# A MULTIPARAMETRIC ANALYSIS OF THE EINSTEIN SAMPLE OF EARLY-TYPE GALAXIES. II. GALAXY FORMATION HISTORY AND PROPERTIES OF THE INTERSTELLAR MEDIUM

PAUL B. ESKRIDGE<sup>1,2</sup> AND GIUSEPPINA FABBIANO<sup>3</sup> Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138

#### Dong-Woo Kim<sup>4</sup>

Harvard-Smithsonian Center for Astrophysics; and Department of Astronomy and Space Science, Chungnam National University, Taejon, 305-764, South Korea

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#### ABSTRACT

We have conducted bivariate and multivariate statistical analysis of data measuring the integrated luminosity, shape, and potential depth of the Einstein sample of early-type galaxies (presented by Fabbiano et al. 1992). We find significant correlations between the X-ray properties and the axial ratios (a/b) of our sample, such that the roundest systems tend to have the highest  $L_X$  and  $L_X/L_B$ . The most radio-loud objects are also the roundest. We confirm the assertion of Bender et al. (1989) that galaxies with high  $L_x$  are boxy (have negative  $a_4$ ). Both a/b and  $a_4$  are correlated with  $L_B$ , but not with IRAS 12  $\mu$ m and 100  $\mu$ m luminosities. There are strong correlations between  $L_x$ ,  $Mg_2$ , and  $\sigma_v$  in the sense that those systems with the deepest potential wells have the highest  $L_x$  and  $Mg_2$ . Thus the depth of the potential well appears to govern both the ability to retain an ISM at the present epoch and to retain the enriched ejecta of early star formation bursts. Both  $L_x/L_B$  and  $L_6$  (the 6 cm radio luminosity) show threshold effects with  $\sigma_v$ , exhibiting sharp increases at  $\log (\sigma_v) \approx 2.2$ . Finally, there is clearly an interrelationship between the various stellar and structural parameters: The scatter in the bivariate relationships between the shape parameters (a/b and  $a_{\Delta}$ ) and the depth parameter  $(\sigma_n)$  is a function of abundance in the sense that, for a given  $a_4$  or a/b, the systems with the highest  $\sigma_v$  also have the highest Mg<sub>2</sub>. Furthermore, for a constant  $\sigma_v$ , disky galaxies tend to have higher Mg<sub>2</sub> than boxy ones. Alternatively, for a given abundance, boxy ellipticals tend to be more massive than disky ellipticals. One possibility is that early-type galaxies of a given mass, originating from mergers (boxy ellipticals), have lower abundances than "primordial" (disky) early-type galaxies. Another is that disky inner isophotes are due not to primordial dissipational collapse, but to either the self-gravitating inner disks of captured spirals or the dissipational collapse of new disk structures from the premerger ISM. The high measured nuclear Mg2 values would thus be due to enrichment from secondary bursts of star formation triggered by the merging event.

Subject headings: galaxies: elliptical and lenticular, cD — galaxies: ISM — galaxies: structure — X-rays: galaxies

### 1. INTRODUCTION

The connection between the structural and stellar properties of galaxies and the nature of their interstellar medium (ISM) was first discussed by Spitzer (1954). The basic situation, as it was understood  $\sim 35$  years ago, was laid out by Sandage (1961). Our ability to observe, and thus our understanding of, the ISM has increased enormously since then. Current observational techniques allow us to collect data on the solid phase of the ISM (dust grains), as well as gas phases ranging from cold molecular cloud cores ( $T \sim 10$  K,  $n \sim 10^6$  cm<sup>-3</sup>) to X-ray-emitting gas ( $T \sim 10^{6-7}$  K,  $n \gtrsim 0.1$  cm<sup>-3</sup>). Our understanding of the relationships between ISM properties and the structural and stellar properties of galaxies is thus undergoing a concomitant rapid development.

Early-type (E and S0) galaxies, once considered devoid of intestellar gas, are now known to possess rich and complex ISM. Although many early-type galaxies exhibit the ISM tracers more traditionally associated with late-type galaxies

(e.g., Huchtmeier & Richter 1989 and Eder, Giovanelli, & Haynes 1991 for HI; Sage & Wrobel 1989 and Thronson et al., 1989 for CO; Goudfrooij et al. 1994 for Hα; Knapp et al. 1989 for FIR), X-ray observations, beginning with the Einstein Observatory (Giacconi et al. 1979) have demonstrated that the ISM in luminous early-type galaxies is typically dominated by a hot ISM (see Fabbiano 1989 and references therein).

In the previous paper of this series (Eskridge, Fabbiano, & Kim 1995, hereafter P1), we presented an analysis of the ISM properties of the Einstein sample of early-type galaxies (Fabbiano, Kim, & Trinchieri 1992, hereafter P0). The major results of P1 are as follows: In agreement with previous studies (see Fabbiano 1989 and references therein), we find a strong correlation between  $L_B$  and  $L_X$ , with a power-law slope of  $1.8 \pm 0.1$ . However, this is actually a combination of a slope 1 relation for the fainter galaxies [log  $(L_x) \le 40.5$ ] and a slope 2 relation for the more luminous galaxies. This result is consistent with previous work indicating that X-ray-faint early-type galaxies do not retain any significant quantities of hot ISM (Trinchieri & Fabbiano 1985; Fabbiano, Gioia, & Trinchieri 1989, hereafter FGT). In this case, their X-ray emission should be dominated by the integrated output of discrete sources similar to those found in the bulge of M31 (van Speybroeck et al. 1979). The X-ray emission from more distant spiral bulges is

<sup>&</sup>lt;sup>1</sup> Current address: Department of Physics and Astronomy, University of Alabama, Tuscaloosa, AL 35487.

paul@hera.astr.ua.edu.

pepi@cfa.harvard.edu.

<sup>4</sup> kim@cfa.harvard.edu.

well modeled by a composite of such sources (Fabbiano, Gioia, & Trinchieri 1988). These results are also supported by differences found between the X-ray spectra of X-ray-bright and X-ray-faint E and S0 galaxies, suggesting the presence of stellar emission in the X-ray-faint objects (Kim, Fabbiano, & Trinchieri 1992b; Fabbiano, Kim, & Trinchieri 1994; Fabbiano 1994).

The mean values of the distribution functions of both  $L_{\rm X}$  and  $L_{\rm X}/L_{\rm B}$  for the S0's are lower than those for the E's at the 2.8  $\sigma$  and 3.5  $\sigma$  levels, respectively. Thus, for a given stellar luminosity, the potential wells of S0's may be shallower than those of E's. The rotation of the S0 disks may be an important factor (see also Pellegrini 1994). The other differences found between E and S0 galaxies may be related to differences in their star formation histories: Our S0 sample has excess 12  $\mu$ m emission compared to the E sample, when scaled by their optical luminosities. This may be due to emission from dust heated in star-forming regions in S0 disks. This interpretation is supported by the existence of a strong  $L_{12}$ - $L_{100}$  correlation for our S0 sample that is not found for the Es and by an analysis of optical-IR colors.

We also find strong indications of a connection between galaxy ISM and nuclear activity. There are steep power-law slopes between radio luminosity and optical, X-ray properties, and FIR properties. This last point argues that the presence of a FIR-emitting ISM in early-type galaxies is coupled to their ability to generate nonthermal radio continuum, as previously argued by, e.g., Walsh et al. (1989). However, we also find that for a given  $L_{100}$ , galaxies with larger  $L_X/L_B$  tend to be stronger nonthermal radio sources, as originally suggested by Kim & Fabbiano (1990). We note that while  $L_B$  is most strongly correlated with  $L_6$ , the total radio luminosity (summed over a  $\sim 1\%$ bandwidth around 6 cm—see P1), both  $L_X$  and  $L_X/L_B$  are more strongly correlated with  $L_{6co}$ , the core radio luminosity. These points support the argument (proposed by FGT) that radio cores in early-type galaxies are fueled by the accretion of cooling flow gas from the hot ISM.

The picture that emerges from P1 connects the properties of the ISM in E and S0 galaxies to their star formation history and nuclear activity. We confirm the differences between X-ray-bright and X-ray-faint galaxies and link these differences to the relative ability to retain a hot ISM. This ability is potentially connected to galaxy morphology, but this is not a complete explanation, as both Es and S0's can be found over a very large range of  $L_{\rm X}/L_{\rm B}$ . However, the results of P1 suggest a link between the characteristics of the galaxy potential and the retention of a hot ISM. This is not a tautology, as other mechanisms such as ram-pressure stripping, interactions with close neighbors (e.g., White & Sarazin 1991), variation in the SN Ia rate, and overall evolutionary state of the ISM (e.g., Ciotti et al., 1991; Pellegrini & Fabbiano 1994) could also effect the  $L_{\rm X}/L_{\rm B}$  for galaxies of a given luminosity.

To further explore the role of the shape and depth of the galaxy potential in determining the state of the ISM in early-type galaxies and how this relates to galaxy formation mechanisms, we extend the study of P1 with a consideration of available data on the structure and stellar populations of the Einstein sample. The data collected in P1 (see Table 1 of P1) will be used in this paper to compare with the information relating to the structural and stellar properties of the sample. In § 2, we describe how we have built our data set for this project and review the required statistical methods. We present our analysis of the axial ratio data in § 3. The Mg<sub>2</sub> results are

given in § 4, those for  $\sigma_v$  in § 5, and those for  $a_4$  in § 6. We summarize our results and conclusions and discuss possible strategies for future research in § 7. The Appendix contains details of our statistical analysis.

