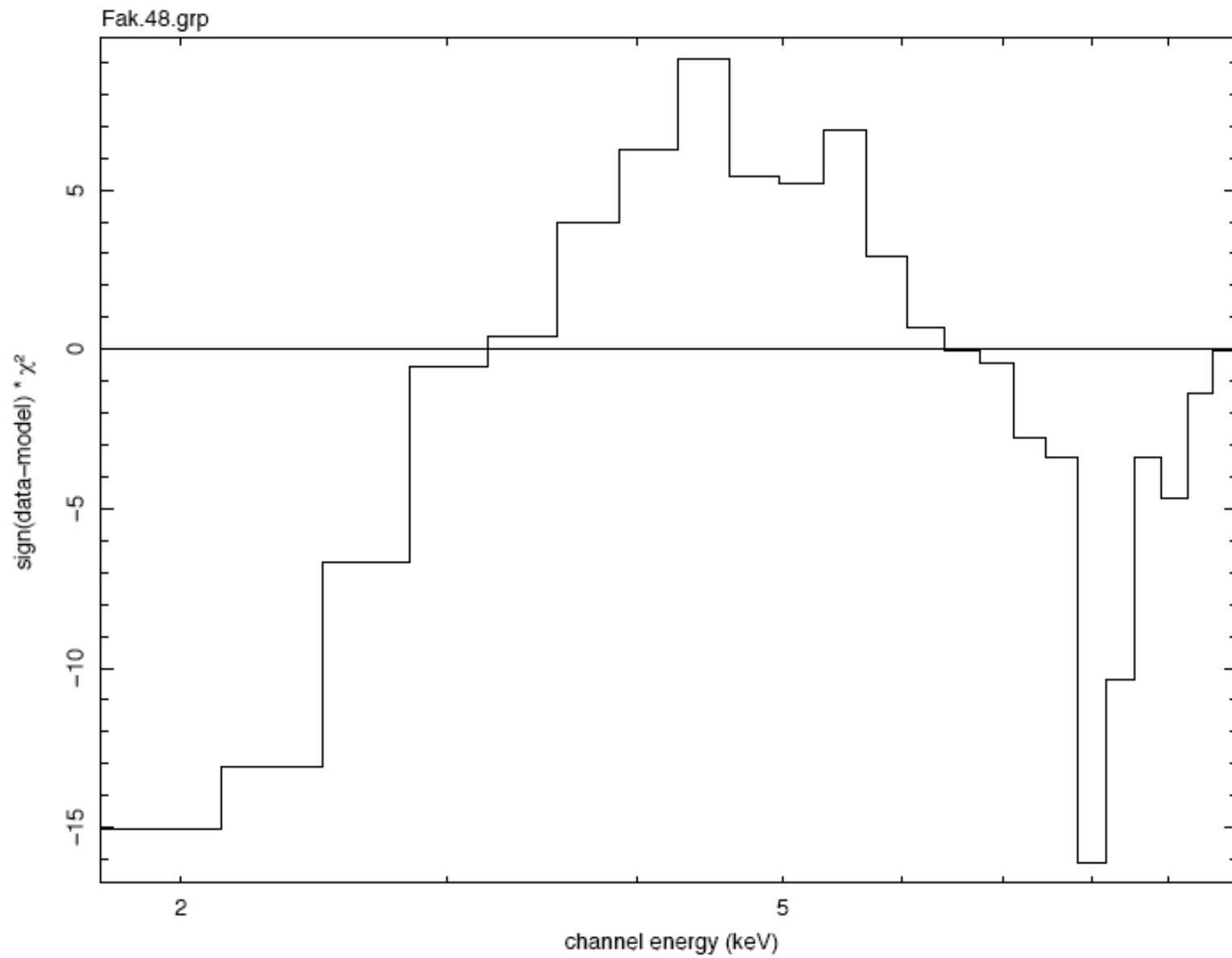
- ✧ Similar to stellar atmosphere calculations
 - ✧ Uses radiative transfer to calculate disk vertical structure
 - ✧ Takes into non LTE account electron scattering and atomic opacities
- ✧ Includes limb darkening and gravitational redshift ONLY

