

# Solar DEM Models

$$\frac{I_b \tau_b}{\sqrt{I_b \tau_b + \sigma_b^2}} = \frac{(\sum_{t=1}^T \beta_t M_{bt}) \tau_b}{\sqrt{I_b \tau_b + \sigma_b^2}} + \text{RandomGaussianField}$$

$I_b$  : A solar image in color band  $b$ ,  $m \times n$  pixels, containing a particular solar feature, for  $b = 1, 2, \dots, B$

$M_{bt}$  : The expected *Emission Measure in color band  $b$  originating at temperature  $t$* , for  $t = 1, 2, \dots, T$ .

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$\beta_t$  : the proportion of the total volume at temperature  $t$ .

$e_{ijb}$  : the measure error of the  $i$ th row and  $j$ th column pixel of the certain image in color band  $b$ .

$\sigma_b$  : computed from the magnitude of the negative values of  $I_b$  in the data.

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Assumptions:

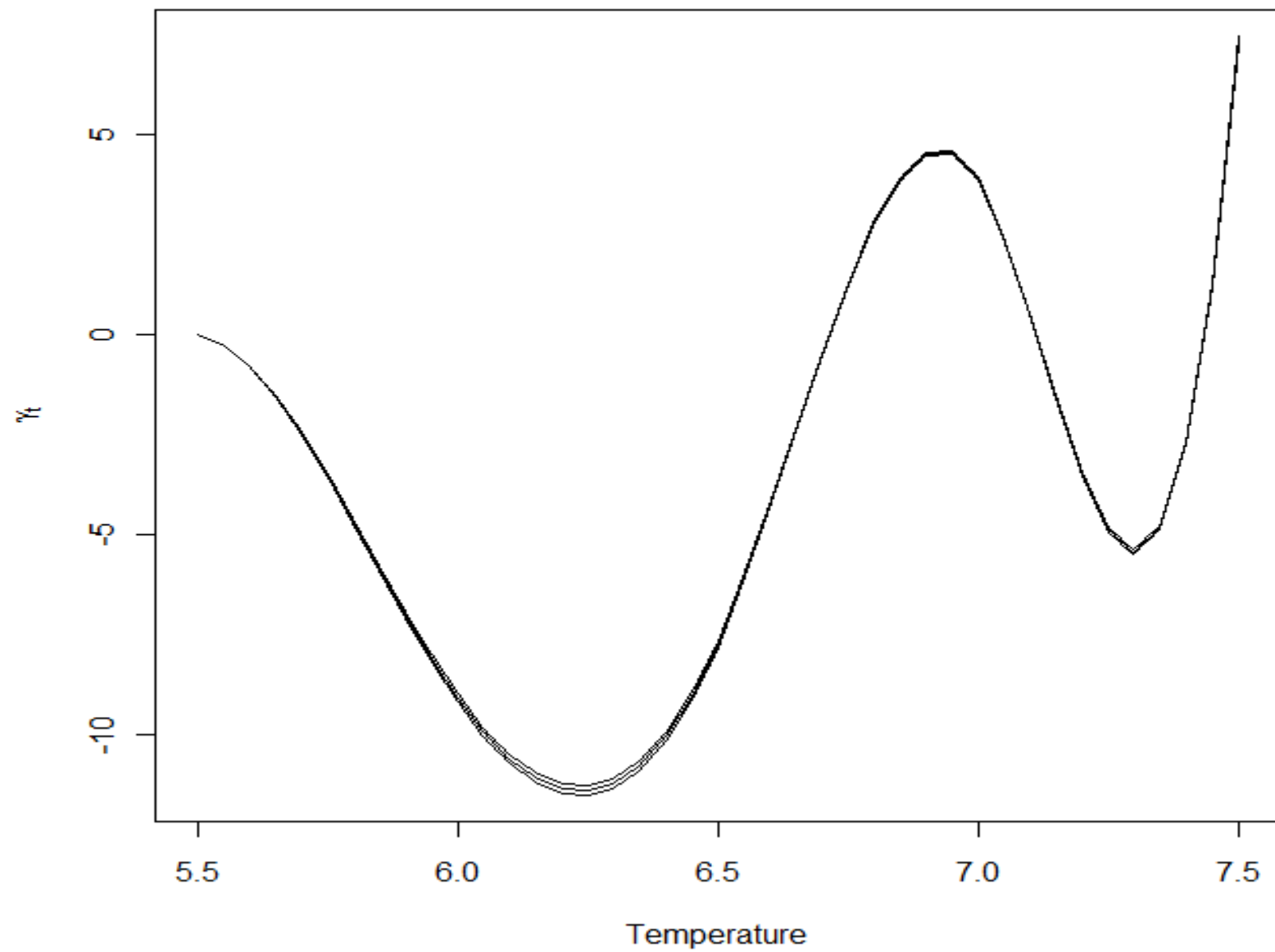
- 1.Errors in different color bands are independent.
- 2.Errors in the same color band have exponential covariance model, that is:

$$\text{Cov}(\hat{e}_{ijb}, \hat{e}_{mnb}) = \text{Nugget}_b + \text{Var}_b * \text{Exp}\left\{-\frac{|ij - mn|}{\text{Scale}_b}\right\}$$

# Use CM algorithm, it converges...

```
> Beta
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```
      [,1]      [,2]      [,3]      [,4]      [,5]      [,6]      [,7]
[1,]  0.018073756  0.5063130  10.10641   9.94494 -13.97194  14.40147 -7.284121
[2,] -0.001229361 -0.5544484 -25.07788 -28.38127  39.73250 -40.37617  19.254062
[3,] -0.001209625 -0.3852280 -14.13066 -15.76870  21.58390 -21.19361   9.469062
[4,] -0.001088313 -0.3346946 -11.82067 -13.24685  17.91289 -17.28480   7.461128
[5,] -0.001081804 -0.3323187 -11.71705 -13.13515  17.74959 -17.10950   7.369508
[6,] -0.001081777 -0.3323136 -11.71680 -13.13495  17.74918 -17.10888   7.369019
[7,] -0.001081774 -0.3323127 -11.71676 -13.13490  17.74912 -17.10882   7.368988
[8,] -0.001081774 -0.3323127 -11.71676 -13.13491  17.74912 -17.10882   7.368988
```



# Other Solar DEM Models

$$\frac{I_b}{\sqrt{I_b \tau_b + \sigma_b^2}} = \frac{(\sum_{t=1}^T \beta_t M_{bt}) \tau_b}{\sqrt{I_b \tau_b + \sigma_b^2}} + \text{RandomGaussianField}$$

$$\frac{I_b \tau_b}{\sqrt{I_b \tau_b + 1/4}} = \frac{(\sum_{t=1}^T \beta_t M_{bt}) \tau_b}{\sqrt{I_b \tau_b + 1/4}} + \text{RandomGaussianField}$$

$$I_b = (\sum \beta_t \cdot M_{ijb}) \cdot \tau_b + N(f(I_b), \sigma_{ijb})$$