### 2. SAMPLE CONSTRUCTION AND STATISTICAL METHODS

We have gathered information from the literature regarding the structural and chemical properties of the galaxies in our sample. Axial ratios have been taken from de Vaucouleurs et al. (1991, hereafter RC3). These are listed, for the entire sample, in Table 1 of P1. We discovered a zero-point offset between the a/b values from de Vaucouleurs, de Vaucouleurs, & Corwin (1976) and those of Faber et al. (1989, hereafter 7S). Such an offset does not exist for the RC3 values compared to the 7S values. We have therefore adopted the more extensive set of values from the RC3. The  $a_4$  parameter, defined in Bender et al. (1989), is a measure of the amplitude of the  $\cos (4\theta)$  Fourier component of the deviation from ellipticity of the isophotes of early-type systems. Values of  $a_4$  for 47 galaxies in our sample have been published by Bender et al. (1989) and Peletier et al. (1990). We have taken values of  $\log (\sigma_n)$  (for 74 galaxies) and Mg<sub>2</sub> (for 73 galaxies ) from 7S. All these available data are given in Table 1.

Many of our data in the X-ray, FIR, and radio are upper limits. Therefore, the use of standard statistical techniques is manifestly invalid for our project. Instead we use techniques from the field of survival analysis for both evaluating the existence of bivariate correlations amongst our data and for determining best-fit regression coefficients. These methods explicitly account for the existence of upper limits in the samples being tested, subject to regularity conditions that may or may not apply in the case of any given data sample. This last point is, of course, the standard problem in all astronomical statistical analysis. In an effort to minimize it, we use a number of different statistical tests, each with their own assumptions about the nature of the data and distribution of the upper limits, in the hopes that gross violations of the normality assumptions by our data will manifest themselves in highly discrepant results for the various statistical tests. Basic references in the astronomical literature for these methods are Feigelson & Nelson (1985), Schmitt (1985), Isobe, Feigelson, & Nelson (1986), LaValley, Isobe & Feigelson (1992), and Fiegelson & Babu (1992). Details of our particular procedures are given in P1.

As we are dealing with a multiparametric data set, it is important to investigate possible interrelationships between the various observables in our sample. A technique used in previous studies (Fabbiano et al. 1988; P1) is the partial Spearman rank method (Kendall & Stuart 1976). In brief, to apply this method, one builds a matrix of modified Spearman rank coefficients for the parameters to be tested, and then tests the correlation between subsamples of the parameters in the matrix set while holding all other variables in the matrix set constant. The major results of the partial-rank analysis are presented in the text below. The full details of our results are tabulated in Appendix A. As we do not have terribly large samples for some combinations of observables, there is some reason for concern that we may obtain correlations (or noncorrelations) from our partial-rank analysis that would not stand up if we had a truly large sample. In order to examine this possibility, we drew a number of random subsamples from our  $L_B$ - $L_X$ -a/b and  $L_B$ - $L_X$ -a/b- $Mg_2$  samples (discussed in §§ 3) and 4, below) and subjected them to partial-rank analysis. In no case did correlations appear for the subsamples that were

TABLE 1
STRUCTURAL DATA

STRUCTURAL DATA							
Name	Type	log(a/b) 7S	log(a/b) RC3	$Mg_2$ mags	$\log \sigma_v \ \mathrm{km/sec}$	$a_4/a \times 100$	
NGC 205	-3	0.26	0.30				
NGC 221	-6	0.06	0.13	0.185	1.892		
NGC 315 NGC 499	-3 -3	$0.14 \\ 0.19$	$0.20 \\ 0.10$	$0.283 \\ 0.334$	$2.546 \\ 2.374$	-0.46	
NGC 499 NGC 507	-2	0.19	0.10	0.334 $0.302$	$\frac{2.574}{2.563}$		
NGC 533	-5	0.10	0.21	0.316	2.504	0.00	
NGC 584 NGC 596	-2 -5	0.22	0.26	0.283	2.337	1.50	
NGC 590 NGC 720	-5	$0.06 \\ 0.22$	$0.19 \\ 0.29$	$0.249 \\ 0.330$	$2.179 \\ 2.392$	$^{1.30}_{-0.30}$	
NGC 1052	-3	0.17	0.16	0.316	2.313	0.00	
NGC 1172	-2	0.04	0.11	0.246	2.083		
NGC 1316 NGC 1395	-2 -5	$0.12 \\ 0.11$	$0.15 \\ 0.12$	0.313	2.412		
NGC 1399	-5	0.07	0.03	0.334	2.491		
NGC 1404	-5	0.08	0.05	0.317	2.353		
NGC 1400 NGC 1407	-3 -5	$0.04 \\ 0.02$	$0.06 \\ 0.03$	$0.309 \\ 0.327$	$2.398 \\ 2.455$	$0.00 \\ -0.30$	
NGC 1553	-2	0.02	0.20	0.021	2.400	-0.50	
NGC 1600	-5	0.19	0.17	0.324	2.506	-1.10	
NGC 2314 NGC 2300	-5 -5	$0.11 \\ 0.11$	$0.09 \\ 0.14$	$0.327 \\ 0.319$	$2.463 \\ 2.430$	1 10	
NGC 2563	-2	0.11	0.14	0.319	2.430 $2.416$	1.10	
NGC 2629	-2	0.15	0.07	0.308	2.380		
NGC 2694 NGC 2693	-5 -5	0.10	0.01	0.328	9 445	1.00	
NGC 2832	-5	$0.18 \\ 0.14$	$0.16 \\ 0.10$	$0.328 \\ 0.340$	$2.445 \\ 2.557$	$\frac{1.00}{-0.40}$	
NGC 2974	-5	0.16	0.23	0.300	2.346	0.50	
NGC 3078	-5	0.19	0.08	0.334	2.376		
NGC 3115 NGC 3258	-2 -5	$0.41 \\ 0.04$	$0.47 \\ 0.07$	$0.309 \\ 0.342$	$2.425 \\ 2.435$	0.00	
NGC 3377	-5	0.27	0.24	0.270	2.116	1.55	
NGC 3379	-5	0.07	0.05	0.308	2.303	0.25	
NGC 3585 NGC 3607	-3 -2	$0.24 \\ 0.09$	$0.26 \\ 0.30$	$0.308 \\ 0.303$	$2.343 \\ 2.394$		
NGC 3608	-5	0.03	0.09	0.303	$\frac{2.394}{2.310}$	-0.20	
NGC 3818	-5	0.20	0.22	0.315	2.314	2.30	
NGC 3894 NGC 3923	-5 -3	$0.27 \\ 0.23$	$0.21 \\ 0.18$	$0.322 \\ 0.306$	$2.422 \\ 2.335$	$-0.70 \\ -0.40$	
NGC 3923 NGC 4105	-3 -2	0.23	0.13	0.300 $0.299$	2.384	-0.40	
NGC 4168	-2 -5	0.04	0.08	0.260	2.259	0.80	
NGC 4251 NGC 4261	-2 -5	0.00	0.39	0.990	2 469	$^{2.80}_{-1.60}$	
NGC 4201 NGC 4291	-5 -5	$0.09 \\ 0.13$	$0.05 \\ 0.08$	$0.330 \\ 0.308$	$2.468 \\ 2.413$	-0.40	
NGC 4365	-5	0.14	0.14	0.321	2.394	-1.10	
NGC 4374	-5	0.08	0.06	0.305	2.458	-0.50	
NGC 4382 NGC 4387	-2 -5	0.24	$0.11 \\ 0.21$	0.240	1.922	$0.80 \\ -1.00$	
NGC 4406	-3	0.13	0.19	0.311	2.398	-0.85	
NGC 4458	-5	0.10	0.04	0.227	2.027		
NGC 4467 NGC 4472	-5 -3	$0.12 \\ 0.12$	$0.10 \\ 0.09$	$0.262 \\ 0.306$	$1.917 \\ 2.458$	-0.35	
NGC 4473	-5 -5	0.12	0.25	0.304	2.250	0.90	
NGC 4550	-3		0.55			1.67	
NGC 4551 NGC 4552	-5 -2	0.15	0.10	0.264	1.999	-0.90	
NGC 4552 NGC 4564	-2 -5	$0.02 \\ 0.40$	$0.04 \\ 0.38$	$0.324 \\ 0.321$	$2.417 \\ 2.185$	2.20	
NGC 4589	-5	0.09	0.09	0.320	2.332		
NGC 4621 NGC 4636	-5	0.19	0.16	0.328	2.381	1.50	
NGC 4649	-3 -2	$0.09 \\ 0.10$	$0.11 \\ 0.09$	$0.311 \\ 0.338$	$2.281 \\ 2.533$	$-0.15 \\ -0.50$	
NGC 4645	-5	0.24	0.21	0.273	2.233	0.00	
NGC 4697	-5	0.23	0.19	0.297	2.218	2.00	
NGC 4782 IC 3896	-5 -5	$0.08 \\ 0.04$	$0.02 \\ 0.12$	0.333	$2.522 \\ 2.346$		
NGC 5044	-5	0.00	0.00	0.324	2.370		
NGC 5077	-5	0.17	0.11	0.295	2.439	-0.90	
NGC 5102 IC 4296	-2 -5	$0.24 \\ 0.06$	$0.49 \\ 0.02$	$0.005 \\ 0.323$	2.509		
IC 4329	-2	0.15	0.24	0.325	2.447	0.80	
NGC 5322	-5	0.17	0.18	0.276	2.350	-0.90	
NGC 5485 NGC 5532	-2 -2	0.04	$0.08 \\ 0.00$	0.291	2.190	-0.70	
NGC 5532 NGC 5576	-5	0.14	0.00	0.253	2.272	-0.70 $-0.50$	
NGC 5846	-2	0.04	0.03	0.321	2.444		
NGC 5982 NGC 6146	-5 -2	$0.14 \\ 0.16$	$0.12 \\ 0.10$	$0.296 \\ 0.289$	$2.425 \\ 2.435$	-0.80	
NGC 6146 NGC 6876	-5	0.10	0.10	0.289 $0.284$	2.435 $2.364$	0.60	
NGC 7236	-3	0.13	0.00	0.309	2.226	· ·	
NGC 7237	-3	0.03	0.00	0.327	2.234		
NGC 7332 IC 1459	-2 -5	0.15	$0.56 \\ 0.14$	0.321	2.488		
NGC 7562	-5	0.18	0.18	0.291	2.385		
NGC 7619	-5	0.12	0.04	0.336	2.528	0.30	
NGC 7626	-5	0.06	0.05	0.336	2.369	0.40	

not also present for the full sample. A number of correlations that are present for the full sample disappeared for some of the subsamples. However, this was typically due to the decrease in the number of objects in the sample, rather than a decrease in the correlation statistic. We conclude that the strong correlations and clear noncorrelations we find are robust. It is, however, quite possible that our more marginal results would be reversed if tested with a larger sample. We urge the reader to keep this caveat in mind.