data and folded model

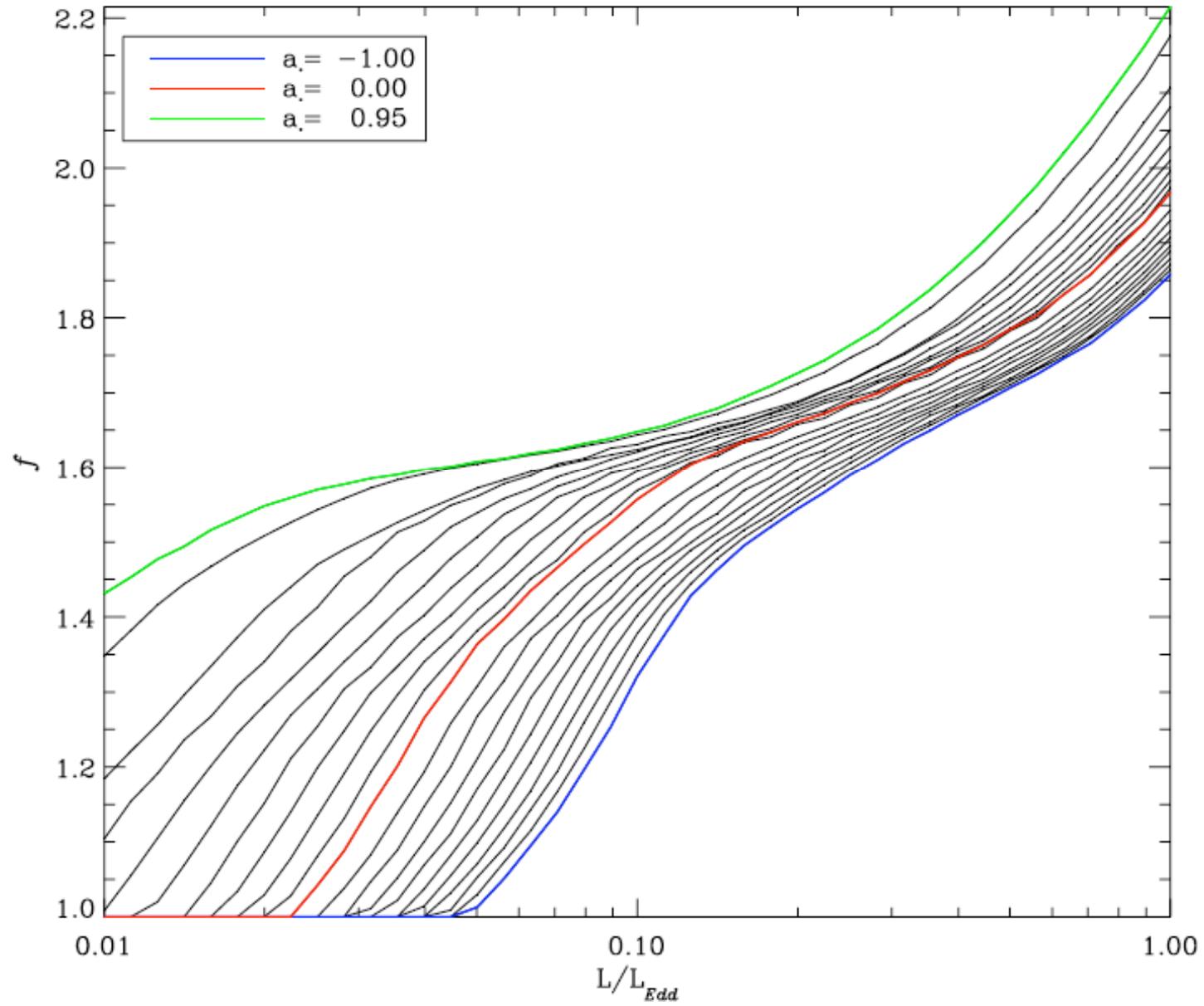
Fak.48.grp



contributions to χ^2



XTE, NH=0



Apples to Apples

- ✧ Current approach :
- ✧ **Simulated data of an accretion disk are produced** by “observing” the BHSPEC model with an RXTE instrumental response matrix.
- ✧ The fake data are **assigned Poisson errors** and fitted with KerrBB **over the same energy range as the data**, fitting for ‘f’
- ✧ **Question: Should we consider an alternative method of comparison?**
 - ✧ e.g. use a uniform response matrix with uniform error bars, fitting over the entire thermal range?