#### 3. COMPARISONS WITH AXIAL RATIOS

## 3.1. X-Ray and Optical Trends

In Figure 1a we show a scatter plot of  $L_B$  against a/b. There is some evidence for a relationship in that the most luminous objects are also the roundest. Table 2 shows the results of the bivariate correlation tests on this sample: there does appear to be a statistically significant effect. If we break the sample into E and S0 subsets, we find similar distributions for both types, with the distinction that the range in axial ratio for the S0's is inevitably larger than that of the ellipticals. However, the statistical analysis of the two subsets shows no compelling evidence for correlation between  $L_B$  and a/b (see Table 2). The correlation for the full sample is only at the  $\sim 1\%$  level: halving the sample size by testing the Es and So's independently may simply reduce the sample size to the point that the correlation vanishes. Also, any intrinsic relationship between axial ratio and luminosity will be partially masked by the projection of the three-dimensional galaxies onto two dimensions. We note, however, that the most optically luminous galaxies in both subsamples are also the roundest.

The comparison of  $L_X$  with a/b is shown in Figure 1b. The trend with a/b noted above for  $L_B$  appears much more pronounced for  $L_x$ . Indeed, the results of the bivariate analysis (Table 2) show the effect to be much stronger than for  $L_R$ . We note that the correlation we see is not a strict linear one. It is more of a wedge: Galaxies with small a/b span the full range of  $L_x$ . Galaxies with large a/b all have  $L_x \lesssim 10^{41}$  ergs s<sup>-1</sup>. One might expect that this effect would be a strong function of morphology, but separation by type shows that, as well as it can be defined (given the inevitably small number of ellipticals with large a/b), the trend holds up for both ellipticals and S0's. The statistical correlation does not, however, (Table 2). It breaks down particularly for the ellipticals. We note that the only two objects with  $\log (a/b) \ge 0.3$  (i.e., roughly E5) have fairly low X-ray upper limits. These could, however, be misclassified S0's. The trend for the S0's is weaker than for the full sample but is still significant in two of the three tests. The relationship defined by  $L_x/L_B$  is stronger than that defined by  $L_X$  (see Table 2 and Fig. 1c), and once again, the trend holds for both morphological subsets. More importantly, with the exception of the Cox-Hazard test for the Es, the statistical correlation holds for both subsets: For either Es or S0's alone, there is a positive correlation such that those systems with the largest  $L_X/L_B$  are the roundest objects. It is very hard to imagine how projection effects could create such a correlation, although they could easily destroy it, as apparently round galaxies could be intrinsically flattened, but viewed face on.

A partial-rank analysis on  $L_B$ - $L_X$ - $L_X$ / $L_B$ -a/b for the full sample confirms that the underlying trend is that between  $L_X/L_B$  and a/b, in the sense that the roundest galaxies have the largest  $L_X/L_B$  (see Table A1a; see Appendix for details on this table). The bivariate trends of a/b with both  $L_B$  and  $L_X$  appear to be driven by this underlying relationship. We obtain the same results if we remove the Local Group dwarfs from the

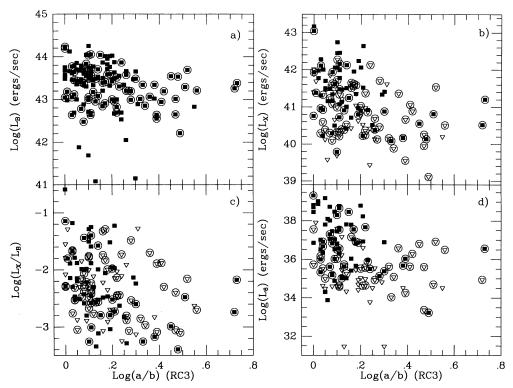


Fig. 1.—Plot of  $\log(a/b)$  against (a)  $L_B$ , (b)  $L_\chi$ , (c)  $L_\chi/L_B$ , and (d)  $L_6$  for the full sample. Solid squares represent detections. Down-pointing open triangles represent upper limits. Circled points represent the S0's.

TABLE 2
BIVARIATE CORRELATION TESTS WITH THE LUMINOSITY DATA

	$L_X$		$L_B$		$L_X/L_B$		$L_{12}$		$L_{100}$		$L_6$	
	$N_{tot}$ Cox-Hazard $^a$ ) Kendall's $ au$ Spearman rank	$N_{lim}^{\ b)}$ prob prob	$N_{tot}$	$N_{lim}$ prob prob	N <sub>tot</sub>	$N_{lim}$ prob prob	$\stackrel{-12}{N_{tot}}$	$N_{lim}$ prob prob	N <sub>tot</sub>	$N_{lim}$ prob prob	N <sub>tot</sub>	$N_{lim}$ prob prob
a/b	147 $9.727$ $4.337$ $-0.346$	$\begin{array}{c} 77 \\ 0.0018 \\ < 10^{-4} \\ < 10^{-4} \end{array}$	$\begin{array}{c} 147 \\ 6.671 \\ 3.260 \\ -0.270 \end{array}$	0 0.0098 0.0011 0.0011	147 $14.343$ $4.735$ $-0.389$	$\begin{array}{c} 77 \\ 0.0002 \\ < 10^{-4} \\ < 10^{-4} \end{array}$	134 $0.549$ $1.013$ $-0.080$	75 0.4587 0.3112 0.3544	$\begin{array}{c} 135 \\ 1.724 \\ 0.594 \\ -0.077 \end{array}$	48 0.1892 0.5522 0.3756	133 $2.876$ $4.960$ $-0.435$	$\begin{array}{c} 63 \\ 0.0899 \\ < 10^{-4} \\ < 10^{-4} \end{array}$
$Mg_2$	73 17.442 4.395 0.514	$\begin{array}{c} 26 \\ < 10^{-4} \\ < 10^{-4} \\ < 10^{-4} \end{array}$	73 20.965 3.212 0.361	$\begin{array}{c} 0 \\ < 10^{-4} \\ 0.0013 \\ 0.0022 \end{array}$	73 13.450 3.962 0.479	$\begin{array}{c} 26 \\ 0.0002 \\ 0.0001 \\ < 10^{-4} \end{array}$	69 8.786 2.991 0.372	39 0.0030 0.0028 0.0022	69 4.549 1.366 0.185	28 0.0329 0.1720 0.1261	72 12.823 3.472 0.426	26 0.0003 0.0005 0.0003
$\sigma_{m{v}}$	74 29.165 6.091 0.670	$\begin{array}{c} 27 \\ < 10^{-4} \\ < 10^{-4} \\ < 10^{-4} \end{array}$	74 50.449 5.984 0.634	$\begin{array}{c} 0 \\ < 10 - 4 \\ < 10 - 4 \\ < 10 - 4 \end{array}$	74 21.787 5.072 0.586	$\begin{array}{c} 27 \\ < 10^{-4} \\ < 10^{-4} \\ < 10^{-4} \end{array}$	68 8.909 2.523 0.312	39 0.0028 0.0116 0.0105	68 11.516 3.166 0.398	29 0.0007 0.0015 0.0011	72 16.694 4.259 0.494	$\begin{array}{c} 27 \\ < 10^{-4} \\ < 10^{-4} \\ < 10^{-4} \end{array}$
a <sub>4</sub>	47 $9.648$ $2.684$ $-0.424$	16 0.0019 0.0073 0.0040	47 6.287 2.351 -0.324	0 0.0122 0.0187 0.0280	$\begin{array}{r} 47 \\ 10.010 \\ 2.397 \\ -0.374 \end{array}$	16 0.0016 0.0165 0.0111	46 2.813 1.371 -0.218	26 0.0935 0.1704 0.1438	46 4.331 1.679 -0.300	18 0.0374 0.0932 0.0439	47 7.338 2.889 -0.381	20 0.0068 0.0039 0.0097
a <sub>4</sub> no dEs	44 $15.540$ $3.333$ $-0.537$	13 0.0001 0.0009 0.0004	$\begin{array}{c} 44 \\ 12.601 \\ 3.261 \\ -0.473 \end{array}$	0 0.0004 0.0011 0.0019	$44 \\ 11.426 \\ 2.795 \\ -0.439$	13 0.0007 0.0052 0.0040	43 6.704 1.878 -0.307	23 0.0096 0.0603 0.0466	$\begin{array}{c} 43 \\ 5.602 \\ 2.076 \\ -0.378 \end{array}$	16 0.0179 0.0379 0.0144	44 10.758 3.526 -0.498	18 0.0010 0.0004 0.0011
a/b Es only	73 1.017 2.620 -0.295	31 0.3132 0.0088 0.0119	73 3.749 1.411 -0.169	0 0.0528 0.1582 0.1484	73 $0.877$ $2.835$ $-0.323$	31 0.3490 0.0046 0.0058	$\begin{array}{c} 64 \\ 3.475 \\ 1.392 \\ -0.181 \end{array}$	36 0.0623 0.1640 0.1500	$\begin{array}{c} 64 \\ 1.572 \\ 0.627 \\ -0.106 \end{array}$	24 0.2099 0.5307 0.4011	70 $1.147$ $4.117$ $-0.479$	$\begin{array}{c} 29 \\ 0.2842 \\ < 10^{-4} \\ 0.0001 \end{array}$
a/b S0s only	74 $2.708$ $2.978$ $-0.329$	47 0.0998 0.0029 0.0049	74 2.699 1.845 -0.215	0 0.1004 0.0650 0.0665	74 3.953 3.259 -0.343	47 0.0468 0.0011 0.0034	70 0.066 0.236 0.004	39 0.7970 0.8134 0.9729	71 1.184 0.474 -0.092	24 0.2764 0.6354 0.4400	62 6.513 2.481 -0.328	34 0.0107 0.0131 0.0104

<sup>&</sup>lt;sup>a</sup> The values in rows (2)-(4) of these columns are the test scores for the three correlation tests.

<sup>&</sup>lt;sup>b</sup> The  $N_{\text{lim}}$  are the number of limit points.

sample. Recalling that projection effects will clearly weaken a trend between  $L_X/L_B$  and a/b, we find compelling evidence for a physical correlation between the presence of X-ray gas and the shape of the gravitational potential in early-type galaxies. The trends of a/b with both  $L_X$  and  $L_X/L_B$  are significantly weakened with  $a_4$  held constant (see Table A1a). This may be an effect of the reduction in sample size (less than a third of our full sample has  $a_4$  measurements), or it may be due to underlying trends of both the X-ray properties and a/b with  $a_4$ . This matter is discussed further in §§ 6.1 and 6.3. An  $L_B$ -a/b trend does appear when pairs or triplets including the X-ray properties and either or both of  $Mg_2$  and  $\sigma_v$  are held constant (see Table A1a). This trend is in the sense that more optically luminous galaxies are flatter for constant  $Mg_2$  or  $\sigma_v$ . This is in keeping with the observation that systems with more predominant disk components (i.e., spirals) tend to have lower abundances than do ellipticals for a given luminosity.

Considering the Es only, the partial-rank analysis gives trends that are substantially weaker (see Table A1b). However, we still find evidence for trends between a/b and both  $L_X$  and  $L_X/L_B$ , with the  $L_X/L_B$ -a/b relation being the stronger. Removal of the Local Group dwarfs does not change these results. For the S0's, the trends are significantly stronger than for the Es (although weaker than for the full sample), with the  $L_X/L_B$ -a/b trend again being the dominant one (see Table A1b). This is particularly interesting, as the presence of significant disks in the S0's should make the  $L_X/L_B$ -a/b correlation more susceptible to projection than the Es. This therefore supports the conclusion that there is an underlying physical effect operating to enhance  $L_X/L_B$  is those galaxies with the roundest potentials.

# 3.2. Trends with Other ISM Tracers

The same sort of trend appears to exist between  $L_6$  and a/b (see Fig. 1d), although the Cox-Hazard test is discrepant for the full sample and the Es (see Table 2). Partial-rank analysis confirms that there is a good correlation between radio power and axial ratio, independent of trends between these parameters and optical or X-ray properties (see Table A1a). This trend is in keeping with the result of Disney, Sparks, & Wall (1984) that radio-loud ellipticals tend to be significantly rounder than radio-silent ellipticals. Smith & Heckman (1989) do not confirm this result. However, they concentrate specifically on the most powerful radio galaxies, whereas both the Disney et al. sample and our own examine galaxies over a much larger range of radio power.

Knapp, Gunn, & Wynn-Williams (1992) argue quite convincingly that the bulk of the midinfrared emission from earlytype galaxies is due to stellar and circumstellar radiation and thus should scale with optical luminosity (see, however the recent work of Sauvage & Thuan 1994). In P1, we found a difference at the 2  $\sigma$  level between the slopes of the relationships of  $L_B$  and  $L_{12}$  with  $L_X$  that appears to be driven entirely by the So's. Having derived a reasonably strong correlation between  $L_B$  and a/b, we have thus tested for a correlation between  $L_{12}$  and a/b. We find no evidence for such a correlation for our full sample (see Table 2). We also find no compelling evidence for correlation for either the Es or S0's tested separately, but the S0's form an essentially random sample, while the Es show at least some weak trend (see Table 2). If there is an underlying (if weak) relationship between the stellar luminosity  $(L_{\star})$  and intrinsic axial ratio of ellipticals/bulges, this relationship will appear weaker due to projection effects. Such a trend is suggested by the result of Kim (1988) that the IRAS 12  $\mu$ m detection rate is significantly higher for round ellipticals than for flattened ones. For S0's, in addition to the bulge there is some contribution from the disk. If S0 disks do, in fact, have significant amounts of cool ISM (as argued in P1), then the total emission at 12  $\mu$ m will be a composite of both stellar emission and diffuse emission from warm grains. The presence of a disk will make the system intrinsically flatter. Furthermore, the more prominent the disk, the more its diffuse ISM will contribute to  $L_{12}$ , and the larger its intrinsic a/b. This will work in the sense of destroying any correlation between  $L_{12}$  and a/b seen for "pure" bulge populations as a manifestation of an intrinsic  $L_*-a/b$  correlation.

We have tested our sample for a possible correlation of  $L_{100}$  with a/b and have found no evidence for any such correlation (see Table 2).

### 4. COMPARISONS WITH Mg.

Mg<sub>2</sub> values are given for 73 of the galaxies in our sample by 7S. Figure 2a shows these data plotted against  $L_{\rm B}$ . The point for NGC 5102 is far off-scale at (0.005, 42.2). However, as this system has an A-type spectrum (Bica & Alloin 1987), it is unlikely that the Mg2 index measures the same physical variable as it is argued to do in typical early-type galaxies. Faber (1973) pointed out that there is a positive correlation between Mg absorption-line strength and  $L_B$  in early-type galaxies (although her original Mg<sub>0</sub> differs slightly from Mg<sub>2</sub>—see Faber, Burstein, & Dressler 1977). Mg<sub>2</sub> is taken to be a variable of metallicity for systems in which the dominant stellar population is old (Terlevich et al. 1981; Buzzoni, Gariboldi, & Mantegazza 1992; Worthey 1994). The conversion between Mg<sub>2</sub> and [Fe/H] used by Terlevich et al. is taken directly from theoretical (Mould 1978) and observational (Burstein 1979) work on K giants and applied without comment to composite galaxy spectra. That of Buzzoni et al. is computed using both observations of Galactic stars, and population synthesis models covering a range of abundances and IMFs. Worthey's (1994) models indicate that the slope and zero point of such a relationship are both functions of the age of the stellar population even without variations in the IMF. Figure 3 shows the loci of the Terlevich et al. and Buzzoni et al. (with a Salpeter IMF) calibrations, and points for Worthey's (1994) models for ages from 1.5 Gyr to 17 Gyr. The agreement between the Terlevich et al. and Buzzoni et al. calibrations becomes quite poor at the lowest metallicities. However, we have only one object with  $Mg_2 < 0.22$ , so that is not a severe problem in our case. The Buzzoni et al. models are computed for a range of IMFs. Changing the IMF mainly affects the zero point of their Mg<sub>2</sub>-[Fe/H] relation, such that a better agreement over our plotted range in Mg<sub>2</sub> is shown by assuming a shallower IMF. Also, the Worthey (1994) models for ages from 8 to 17 Gyr mainly fall between the Terlevich et al. and Buzzoni et al. calibrations.

The Mg<sub>2</sub> index depends on stellar surface gravity and temperature as well as both luminosity and abundance (e.g., Faber et al. 1985). Faber et al. (1985) also point out that high-resolution spectral studies often conclude that the metallicities of strong-lined stars are significantly lower than do medium-and low-resolution studies. Also, recent work (Efstathiou & Gorgas 1985; Worthey, Faber, & Gonzalez 1992; Carollo, Danziger, & Buson 1993) indicates that [Mg/Fe] is not constant among samples of elliptical galaxies. Theoretical work (Stiavelli & Matteucci 1991), and observations of the Galactic bulge (Matteucci & Brocato 1990) and of line-strength gra-

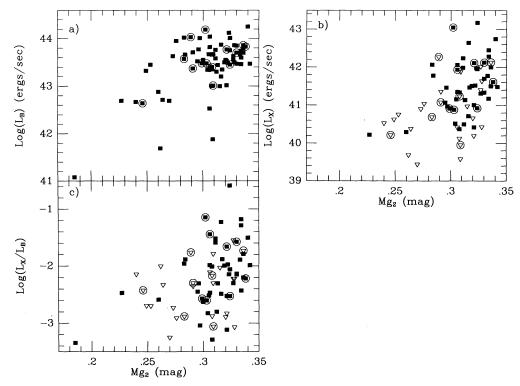


Fig. 2.— $\mathrm{Mg_2}$  vs. (a)  $L_B$ , (b)  $L_X$ , and (c)  $L_X/L_B$  for our sample. Symbols as in Fig. 1.