Data Classification

- ✧ Currently, we are using two selection criteria to determine which data are considered.
- ✧ I'd like to consider blurring these sharp boundaries
 - ✧ Is there a preferred way to introduce this?
 - ✧ e.g. sigmoid

“Thermal-Dominant”: $L_{\text{disk}} > 75\% L_{\text{tot}}$ thermal disk flux

Zero Torque, Thin Disk: $L_{\text{disk}} < 30\% L_{\text{edd}}$

MC Sampling

- ✧ Genetic fitting produces a high dimensional ($D > 10$) hypersurface.
- ✧ Collapse this into a 4-D topology of M, i, D vs. χ^2
- ✧ We will need to run an iteration of our analysis at each point in a large sample of M, i, D .
- ✧ Since these uncertainties dominate our error in a^* , representative sampling from this space is crucial for determining spin.
- ✧ **Challenge: how to sample from a sparsely, and nonrandom space**
- ✧ Our Answer: try to grid-sample near the best fit
- ✧ The plan is to shoot for a few thousand points and compare 2 runs as a convergence check.

Uniform Weight Resampling

- ✧ The current plan:
 - ✧ N iterations (~5000)
 - ✧ Each iteration will produce 'm' spin estimates (~100)
 - ✧ Selection function y
- ✧ Randomly select a group of "n" results from each of the N iterations such that $y(x_{ik}) \mid i \in 1 \dots m$ and $k \in 1 \dots N$ gives the probability of selecting x_{ik} .
- ✧ Use this to construct the spin PDF

Summary

- ✧ By using the constant inner radius (ISCO) of accretion disks, we are able to determine black hole spin via X-ray continuum fitting
- ✧ Spin is a very new field with promise to test and motivate fundamental theory
- ✧ We are now working to perfect our methodology, and to bring in modern statistical techniques



Fin.

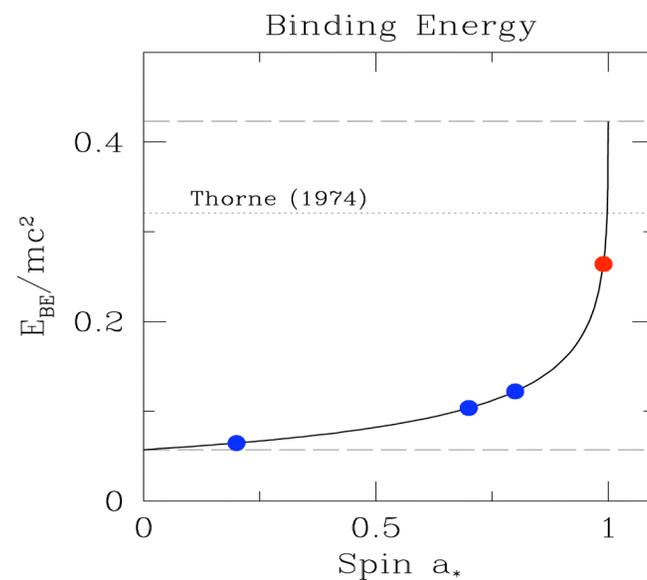
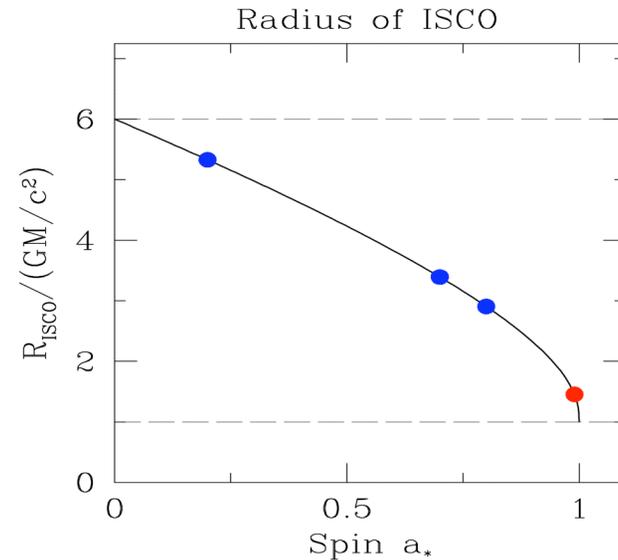
Nominal Spins of 4 BHs