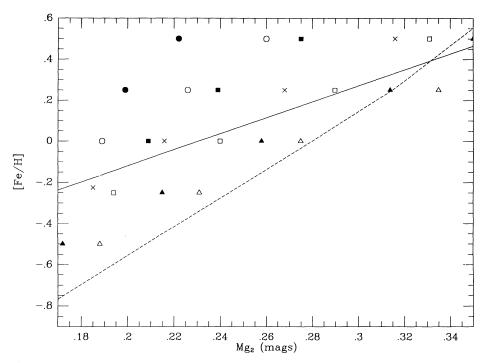


Fig. 3.—Mg<sub>2</sub>-[Fe/H] calibrations from Terlevich et al. (1981), shown as a solid line, and Buzzoni et al. (1992) for a Salpeter IMF, shown as a dashed line. Also shown are points from the models of Worthey (1994) for a Salpeter IMF and ages of 1.5 Gyr (solid circles), 2 Gyr (open circles), 3 Gyr (solid squares), 5 Gyr (crosses), 8 Gyr (open squares), 12 Gyr (solid triangles), and 17 Gyr (open triangles).

dients in ellipticals (Davies, Sadler, & Petetier 1993; Carollo et al. 1993) point to Mg and Fe having very different evolutionary enrichment paths. The principal source for Mg appears to be Type II SNs (Woosley & Weaver 1986), while Type Ia and Ib SNs appear to be the source for the majority of the Fe (Nomoto, Thielemann, & Yokoi 1984; Iben et al. 1987). Furthermore, Worthey et al. (1992) and Worthey (1993) both note that their models (based on fits to field and cluster GK stars, and fits to theoretical isochrones) predict variations in [Mg/Fe] as a function of the age of a stellar population, such that older metal-rich populations will have higher [Mg/Fe] than younger ones of similar [Fe/H] (see Fig. 3). This suggests that some of the scatter in the Mg-Fe trend is due to scatter in the mixture of ages in the stellar populations of early-type galaxies. Finally, Schweizer et al. (1990) note that the magnitude and direction of the scatter about their  $Mg_2-M_B$  relationship have a negative correlation with the  $\Sigma$ -parameters (defined by Schweizer et al. 1990 to quantify fine structure in early-type galaxies), and Bender & Surma (1992) find evidence in four galaxies that Mg<sub>2</sub> increases discontinuously at the same radii as the onset of kinematically decoupled cores in these galaxies. Both of these findings argue that the dynamical history of an early-type galaxy will have a significant effect on its Mg<sub>2</sub> strength.

As the Buzzoni et al. and Worthey (1994) models include at least some of these considerations, it is hoped that they would give a systematically more robust calibration than that of Terlevich et al. However, over the range in  $Mg_2$  populated by our sample, the calibrations for old stellar populations differs by no more than  $\leq 0.15$  dex in [Fe/H], or less than a factor of 2. It appears from this that the use of the  $Mg_2$  index as indicative of trends in abundance in elliptical galaxies is quite reasonable, although the results discussed above indicate that an accurate conversion of  $Mg_2$  measurements to values of [Fe/H] is likely to be unobtainable.

## 4.1. X-Ray and Optical Trends

Accepting the above cautionary note, we conclude that our data show a correlation of higher luminosity with higher metallicity. The results of the correlation tests between Mg<sub>2</sub> and  $L_X$ ,  $L_B$ , and  $L_X/L_B$  are given in Table 2 (NGC 5102) excluded). They all support the impression from the plots in Figure 2. The brightest systems, as well as those systems with the highest  $L_X/L_B$ , are the most metal-rich. This is generally in keeping with current notions of galaxy formation and evolution (e.g., Ferrini & Poggianti 1993 and references therein). We note that the statistically strongest correlation is that between  $Mg_2$  and  $L_X$ . This is borne out by a partial-rank analysis on  $L_B$ - $L_X$ - $L_X/L_B$ -Mg<sub>2</sub> (see Table A2; see Appendix for details on this table). The analysis of this parameter space shows no evidence for any underlying relationship between  $L_B$  and  $Mg_2$ ! The bivariate trend shown in Table 2 is entirely driven by the mutual correlations of both  $Mg_2$  and  $L_B$  on  $L_X$ . This is a very curious result. It may be due to the strong nonlinear relationship between  $L_B$  and  $L_X$  ( $L_X \propto L_B^{\sim 2}$ —see P1). The rapid increase in X-ray flux among the most luminous galaxies could be driving the statistical outcome. Even so, this result indicates that the retention of metals produced in the initial burst of star formation and of a gravitationally bound hot ISM are physically coupled to one another. Both the existence of an X-ray halo and the retention of metals may be tied to the depth and shape of the gravitational potential. In keeping with this interpretation, we note that an  $L_B$ -Mg<sub>2</sub> trend does appear for constant a/b (see Table A2), and that the  $L_x$ -Mg<sub>2</sub> and  $L_x/L_B$ -Mg<sub>2</sub>

trends tend to break down when tested for constant  $\sigma_v$  or  $a_4$  (see Table A2). This matter is discussed further in §§ 5.3 and 6.3 below.

In P1 we demonstrated a correlation between  $L_X$  and the X-ray spectral shape parameter  $C_{21}$ . This parameter is defined as the ratio of counts in the 0.8-1.36 keV band to that in the 0.16-0.8 keV band (Kim et al. 1992a). The trend is in the sense that more luminous galaxies tend to have more pronounced low-energy cutoffs in their X-ray spectra. As discussed in P1, recent ROSAT results (e.g., Fabbiano et al. 1994; Trinchieri et al. 1994; Fabbiano & Schweizer 1994; Kim & Fabbiano 1995) suggest that this is due to a change in the intrinsic source spectrum as a function of  $L_X$  rather than to an increase in intrinsic absorption in high  $L_x$  galaxies. Another possible explanation is that galaxies with higher  $L_x$  tend also to have higher gas-phase abundances. In fact, Trinchieri, Fabbiano, & Canizares (1986) find that some of the brightest X-ray ellipticals would require gas Fe abundances substantially larger than the stellar abundances derived from Mg<sub>2</sub> measurements in order to reduce the derived  $N_{\rm H}$  to the Galactic foreground value. It is quite possible that the two abundance scales are systematically offset. However, recent papers generally claim significantly lower abundances in the hot ISM than those determined for the stellar populations: Recent Ginga measurements of the 6.5 keV Fe line from NGC 1399 and NGC 4472 suggest Fe abundances between solar and 0.3 solar (Awaki et al. 1991; Ikebe et al. 1992). Results from ROSAT (Forman et al. 1993) are in agreement. Results for these same galaxies from BBXRT also suggest subsolar gas abundances (Serlemitsos et al. 1993). These results have, however, been questioned by Renzini et al. (1993). To explore this point further, we tested for a correlation between  $Mg_2$  and  $C_{21}$ . The results are shown in Table 3: There is no significant bivariate correlation between these two quantities for our sample. This result is reinforced by a partial-rank analysis on  $L_B$ - $L_X$ - $L_X/L_B$ - $Mg_2$ - $C_{21}$ : again, we find no evidence for any correlation between  $Mg_2$  and  $C_{21}$  (see Table A2). This suggests that stronger low-energy cutoffs in X-ray-luminous early-type galaxies cannot be related solely to higher metal abundances in the X-ray-emitting gas, unless the metallicity of the ISM is totally unrelated to that of the stars. This result has clear implications for our understanding of the X-ray spectra of early-type galaxies. In particular, it supports modelling of ROSAT data of X-ray-faint galaxies with multicomponent spectra, rather than with very low abundance, single-temperature models (Fabbiano et al. 1994).

# 4.2. Trends with Other ISM Parameters

The same general trend of higher luminosity with higher metallicity is also seen in all other plots of luminosity against Mg<sub>2</sub> (see Fig. 4). Our bivariate analysis (see Table 2) shows that, of these, the strongest relationship is between Mg2 and  $L_6$ . This correlation is, however, weaker than that with  $L_X$ . There is some evidence that  $Mg_2$  is correlated with  $L_{12}$ , but no significant evidence for a correlation with  $L_{100}$ . This supports the notion that the 12  $\mu$ m luminosity is related to the stellar emission (e.g., Jura et al. 1987; Knapp et al. 1992). The 100  $\mu$ m emission may be due to some component that is not intrinsic to the host galaxy (e.g., Forbes 1991). Alternatively, the grains radiating at 100  $\mu$ m may be evaporated by the hot ISM and harsh ISRF characteristic of early-type galaxies (e.g., Boulanger et al. 1988; Knapp et al. 1992). Given that essentially all the objects with Mg<sub>2</sub> values from 7S in our sample are ellipticals, this is in keeping with the lack of correlation between  $L_X$ and  $L_{100}$  found in P1.

Sample	$a/b \ N_{tot}$ Cox-Hazard Kendall's $ au$ Spearman rank	N <sub>lim</sub> prob prob prob	$Mg_2 \ N_{tot}$	N <sub>lim</sub> prob prob prob	$rac{\sigma_v}{N_{tot}}$	N <sub>lim</sub> prob prob prob	a <sub>4</sub> N <sub>tot</sub>	N <sub>lim</sub> prob prob prob
E+S0	39 2.103 0.984 -0.178	0 0.1470 0.3253 0.2734	$28 \\ 0.646 \\ 0.158 \\ -0.030$	0 0.4217 0.8742 0.8744	28 2.494 1.225 0.200	0 0.1143 0.2204 0.2991	19 1.624 1.053 -0.259	0 0.2026 0.2922 0.2710
E	24 1.758 0.722 -0.197	0 0.1849 0.4705 0.3448	22 0.122 0.537 0.073	0 0.7271 0.5915 0.7382	22 0.008 0.677 0.106	0 0.9294 0.4984 0.6265	17 0.263 0.414 -0.102	0 0.6083 0.6792 0.6832
S0	15 1.069 0.698 -0.178	0 0.3011 0.4854 0.5060	$     \begin{array}{r}       6 \\       1.305 \\       1.315 \\       -0.429     \end{array} $	0 0.2533 0.1885 0.3379	6 3.110 1.691 0.657	0 0.0778 0.0909 0.1417	2	0

Note.—Table entries as defined in notes to Table 2.

#### 4.3. The Trend with a/b

We see no relationship in the scatter plot of  $Mg_2$  against a/b, and both the bivariate correlation tests (see Table 4) and partial-rank analysis (see Table A2) confirm this.

### 5. COMPARISONS WITH $\sigma_{n}$

### 5.1. X-Ray and Optical Trends

There are central velocity dispersion measurements [log  $(\sigma_v)$ ] from 7S for 74 galaxies in our sample. Under the reasonable assumption that  $\sigma_v$  measures the depth of the gravitational potential well of a galaxy, and the perhaps somewhat less reasonable assumption that  $L_B$  traces the mass of the galaxy, we would expect a strong positive correlation between

 $L_B$  and  $\sigma_v$  in our sample. This is, in fact what we find (see Fig. 5a and Table 2). The plots against  $L_X$  and  $L_X/L_B$  (Figs. 5b and 5c) show the same sort of relationship. The bivariate correlation analyses given in Table 2 confirm that the relationship is quite strong for  $L_X$  and  $L_X/L_B$ . Given that the sense of the correlation is maintained when we scale the X-ray luminosities by the B-band luminosities in our sample, we conclude that the existence of a deep potential well appears to be crucial for large  $L_X/L_B$  in early-type galaxies (see also FGT). A partial-rank analysis on  $L_B-L_X-L_X/L_B-\sigma_v$  reveals the trends of  $\sigma_v$  with  $L_B$  and  $L_X$  to be of roughly comparable strength, and stronger than that between  $\sigma_v$  and  $L_X/L_B$  (see Table A3; see Appendix for details on this table). These trends indicate that total luminous mass and hot ISM content are both linked to the depth of

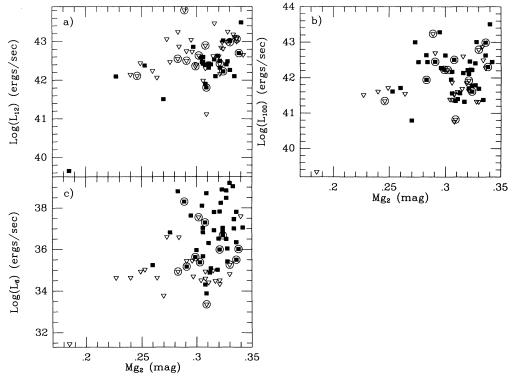


Fig. 4.— $\mathrm{Mg_2}$  vs. (a)  $L_{12}$ , (b)  $L_{100}$ , and (c)  $L_6$  for our sample. Symbols as in Fig. 1.

TABLE 4
BIVARIATE CORRELATION TESTS ON THE STRUCTURAL DATA

	a/b		$Mq_2$		$\sigma_v$	
	$N_{tot}$	$N_{lim}$	$N_{tot}$	$N_{lim}$	$N_{tot}$	$N_{lim}$
	Cox-Hazard	prob		prob		prob
	Kendall's $ au$	prob		prob		prob
	Spearman rank	prob		prob		prob
$Mg_2$	73	0				
-	1.356	0.2442				
	0.940	0.3472				
	-0.101	0.3908				
$\sigma_v$	74	0	74	0		
	1.383	0.2396	46.057	$< 10^{-4}$		
	2.150	0.0316	5.284	$< 10^{-4}$		
	-0.249	0.0331	0.576	$< 10^{-4}$		
$a_4$	47	0	43	0	43	0
	11.247	0.0008	0.135	0.7138	8.150	0.0043
	2.510	0.0121	0.252	0.8013	2.369	0.0179
	0.374	0.0112	0.027	0.8630	-0.342	0.0265
a4	44	0	40	0	40	0
no dEs	11.472	0.0007	0.577	0.4477	11.649	0.0006
	2.829	0.0047	0.420	0.6743	3.278	0.0010
	0.421	0.0058	-0.079	0.6201	-0.515	0.0013

NOTE.—Table entries as defined in notes to Table 2.

the potential well; a satisfying, if not terribly surprising result. The  $L_X$ - $\sigma_v$  and  $L_X/L_B$ - $\sigma_v$  trends do tend to weaken somewhat when tested for constant  $a_4$ , but this appears to be due mainly to the decrease in sample size (from 73 to 40 objects) when  $a_4$  is considered.

## 5.2. Trends with Other ISM Parameters

For the 6 cm data, the distribution looks more like a threshold relation than a linear correlation (see Fig. 6). For log

 $(\sigma_v)\lesssim 2.2$  (measured in km s<sup>-1</sup>) there are no detected 6 cm radio sources with luminosities greater than  $10^{35}$  ergs s<sup>-1</sup>. Above this threshold, there are immediately systems with 6 cm luminosities of  $\approx 10^{39}$  ergs s<sup>-1</sup>. The *IRAS* data at both 12  $\mu$ m and 100  $\mu$ m (also shown in Fig. 6) suggest positive correlations also, but do not appear as strong as those with either  $L_X$  or  $L_6$ . This impression is confimed by the bivariate analysis in Table 2: The correlations with the *IRAS* luminosities are significant at the 0.1%-1% level. The optical, radio, and X-ray corre-

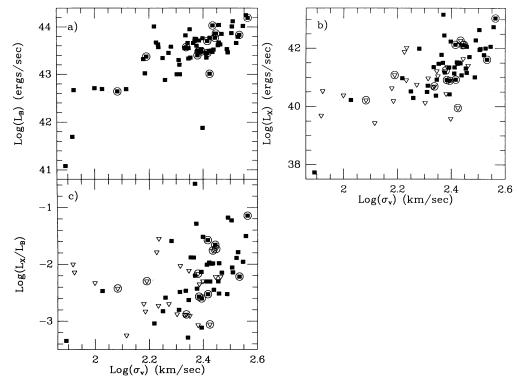


Fig. 5.— $\sigma_v$  vs. (a)  $L_B$ , (b)  $L_X$ , and (c)  $L_X/L_B$  for our sample. Symbols as in Fig. 1.

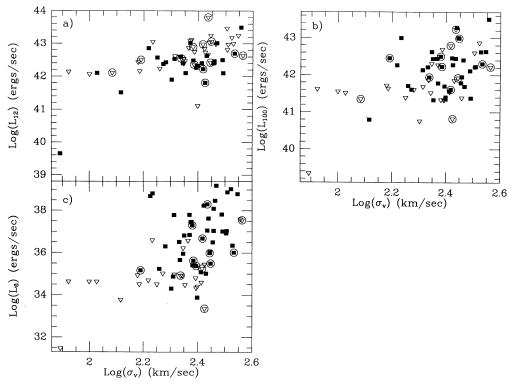


Fig. 6.— $\sigma_v$  vs. (a)  $L_{12}$ , (b)  $L_{100}$ , and (c)  $L_6$  for our sample. Symbols as in Fig. 1.

lations are all significant at levels of <0.01%. This suggests a picture in which the fuel source (cooling X-ray gas) and feeding rate (which determines the radio power) of the central engine are both directly coupled to the central potential depth, in keeping with the notions of FGT.

## 5.3. Trends with Other Structural Parameters

It is not surprising that we should find a good correlation between Mg<sub>2</sub> and  $\sigma_v$  for our sample, given that these data are drawn from 7S, who find such a correlation for their full sample (also see Bender 1992). The results for our objects are shown in Figure 7b and Table 4. It is somewhat surprising that the correlation between a/b and  $\sigma_n$  is so weak, however (see Fig. 7a and Table 4). While there is a general trend for the galaxies with the largest values of  $\sigma_v$  to be the roundest, the data are not at all compelling. Partial-rank analysis shows that the only example of a significant  $a/b-\sigma_n$  trend occurs for constant  $L_B$ , in the sense that galaxies with deeper potential wells tend to be rounder than those with shallow potential wells. This could be because there is more internal support from rotation in the flatter systems at a given luminosity. There is a very strong correlaton between  $Mg_2$  and  $\sigma_v$  for all tested combinations (see Table A3); see Appendix for details on this table).

# 6. COMPARISONS WITH $a_{\lambda}$

## 6.1. X-Ray and Optical Trends

We have taken measurements of the amplitude of the cos (4  $\theta$ ) Fourier term of the isophotal deviations from ellipticity for 47 galaxies in our sample from the papers of Bender et al. (1989) and Peletier et al. (1990). These data are given in Table 1. These  $a_4$  values are measured from isophotes at  $\lesssim 2r_e$  (typically  $\sim 0.5r_e$  for the Peletier et al. sample), and thus describe the

morphology of the inner parts of these galaxies. In Figure 8a we show that our sample is representative of the full samples of these earlier studies in that more luminous ellipticals tend to be boxy (have negative  $a_4$  terms), while the less luminous tend to be disky (positive  $a_4$ ). The exceptions to this are three boxy dwarf ellipticals, marked in the figure. Recent work (e.g., Bender & Nieto 1990; Carter & Sadler 1990; Held, Mould & de Zeeuw 1990; Bender, Paquet, & Nieto 1991) indicates that these galaxies do not fall along a simple extension of the properties of giant ellipticals. This deviation is therefore neither surprising nor (for the work discussed here!) terribly significant.

Bender et al. (1989) comment that they see a relationship between  $L_X$  and  $a_4$  for their sample. They do not test for such a relationship, possibly due to the very small number of objects for which they had X-ray data. Our sample is substantially larger (see Figs. 8b and 8c). The results of the bivariate correlation analysis of  $a_4$  with  $L_B$ ,  $L_X$ , and  $L_X/L_B$  are given in Table 2. This analysis confirms the assertion of Bender et al. (1989) that X-ray-luminous galaxies tend to be boxier than X-rayfaint galaxies at the  $\sim 0.1\%$  level if the dE's are not included. The strength of the bivariate correlation with  $L_B$  is marginally worse than that with  $L_X$ . The trend with  $L_X/L_B$ , again in the sense that the galaxies with the highest  $L_X/L_B$  tend to be boxy, is statistically the weakest of the three, but the correlation is still significant at a level of  $\lesssim 0.5\%$  for all three tests. Partialrank analysis on  $L_B$ - $L_X$ - $L_X/L_B$ - $a_4$  reveals that the trend of  $L_X$ with  $a_4$  is the strongest of the three and appears to drive the other two (see Table A4; see Appendix for details on this table). The  $L_x$ - $a_4$  trend breaks down when tested for constant  $\sigma_v$ . We noted in § 5.1 that there is a strong  $L_x$ - $\sigma_v$  trend. This trend is maintained for constant  $a_4$  (see Table A3), arguing that an underlying trend between  $a_4$  and  $\sigma_v$  is driving the  $L_{X}$ - $a_4$  correlation. We explore this result further in § 6.3 below.