LMC X-3: $a_* = 0.2$

GRO J1655-40: $a_* = 0.7$

4U 1543-47: $a_* = 0.8$

GRS 1915+105: $a_* = 0.99$



McClintock, Shafee, Narayan, et al.

Tempus Fugit

- ✧ Despite all our best intentions, we need to weigh in the computer-time required to run through our analysis
- ✧ 3000 iterations (with no MCMC) \Leftrightarrow 1 month
- ✧ Want to optimize the tradeoff between quality of our result and time

3 Other Avenues to Spin

Remillard & McClintock 2006, ARAA 44, 49

✧ Fe line profile

Fabian et al. 1989

Reynolds & Nowak 2003

✧ High-frequency X-ray QPOs (100-450 Hz)

Abramowicz & Kluzniak 2001

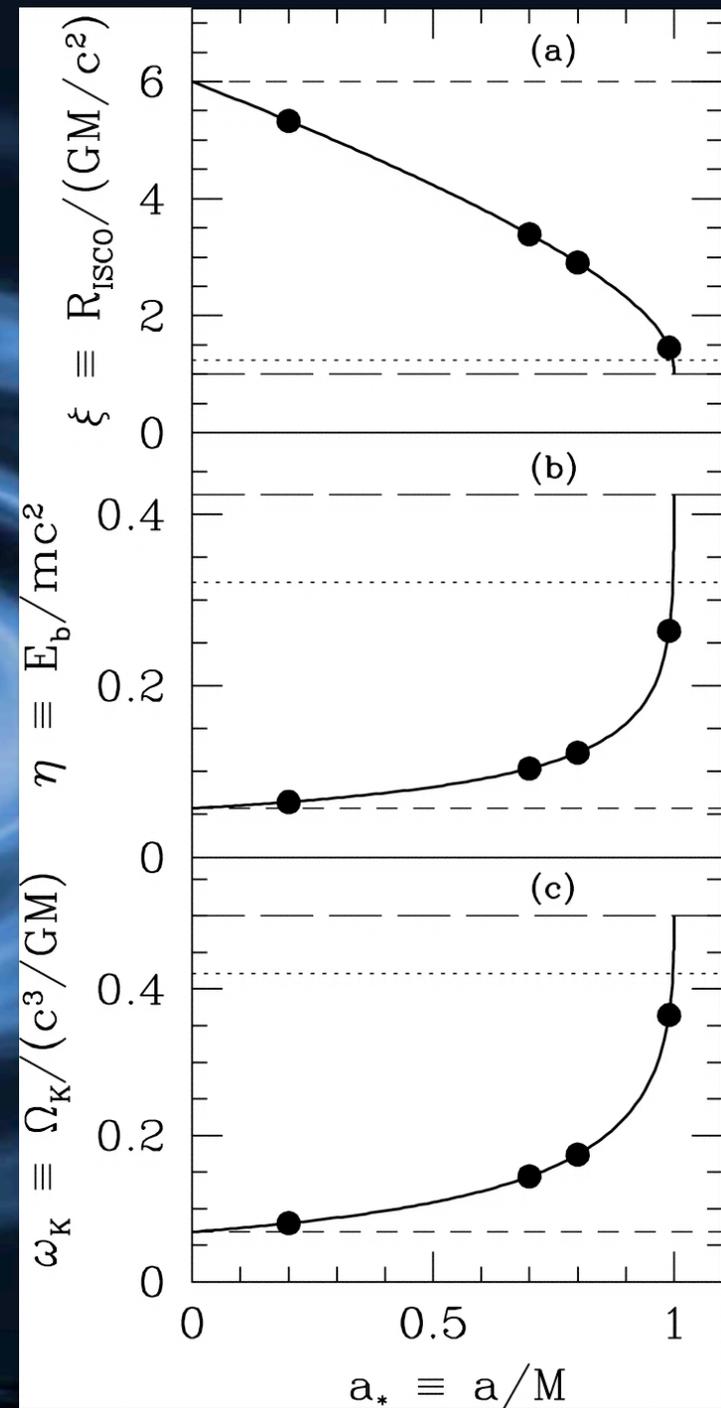
Torok et al. 2005

✧ X-ray polarimetry

Lightman & Shapiro 1975

Connors, Piran & Stark 1980

- ✧ Properties of the ISCO as a function of spin.
- ✧ Note the nonlinearity at high spin.
- ✧ (Shafee et al, 2006)



Spectral States

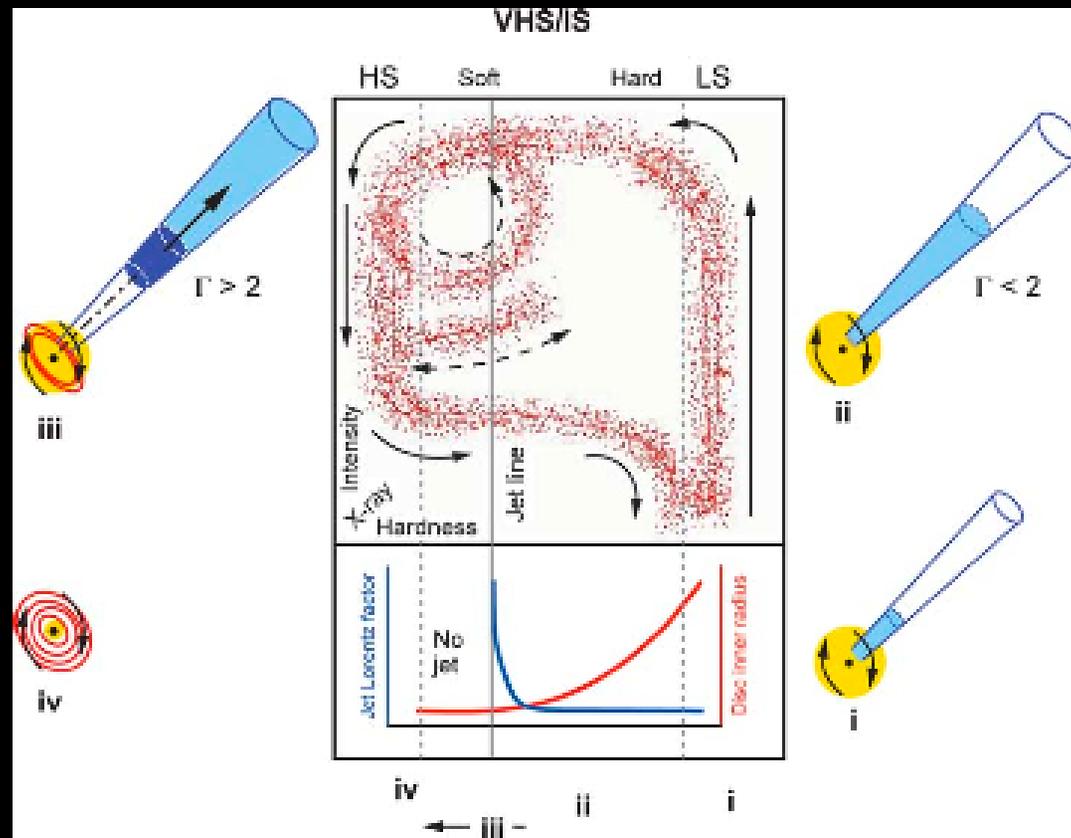


Figure 1

Fender et al. (2004)