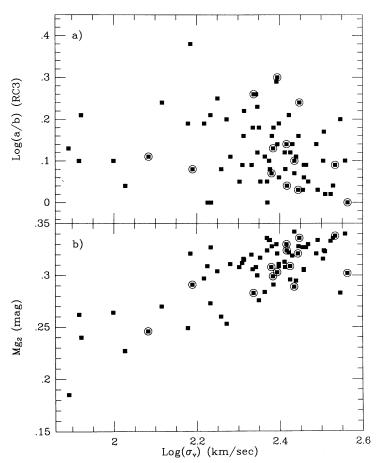


Fig. 7.— $\sigma_v$  vs. (a) a/b, and (b) Mg<sub>2</sub> for our sample. Symbols as in Fig. 1.

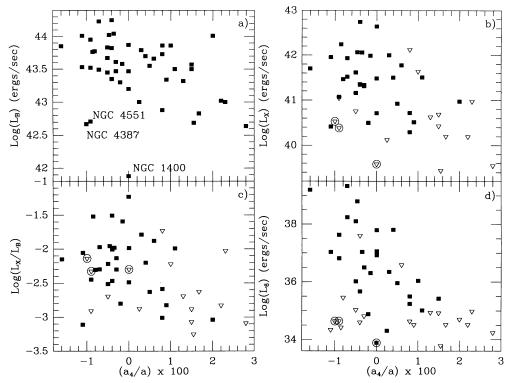


Fig. 8.— $a_4$  vs. (a)  $L_B$ , (b)  $L_\chi$ , (c)  $L_\chi/L_B$ , and (d)  $L_6$  for our sample. The dwarf ellipticals are identified in (a), and circled in (b), (c), and (d). All other symbols as in Fig. 1.

#### 6.2. Trends with Other ISM Parameters

There are trends of marginal statistical significance between  $a_4$  and both  $L_{12}$  and  $L_{100}$ , at the  $\lesssim 6\%$  and  $\lesssim 4\%$  confidence levels respectively (see Table 2). A strong trend is apparent between  $a_4$  and  $L_6$  in Figure 8d. This correlation is confirmed at roughly the 0.1% level (Table 2). There are no highluminosity 6 cm sources in our sample that are disky galaxies. This is in keeping with previous findings that central radio sources are more prevalent in ellipticals without disk features (Peletier et al. 1990). A partial-rank analysis including  $L_6$  indicates that the relationship between  $L_6$  and  $a_4$  is stronger than that between  $L_B$  and  $a_4$  (see Table A4), although weaker than the  $L_X$ - $a_4$  correlation: Boxy galaxies generate more radio power than disky galaxies of the same optical and X-ray luminosities.

The picture that emerges from our consideration of the relationship of structural parameters to the luminosities in our various wavebands is that  $L_B$ ,  $L_X$ ,  $L_X/L_B$ , and  $L_6$  are correlated with both the depth of the potential (as measured by  $\sigma_v$  and  $\mathrm{Mg}_2$ ) and the shape of the potential (as measured by a/b and  $a_4$ ).

### 6.3. Trends with Other Parameters

We find a correlation at the  $\sim 0.5\%$  level (see Table 4) between  $a_4$  and a/b in the sense that rounder galaxies tend to be boxy, and flatter galaxies tend to be disky. This is not a tautology: recall that a/b simply measures the ratio of the projected major and minor axes of a system;  $a_4$  measures the extent and sense of deviation of the isophotes of a system from pure elliptical symmetry. It is entirely possible, from a mathematical point of view, for a system with high ellipticity to have boxy isophotes, or one with very low ellipticity to have disky

isophotes. The data are shown in Figure 9a. A partial-rank analysis on  $L_{B}$ - $L_{X}$ - $L_{X}$ / $L_{B}$ -a/b-a4 supports this picture (see Tables A1 and A4) but suggests that the a/b-a4 trend may be largely driven by underlying relationships of both a4 and a/b with the luminosity parameters.

Much to our surprise, the data show no indication for a correlation between  $a_4$  and  $Mg_2$  (see Fig. 9b and Table 4). One might expect there to be a relationship between these such that boxy galaxies would tend to have higher  $Mg_2$  than disky galaxies. Indeed, Sil'chenko (1994) finds some evidence for just such a result. However, if anything, the data we have show an opposite trend: the lowest values of  $Mg_2$  tend to be from boxy galaxies. Overall, though, there is no indication from this sample for any significant trend. A partial-rank analysis on  $L_B-L_X-L_X/L_B-a/b-a_4-Mg_2$  confirms this result (see Table A4).

With the exception of two dwarf galaxies, we see a steep correlation between  $a_4$  and  $\sigma_v$  for our sample (see Fig. 9c), in the sense that boxy galaxies tend to have large velocity dispersions. For the full sample this correlation is significant at the ~2.7% level (see Table 4). Removing the dwarfs galaxies improves this to a  $\sim 0.1\%$  correlation. A partial-rank analysis on  $L_B$ - $L_X$ - $L_X$ / $L_B$ -a/b- $a_4$ - $\sigma_v$  suggests that this correlation may be the underlying cause of the observed relation between  $a_{\perp}$ and a/b (see Table A4). Testing  $L_B-L_X-L_X/L_B-a/b-a_4-Mg_2-\sigma_v$ , we find statistical evidence for a positive correlation between  $a_4$  and Mg<sub>2</sub> at the ~4%-5% level. We note that this correlation appears only when we test for a constant  $\sigma_v$ . This therefore implies that, for a given potential depth, disky galaxies have higher metallicity or older stellar populations than boxy galaxies. We also note that the strongest  $\sigma_v$ - $a_4$  correlations all result when tested with constant Mg<sub>2</sub> (see Table A4). The effect of Mg<sub>2</sub> can be seen in Figure 9c where the points enclosed in

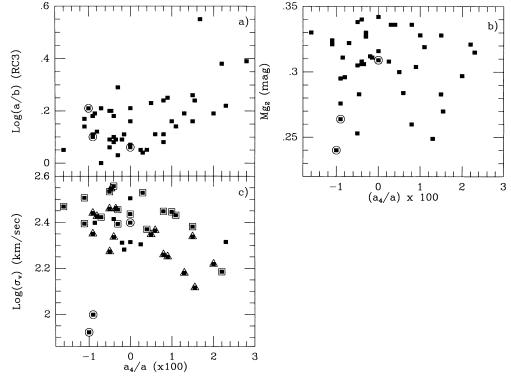


Fig. 9.— $a_4$  vs. (a) a/b, (b) Mg<sub>2</sub>, and (c)  $\sigma_v$  for our sample. Symbols as in Fig. 8. In (c) the points enclosed in squares are the systems with the highest 40% of Mg<sub>2</sub> values; those enclosed in triangles are the lowest 40%.

squares are the 40% of the sample with the largest  $Mg_2$  values, and those enclosed in triangles are the 40% with the smallest  $Mg_2$  values. For a given  $a_4$  value, the high- $Mg_2$  objects have systematically higher  $\sigma_v$  than the low- $Mg_2$  objects.

One possible interpretation of these results is suggested by the hypothesis that boxy ellipticals are the product of mergers of smaller systems, while disky ellipticals are "primordial" in the sense that the overall morphology of the system is a reflection of its state at the epoch of galaxy formation (e.g., Nieto & Bender 1989; Kormendy & Djorgovski 1989; Barnes & Hernquist 1992). At the present epoch, there appears to be a massabundance relationship amongst galaxies of a given morphology (e.g., Faber 1973; Wyse & Silk 1985; Dekel & Silk 1986; DeYoung & Gallagher 1990; Franx & Illingworth 1990) such that less massive systems are less metal-rich. If such a relationship has always held, then the formation of a boxy E of some mass M from two smaller objects would result in a lower abundance galaxy than a disky E of the same mass M if the bulk of the stars in the boxy galaxy had already formed before the merger. Furthermore, boxy galaxies that formed from the merging of lower mass progenitors will result in objects with lower current stellar abundances compared to those formed from the merging of higher mass progenitors, because a larger fraction of the enriched ejecta from the initial merger induced burst of star formation will escape from their shallower potential wells.

A second possibility is that disky systems are the products of mergers involving at least one disk galaxy, in which either the self-gravitating part of the disk survives the accretion event (as may be the case in Cen A), or the ISM undergoes dissipational collapse to form a new central disk system (e.g., Hernquist & Barnes 1991). This is the most reasonable explanation for galaxies with kinematically decoupled cores (e.g., Bender 1990; Bertola 1992) and may hold for disky galaxies in general. This is because both the studies of Bender et al. (1989) and Peletier et al. (1990) determine the  $a_4$  parameter at fairly small radii. Bender et al. (1989) state that all their  $a_4$  values are computed from isophotes within  $2r_e$ . Peletier et al. (1990) publish the radii at which they determined  $a_4$ . The mean is  $\sim 0.5r_e$ , with a few as low as  $0.1r_e$ , and only three of 35 galaxies  $\geq 1r_e$ . Thus "disky" systems are so labeled because their inner isophotes have disk features. Several of the systems with negative  $a_4$  from the Bender et al. (1989) sample have very boxy isophotes at large radii (F. Schweizer 1994, private communication) and thus appear to be merger remnants on that criterion. Bender & Surma (1992) observed four ellipticals with kinematically decoupled cores and found a sharp increase in the Mg<sub>2</sub> line strengths at the same radii at which the peculiar kinematics appear. As the Mg<sub>2</sub> values from 7S are all nuclear values, the trend of higher Mg2 line strengths in disky systems at a given  $\sigma_v$  may be due to higher abundances in the captured or secondary nuclear disks of merger remnants with disky central isophotes.

### 7. SUMMARY AND SUGGESTIONS FOR FUTURE RESEARCH

1. Rounder galaxies tend to have larger  $L_X$ ,  $L_X/L_B$ , and  $L_6$ . Partial-rank analysis shows the  $L_X/L_B$ -a/b trend to be the strongest of the three. This suggests a connection between the shape of the potential and the ability to retain substantial halos of hot ISM. These in turn could be responsible for both feeding the nuclear sources through cooling flows and confining radio lobes (see also FGT). The same general trends hold for corre-

lations with  $a_4$ , but the strongest trend here is that between  $a_4$  and  $L_X$  (confirming the observation of Bender et al. 1989).

- 2. Axial ratio (a/b) and boxiness  $(a_4)$  are correlated in the sense that flatter galaxies tend to have diskier isophotes. Partial-rank analysis suggests that the trends between  $a_4$  and a/b may be driven by underlying relationships of both axial ratio and  $a_4$  with the luminosity parameters.
- 3. Both a/b and  $a_4$  are correlated with  $L_B$  but are not strongly correlated with either  $L_{12}$  or  $L_{100}$ . The lack of any strong trend with  $L_{12}$ , and the results of P1, indicate that there may be some significant contribution to the 12  $\mu$ m emission from hot dust in early-type galaxies that is not directly related to the stellar component. For the S0's, there may be a contribution from dust associated with disk star formation regions. The lack of trends with  $L_{100}$  is consistent with the notion that the FIR-emitting material is accreted (e.g., Forbes 1991), or that it is evaporated by the hot ISM and hard ISRF on fairly short timescales (e.g., Knapp et al. 1992).
- 4. There are strong correlations between  $Mg_2$ ,  $\sigma_v$ , and  $L_X$ . Partial-rank analysis shows that the depth of the potential well is the crucial parameter. From a physical standpoint, the deeper the potential well, the better a galaxy is able to retain its hot ISM at the current epoch (the  $L_X$ - $\sigma_v$  correlation), and the better it was able to retain the enriched ejecta from its initial phase of strong star formation, and reprocess this ejecta into new stars (the  $Mg_2$ - $\sigma_v$  correlation).
- 5. There is no significant correlation between the X-ray spectral parameter  $C_{21}$  and  $Mg_2$ .  $C_{21}$  is defined by Kim et al. (1992a) as the ratio of emission in the 0.8–1.36 keV band to that in the 0.16–0.8 keV band and thus measures the shape of the X-ray spectrum in this region. The lack of correlation between  $C_{21}$  and  $Mg_2$  suggests that the relative absence of low-energy cutoffs in X-ray-faint early-type galaxies (see Kim, Fabbiano, & Trinchieri 1992b) is not related to lower abundances in the X-ray-emitting gas, unless the metallicity of the ISM is unrelated to that of the stars. This supports the conclusion of Fabbiano et al. (1994) that X-ray-faint ellipticals have complex X-ray spectra.
- 6. Many of the trends we find are "wedgelike" or "threshold-like" rather than being a simple power law. One of the most impressive of these is the  $L_6$ - $\sigma_v$  trend discussed in § 5.2. We find a threshold of  $\log{(\sigma_v)} \approx 2.2$  above which the maximum radio luminosities in our sample jump abruptly by more than an order of magnitude. Below this value of  $\sigma_v$ , it appears that the potential well is too shallow to efficiently transport material to the nuclear engine. It does not seem coincidental that, at this same value of  $\sigma_v$ , we see a jump in the maximum detected  $L_\chi/L_B$  of more than one order of magnitude.
- 7. X-ray, radio, and optical luminosities are all correlated with both shape  $(a/b, a_4)$ , and depth  $(Mg_2, \sigma_v)$  parameters. There are also strong relationships among the shape and the depth parameters. However, trends between the shape parameters  $(a/b, a_4)$  and one of the depth parameters  $(Mg_2 \text{ or } \sigma_v)$  are modulated by the other parameter. That is, for instance, at a given  $a_4$  value, the spread in  $\sigma_v$  appears directly related to the spread in  $Mg_2$  such that the higher  $\sigma_v$  objects also have higher  $Mg_2$ . Alternatively, for a given  $\sigma_v$ , boxy galaxies tend to have lower  $Mg_2$  values (and thus, we surmise, lower stellar abundances) than disky galaxies. This suggests that the presence of a hot ISM is dependent on both the shape  $(a/b, a_4)$  and the depth  $(Mg_2, \sigma_v)$  of the potential, but that these two families of parameters are not related in a simple way.

The nature of the coupling between the shape and depth parameters is clearly an important input for understanding the formation and evolution of early-type systems. A galaxy may have a deep potential either because of initial conditions (the result of a large primordial fluctuation) or because it is the product of mergers of a number of less massive objects. We observe that Es with disky inner isophotes have larger nuclear Mg<sub>2</sub> strengths than galaxies with boxy inner isophotes at a given  $\sigma_v$ . If disky isophotes signal "primordial" ellipticals (ones that have not experienced significant merging since the epoch of galaxy formation) and boxy isophotes signal systems that have been built up by mergers, two possible explanations of this result suggest themselves. First, if the presently observed mass-abundance relationship for galaxies is a relic of a fundamental constraint of the galaxy formation process, then a disky elliptical of a given mass could have a higher average central stellar abundance than a merger product (a boxy elliptical) of the same mass that was formed from lower mass (and thus lower abundance) precursors. Second, boxy ellipticals could have lower Mg<sub>2</sub> values for a given [Fe/H] due to an overall younger stellar population resulting from merger-induced star formation bursts. Alternatively, if disky isophotes signal merger systems that have either formed secondary nuclear disks (see Hernquist & Barnes 1991), or captured selfgravitating spiral disks, then the enhancement of nuclear Mg<sub>2</sub> strengths at a given  $\sigma_v$  may be due to high abundances in those disks (see Bender & Surma 1992).

Various avenues present themselves for further study of

these possibilities. One that we are pursuing is the comparison of the database from this work and P1 with the dynamically motivated  $\kappa$ -parameters defined by Bender, Burstein, & Faber (1992). It would also be very interesting to study the radial gradients of  $Mg_2$  and  $\sigma_v$  for early-type galaxies with a range in X-ray properties and to look for other signs of fine structure (as discussed by, e.g., Schweizer & Seitzer 1992) as a function of X-ray properties. Such studies ought to make great contributions to our understanding of the formation histories and physical evolution of early-type galaxies.

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TABLE A1a Partial Spearman Rank Analysis: Trends with  $\log{(a/b)}$ , E + S0 Sample

Test Pair	Held parameters	Size	Paritial Spearman rank	Probability
$L_{B}$ - $a/b$	$L_X$	147	-0.047	0.287
	$L_X/L_B$	147	-0.108	0.099
	$Mg_2$	73	0.066	0.292
	$\sigma_{m{v}}$	74	0.176	0.072
	$a_4$	44	-0.138	0.199
	$L_X, L_X/L_B$	147	-0.030	0.361
	$L_X,\!Mg_2$	73	0.254	0.019
	$L_X,\!\sigma_v$	74	0.277	0.010
	$L_X,a_4$	44	0.024	> 0.400
	$L_X/L_B,\!Mg_2$	73	0.197	0.051
	$L_X/L_B,\!\sigma_{m v}$	74	0.231	0.026
	$L_X/L_B,a_4$	44	-0.063	0.349
	$L_6,a_4$	44	-0.004	> 0.400
	$Mg_2,\!\sigma_v$	73	0.164	0.090
	$Mg_2,a_4$	40	0.057	0.368
	$\sigma_v, a_4$	40	0.197	0.125
	$L_X,\!L_X/L_B,\!Mg_2$	73	0.278	0.010
	$L_X, L_X/L_B, \sigma_v$	74	0.282	0.009
	$L_X, L_X/L_B, a_4$	44	0.015	> 0.400
	$L_X, L_6, a_4$	44	0.076	0.319
	$L_X,\!Mg_2,\!\sigma_{\boldsymbol{v}}$	73	0.274	0.012
	$L_X,\!Mg_2,\!a_4$	40	0.120	0.241
	$L_X,\!\sigma_v,\!a_4$	40	0.211	0.108
	$L_X/L_B, L_6, a_4$	44	0.026	> 0.400
	$L_X/L_B, Mg_2, \sigma_v$	73	0.223	0.035
	$L_X/L_B,\!Mg_2,\!a_4$	40	0.098	0.283
	$L_X/L_B,\!\sigma_v,\!a_4$	40	0.200	0.125
	$Mg_2,\!\sigma_v,\!a_4$	40	0.170	0.169
	$L_X, L_X/L_B, L_6, a_4$	44	0.070	0.336
	$L_X,\!L_X/L_B,\!Mg_2,\!\sigma_v$	73	0.283	0.010
	$L_X, L_X/L_B, Mg_2, a_4$	40	0.116	0.249
	$L_X, L_X/L_B, \sigma_v, a_4$	40	0.201	0.127
	$_{L_X,Mg_2,\sigma_{\boldsymbol{v}},a_{\boldsymbol{4}}}$	40	0.182	0.155
	$L_X/L_B, Mg_2, \sigma_v, a_4$	40	0.173	0.168
	$L_X, L_X/L_B, Mg_2, \sigma_v, a_4$	40	0.173	0.171

### **APPENDIX**

Tables A1-A4 contain the detailed results of the partial Spearman rank statistical analysis. Table A1 shows the analysis of  $L_B$ -a/b,  $L_X$ -a/b,  $L_X$ - $L_B$ -a/b, and  $L_G$ -a/b. Table A2 shows  $L_B$ -Mg<sub>2</sub>,  $L_X$ -Mg<sub>2</sub>,  $L_X$ -Mg<sub>2</sub>,  $L_X$ -Mg<sub>2</sub>, and a/b-Mg<sub>2</sub>. Table A3 shows  $L_B$ -a/v,  $L_X$ 

Tables A1-A4 are published in their entirety in computer-readable form in the AAS CD-ROM Series, Volume 4. A portion of Table A1a appears on the preceding page.

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